# A Novel Design of Microwave Absorbers Based on Multilayered Composite Materials for Reduction of Radar Cross Section

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Abstract - Reduction of radar cross section (RCS) for targets can be achieved by different approaches and coating absorbing materials at the surfaces of targets is one of widely used methods because of its flexibility and good effect. In the work, we put forward a novel method of reducing the RCS based on the design of multilayer composite absorbing materials. The transmission line theory and particle swarm optimization (PSO) are used to guide the design and analysis, and two kinds of designs, i.e., Type IV and Type VII, are selected finally. Simulation experiments show that the designs are insensitive to the incident angles and polarizations of incident EM wave, which is required for being coated at the surfaces of real objects. Also, the designed absorbing materials are very thin and have an ultra-wide frequency band. The bandwidth of Type-IV design can reach 14.63 GHz, ranging from 3.37 to 18.0 GHz, while Type-VII design can cover the frequency range from 2.0 to 18.0 GHz, which represents the major part of radar's frequency range. The designed absorbing materials are coated at the surface of a perfectly-electric-conducting (PEC) cylinder to validate the effectiveness of the materials, and good results have been obtained.

*Index Terms* – Microwave absorber, absorbing media, radar cross section, transmission line theory, particle swarm optimization.

### I. INTRODUCTION

Radar cross section (RCS) is a measure for the strength of electromagnetic (EM) fields scattered by targets and reducing the RCS as much as possible is the basic requirement for designing stealth targets [1]. With the significant development of radar techniques since World War II, reducing the RCS of targets has become a passive and indispensable technique for reducing the detectability of targets [2] and has been eagerly needed in military applications or even in some civilian applications [3]. Generally, there are four categories of techniques for reducing the RCS, i.e., design of geometric shape, coating of microwave absorbing material, passive cancelation, and active cancelation [4]. Each method has its advantages and disadvantages. Compared with the other three methods, coating the absorbing materials could be the most important because it is flexible, cost-effective, of good performance, and has been widely applied in the RCS reduction for the targets like airplanes, ships, missiles, etc., or even used in the interference shielding of some targets [5–7].

The reduction of RCS by covering appropriate absorbing materials is a very hot research topic and many researchers have been dedicated to working on the topic for a long time. The earliest microwave absorber can date back to the early 1940s when Winfield Salisbury invented the Salisbury screen [8]. After that, various microwave absorbers, such as the Jaumann screen, the Dallenbach layer, the frequency selective surface, etc., were proposed and have been developed for many years [9-13]. In recent years, the metamaterial as a novel absorbing material has caught up a wide attention [14]. Although the metamaterial has the property that can greatly extend the parameter space accessible with natural materials, it has some obvious drawbacks in practical applications. The metamaterial absorbers usually have a narrow bandwidth [15] although they could be insensitive to the incident angles and polarizations of incident waves which is also very desirable. He and Jiang proposed a kind of metamaterial absorber that had shown a wideband absorption, but it still cannot cover a wider frequency range which most of the radars are using [16]. Also, some metamaterial absorbers are actually sensitive to the incident angles and polarizations of incident waves, greatly reducing their applicability.

Compared with the metamaterial, some composite materials have shown a better performance, i.e., they can not only cover a much wider frequency range but also be insensitive to the incident angles and polarizations [17]. Thanks to the significant progress of material science, it has become feasible to synthesize composite materials that have much lower or higher EM parameters which allow to extensively adjust the performance of materials [18]. Yuan *et al.* proposed an ultrathin broadband composite absorbing material which has an operating bandwidth ranging from 4.0 to 18.0 GHz [19]. Ali *et al.* presented the design of novel and lightweight microwave absorbers, which also exhibited a broad bandwidth of 3.74 GHz [20]. Ling *et al.* designed a broadband absorbing material whose effective absorption bandwidth reaches 12.6 GHz and total thickness is only 2.3 mm [21].

All designs for the microwave absorbers in the above are assumed to work on an infinitely large plate and their EM performance is also obtained under this assumption. However, real objects like airplanes have curvilinear surfaces that could include finite plates, corners, and othershaped parts in various sizes. As a result, the absorbers are required to possess a stable performance when incident waves are of different incident angles and polarizations. Some composite materials like carbonyl iron powders (CIPs) [22] have been proven to be insensitive to the incident angles and polarizations so that they can be used as such absorbers [23]. The existing materials have the problems of narrow operation bandwidth. Meanwhile, the relative bandwidths of the absorbing materials which are suitable for the detection frequency band of the radar are small. In the operation frequency band, the existing materials also have the disadvantages of low absorptivity and angle sensitivity and the EM parameters of which are instable neither. The existing design methods often determine the final structure through the analysis of EM parameters or repeated simulation. This method costs a lot of time and may not necessarily obtain the best iterative convergence result under this condition.

In this work, we propose a novel method to design the absorbers for reducing the RCS of some objects. Since most of the radar systems are working at the frequency range from 2.0 to 20.0 GHz, we try to design the absorbers that can cover most of radar's frequency range, i.e., from 2.0 to 18.0 GHz. We apply the transmission line theory (TLT) and particle swarm optimization (PSO) to the design of multilayered absorbers which are composed of two types of CIP composite materials. We then choose two representative designs to investigate their performance on the reduction of RCS under the different incident angles and polarizations of incident waves. Based on the simulation experiments, we can find the best design of absorbers that are most insensitive to the incident angles and polarizations. Finally, the designed absorbers are coated on the surface of a perfectly-electric-conducting (PEC) cylinder and we demonstrate that the designed absorbers can perform well for real objects.

## **II. MICROWAVE ABSORBING MATERIALS**

Microwave absorbing materials are used to coat the surface of targets in the reduction of RCS. Compered with single-layer absorbers, multilayered absorbers are more flexible and can achieve better performance, including wider bandwidth and smaller thickness [24]. As shown in Figure 1, a multilayered absorber usually consists of the matching layer and the absorbing layer [25]. The matching layer, which is on the top of the absorber, helps couple the impedance of the free space with the impedance of the absorber. On the other hand, the absorbing layer, which is on the bottom of the absorber, absorbs most of EM energies.

The used materials are essential in the design of absorbers since the performance of absorbers mainly depends upon the performance of used materials. Each layer consists of different materials so that different designs of absorber with different performances can be obtained. Usually, there are three types of material in the design of microwave absorbers, i.e., dielectric material, magnetic material, and composite material [26]. In this paper, two types of composite materials with different proportions of CIPs are used since the CIPs have exhibited a very strong absorbing capability for EM energies [22]. The composite material with 10% CIP is used to build the matching layer, and the composite material with 35% CIP is used to construct the absorbing layer. Hereinafter, we will use  $S_1$  to represent the composite material with 10% CIP and use  $S_2$  to indicate the composite material with 35% CIP. The complex permittivity and complex permeability of the two composite materials are frequency-dependent and their relationships are shown in Figures 2 and 3, respectively.

From the figures, we can see that the complex permittivity and complex permeability (referring to the magnitudes of their real and imaginary parts) of  $S_1$ 

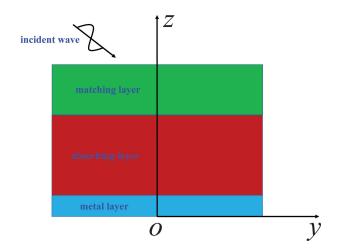


Fig. 1. Structure of a multilayered absorber.

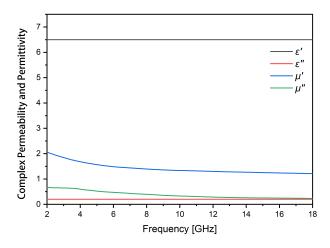


Fig. 2. Permittivity  $\varepsilon$  and permeability  $\mu$  of composite material with 10% CIP. Prime denotes the real part while double prime denotes the imaginary part.

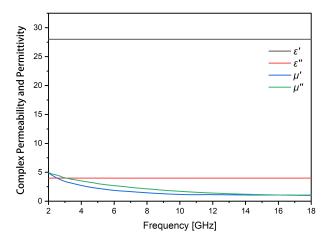


Fig. 3. Permittivity  $\varepsilon$  and permeability  $\mu$  of composite material with 35% CIP. Prime denotes the real part while double prime denotes the imaginary part.

are relatively low in the frequency range from 2.0 to 18.0 GHz. Also, the complex permittivity of  $S_1$  is almost constant in the above frequency range and the complex permeability varies with the frequency very slowly. As a result, it is possible that the impedance of a layer composed of  $S_1$  is close to the impedance of free space in the above frequency range. Compared to  $S_1$ , the material  $S_2$  owns a higher complex permittivity and complex permeability. Moreover, the magnitude of complex permeability decreases slightly. This feature leads to that  $S_2$  has a good absorption and poor impedance matching while  $S_1$  has an opposite behavior.

#### III. DESIGN OF MULTILAYERED ABSORBERS

The design of absorbers requires an efficient and accurate analysis or evaluation for their performance. Fullwave EM simulation is a good way to do that, but it consumes much time and resources. Compared to the former approach, the TLT can also be used to analyze but requires much less time and resources. Usually, a planar multilayered absorber can be represented by a transmission-line model so that we can apply the TLT to analyze the behavior of multilayered absorbers. In the analysis, the reflection coefficient of absorbers can be used to evaluate the performance if the input impedance is available. The input impedance can be calculated by using the TLT [27], i.e.,

$$Z_{\text{in}_{j}} = Z_{j} \frac{Z_{\text{in}_{j-1}} + Z_{j} \tanh\left[j\left(2\pi f d_{j}/c\right)\sqrt{\mu_{j}\varepsilon_{j}}\right]}{Z_{j} + Z_{\text{in}_{j-1}} \tanh\left[j\left(2\pi f d_{j}/c\right)\sqrt{\mu_{j}\varepsilon_{j}}\right]}$$
(1)

where

$$Z_j = Z_0 \sqrt{\mu_j / \varepsilon_j} \tag{2}$$

$$\mu_j = \mu_{r_j} \mu_0, \quad \varepsilon_j = \varepsilon_{r_j} \varepsilon_0 \tag{3}$$

$$j = 1, 2, 3, \dots, n.$$
 (4)

Also,  $d_j$ , f, c,  $\varepsilon_{r_j}$ ,  $\mu_{r_j}$ , and  $Z_j$  denote the thickness, frequency, speed of light, complex permittivity, complex permeability, and intrinsic impedance of the *j*th layer (j = 1, 2, 3, ..., n), respectively. In addition,  $\varepsilon_0$  and  $\mu_0$  are the permittivity and permeability of free space,  $Z_{in_j}$  is the wave impedance of the *j*th layer, and *n* is the total number of layers. Based on the input impedance, the overall reflection coefficient of the multilayered absorber at an air-absorber interface is given by

$$\Gamma = -20 \lg \left| \frac{Z_{\text{in}j} - Z_0}{Z_{\text{in}j} + Z_0} \right|.$$
<sup>(5)</sup>

If we choose n = 2, i.e., design a two-layer absorber, then the input impedance can be simplified as

$$Z_{\rm in} = Z_2 \frac{Z_{\rm in_1} + Z_2 \tanh\left[j(2\pi f d_2/c)\sqrt{\mu_2 \varepsilon_2}\right]}{Z_2 + Z_2 \tanh\left[i(2\pi f d_2/c)\sqrt{\mu_2 \varepsilon_2}\right]} \tag{6}$$

where

$$Z_{\text{in}_1} = Z_0 \sqrt{\frac{\mu_1}{\varepsilon_1}} \tanh\left[j\frac{2\pi f d_1}{c}\sqrt{\mu_1\varepsilon_1}\right]$$
(7)

and the overall reflection coefficient is

$$\Gamma = -20 \lg \left| \frac{Z_{\rm in} - Z_0}{Z_{\rm in} + Z_0} \right|. \tag{8}$$

In the above,  $Z_{in_1}$  is the wave impedance at the surface of the first layer and  $Z_{in}$  is the wave impedance at the second layer. With the reflection coefficient, we can calculate the absorption of the incident EM wave normal to the planar multilayered absorber.

Based on the above method of evaluating the performance of absorbers, we can then design desirable multilayered absorbers. How to determine the number of layers, type of materials, and thickness of each layer is the key in the design, and optimization algorithms can be used to efficiently select those parameters with a low cost [28]. Compared with other optimization methods, the PSO is an efficient method that can be easily used in the design of absorbers [29]. The PSO was inspired by a flying swarm of birds searching for food and we use it to seek optimal values for the thickness of each layer and the number of layers [30]. In order to obtain the optimal result, we should take the total thickness, bandwidth, and reflection peak together into consideration. Therefore, the cost function to be optimized can be set as [31, 32]

$$f = k_1 \cdot \Gamma_{\min} + k_2 \sum d_i + k_3 \cdot WB + k_4 \cdot \Gamma_{ave}$$
  
$$i = 1, 2, 3, \dots, n$$
(9)

where  $\Gamma_{\min}$  is the minimum of reflection coefficient,  $d_i$  is the thickness of *i*th layer, *WB* is the bandwidth of the absorber,  $\Gamma_{\text{ave}}$  is the average of reflection coefficient, and  $k_j$  (j = 1, 2, 3, 4) is the weight of each term. Also,  $\sum d_i$  represents the total thickness of the multilayered absorber. Selecting the appropriate weight for each term, we can get the optimal values for those parameters by minimizing the cost function.

Considering the simplest case, namely, the number of layers is chosen as n = 2, we can get a planar design. The two-layer absorber is composed of the matching layer and absorbing layer. The matching layer on the top of the absorber consists of the material  $S_1$  while the absorbing layer on the bottom of the absorber consists of the material  $S_2$ . After using the PSO to minimize the above cost function, we can obtain the optimal value 2.13 mm for the matching layer and 0.87 mm for the absorbing layer, respectively, and the total thickness of the absorber is then 3.0 mm. With the optimal thickness of each layer, the reflection coefficient of the two-layer absorber can be calculated and is shown in Figure 4.

As shown in Figure 4, the absorber can cover most of the frequency range from 2.0 to 18.0 GHz. Furthermore, the bandwidth of the absorber is 14.63 GHz

Fig. 4. Reflection coefficient of a two-layer absorber.

 Table 1: Multilayered absorber design (unit: mm)

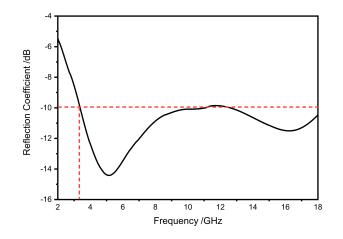
Absorber	Layer I	Layer II	Layer III	Layer IV	Layer V
Type I	S1	-	-	-	-
	3.00	-	-	-	-
Type II	S2	-	-	-	-
	3.00	-	-	-	-
Type III	S1	S2	-	-	-
	0.64	0.30	-	-	-
Type IV	S2	S1	-	-	-
	0.87	2.13	-	-	-
Type V	S2	air gap	S1	-	-
	0.01	0.87	2.20	-	-
Type VI	air gap	S2	air gap	S1	-
	0.01	1.14	1.16	1.03	-
Type VII	S2	air gap	S2	air gap	S1
	1.19	1.14	0.33	1.47	1.06

ranging from 3.37 to 18.0 GHz. The minimum return loss appears at 5.14 GHz and the value is -14.42 dB. These data demonstrate that the two-layer absorber has a good performance.

If we increase or decrease the number of layers, the behavior of the absorber could significantly change. When a multilayer absorber is designed, the performance of absorber will vary in terms of the thickness of each layer, type of materials, and number of layers. Based on the design of two-layer absorber, we change the number of layers from 1 to 5 and the thickness of each layer is different in different cases. Through the optimization by the PSO, we obtain seven multilayered designs and the final results are shown in Table 1.

As we can see from Table 1. the seven designs have different values for the number of layers, type of materials, and thickness of each layer, and their performances vary greatly in the working frequency range of 2.0 - 18.0 GHz, as shown in Figure 5.

From Table 1 and Figure 5, we can see that the designs of Type I and Type II are both single-layer absorbers with a narrow bandwidth. The reflection peak of Type-I design cannot reach a reflection peak of -10 dB when the thickness is 3.0 mm, and Type-II design only covers a very narrow frequency band with a thickness of 3.0 mm. Thus, a single-layer absorber cannot well absorb the EM energy at most frequencies and a multilayered design is needed to increase both the reflection peak and bandwidth. Type-III design consists of the material  $S_1$  as the absorbing layer and the material  $S_2$  as the matching layer. As shown in the Table 1 and Figure 5, this design presents a good reflection peak with about -30 dB and covers a wider frequency band from 12.0 to 18.0 GHz. After exchanging the materials of the matching layer and the absorbing layer, Type-IV design shows a lower reflection peak with about -15.0 dB, but



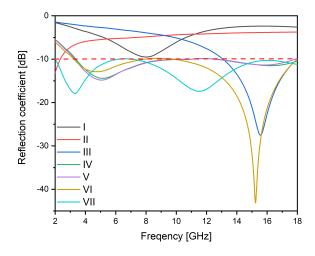


Fig. 5. Reflection coefficients of multilayered absorbers.

its bandwidth increases to nearly 15.0 GHz. After adding several air gaps to the design, we can get three different planar designs which are labeled as Type V, Type VI, and Type VII, respectively. Type-V design is a threelayer absorber composed of the material  $S_1$ , an air gap, and the material  $S_2$ . Its total thickness is 3.18 mm and bandwidth is also nearly 15.0 GHz. The total thickness of Type-VI design is 3.34 mm and its reflection peak reaches -43 dB. However, Type-VI design cannot give a good absorption performance at lower frequencies. In addition, Type-VII design is a five-layer absorber which consists of the material  $S_1$ , two air gaps, and the material  $S_2$ . Its absorption performance is improved because its absorption can cover all frequencies in the bandwidth of 2.0 - 18.0 GHz. Moreover, its total thickness is 5.37 mm which is still small, and its minimum reflection peak achieves -17.0 dB. From the above results, it is clear that increasing total thickness by increasing the number of layers can significantly improve the performance of absorbers, but the thickness is still small enough when the wisely chosen composite materials are used.

## IV. DESIGN OF ABSORBERS FOR COATING REAL OBJECTS

The above designs assume that the surfaces of absorbers are planar and infinitely large, but the absorbers need to cover the surfaces of arbitrarily shaped objects rather than infinitely large planar surfaces. Thus, it is required that the designed absorbers should not only have a wide bandwidth but also be insensitive to the incident angles of incident waves. We investigate how the incident angles impact the performances of absorbers by choosing Type-IV and Type-VII designs from the previous designs as examples and setting up four different incident angles from  $0^{\circ}$  to  $45^{\circ}$  with an interval of  $15^{\circ}$ . With the four different incident angles, we calculate the reflection coefficients for Type-IV and Type-VII designs and the results are shown in Figures 6 and 7, respectively. Type IV is a two-layer planar design whose thicknesses of the matching layer and absorbing layer are 2.13 and 0.87 mm, respectively. The planar design can cover the frequency range from 3.37 to 18 GHz with a bandwidth of nearly 15 GHz. The minimum reflection loss appears at 3.26 GHz with a value of -17.75 dB. Additionally, the total thickness of the design is only 3.00 mm, which is very thin. As shown in Figure 6, there are four absorption rates that are similar to each other but in different positions. The reflection coefficient becomes smaller at a certain frequency when the incident angle increases from  $0^{\circ}$  to  $45^{\circ}$ . Moreover, similar results can be seen when the incident angle is  $0^{\circ}$  and  $45^{\circ}$ , which means that the design can still give an optimal performance if the range of incident angle is not very large. Even though the incident angle increases to  $45^{\circ}$ , all the four cases have shown a good performance and their reflection coefficients are below -7.0 dB for most frequencies from 2.0 to 18.0 GHz.

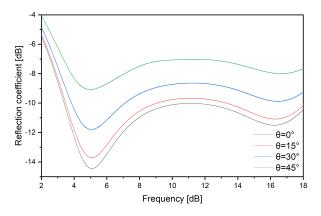


Fig. 6. Reflection coefficient of Type-IV design at four different incident angles.

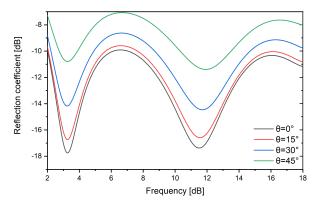


Fig. 7. Reflection coefficient of Type-VII design at four different incident angles.

Type VII is a five-layer planar design, which consists of the material  $S_2$ , an air gap, the material  $S_2$ , an air gap, and the material  $S_1$  in the order from the bottom to the top. In addition, thicknesses of five layers from the bottom to the top are 1.19, 1.14, 0.33, 1.47, and 1.06 mm, respectively. The absorber can overcome the drawback of Type-IV design, i.e., the poor performance at lower frequencies. It can achieve a broadband from 2.0 to 18.0 GHz and a minimum reflection loss at 5.14 GHz, whose value is -14.42 dB. Obviously, Type-VII design gives a better performance as shown in Figure 7. This clearly demonstrates that the smaller the incident angle is, the lower the absorption rate of Type-VII design is. In addition, the four curves in Figure 7 resemble each other but have different Y-axis positions. Furthermore, the reflection coefficients of all the four cases are not more than -7.0 dB at the frequency range from 2.0 to 18.0 GHz.

Compared to the Type-IV design, the Type-VII design has better results for all the four cases. Type-VII design can still produce excellent results for all the four cases even at lower frequencies, and its minimum reflection loss is also smaller than that of Type-IV design. Nevertheless, both Type-IV and Type-VII designs are insensitive to the incident angles; so they can both perform well when coated at other objects with different shapes.

In order to validate the performances of designed absorbers, we coat the absorbers on the surface of a PEC cylinder and calculate the monostatic RCS for the cylinder with and without the coating. The PEC cylinder has a height of h = 60 mm and a cross-sectional radius of a = 60 mm, which is equivalent to two wavelengths at the frequency of 10 GHz. We select three incident angles to verify the absorbing capacity of two types of coating materials. When the incident wave perpendicularly incidents to the upper circular surface of the cylinder and its polarization is horizontally polarized, the results of monostatic RCS of the cylinder with Type-IV coating or Type-VII coating or without coating are shown in Figure 8.

Figure 8 shows that the performance of two kinds of coating is obviously better than that without the coating and the performance of the Type-IV coating is better than that of the Type-VII coating, especially at the lower frequencies from 2.0 to nearly 14.5 GHz. From 14.5 to 18 GHz, the performance of Type-IV is better than Type-VII. The Type-IV coating can help to reduce the RCS in minimum 2.0 dB at 2.0 GHz and in maximum 17.5 dB at 17 GHz. The Type-VII coating can help to reduce the RCS in minimum 5.0 dB at 2.0 GHz and in maximum 16.5 dB at 12.0 GHz. The RCS of the PEC cylinder without the coating increases from -10.0 to 7.0 dB as the frequency increases. In addition, for

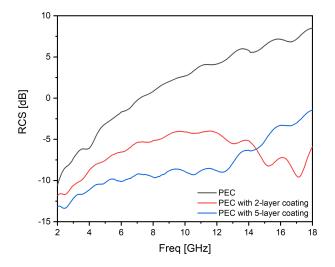


Fig. 8. Comparison of monostatic RCS solutions for the PEC cylinder without and with the coating tested by the perpendicularly incident wave.

the Type-IV coating, its RCS reduction becomes larger as the frequency increasing in most part of the operation band. While with the coating of Type-VII, its RCS reduction becomes larger from 2.0 to 9.0 GHz and then maintains a large reduction of nearly 14 dB from 9.0 to 18 GHz.

When the incident wave which is horizontally polarized incidents with an angle of  $45^{\circ}$  to the upper circular surface of the cylinder, the results of RCS of the cylinder with Type-IV coating or Type-VII coating or without coating are shown in Figure 9. The RCS of the PEC cylinder without the coating is below -20 dB at

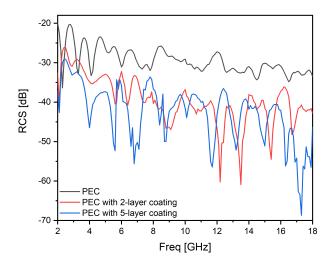


Fig. 9. Comparison of monostatic RCS solutions for the PEC cylinder without and with the coating at the incident angle of  $45^{\circ}$  to the upper circular surface of the cylinder.

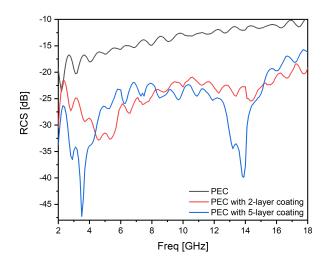


Fig. 10. Comparison of monostatic RCS solutions for the PEC cylinder without and with the coating at the incident angle of  $90^{\circ}$  to the upper circular surface of the cylinder.

low frequency and decreases to -30 dB as the frequency increases to 18 GHz. Both of the coatings have the ability to reduce the RCS more than 8.0 dB at most of the frequency band. At a huge part of the frequency band, the reduction of Type-VII coating is higher than that of Type-IV coating, especially at the lower frequencies and higher frequencies.

By further using the incident wave which is horizontally polarized incidents with an angle of 90° to the upper circular surface of the cylinder, the Poynting vector of the incident wave is parallel to the upper circular surface, and the new different consequences are obtained as shown in Figure10. From the figure, it can be seen that the coating on the cylinder generates a similar RCS reduction to that of the coating on an infinitely large plate. The performance of Type-IV coating is good at a huge part of the frequency band but cannot give a good RCS reduction at nearly 2.0 GHz. However, the Type-VII coating can reach a low RCS from 2.0 to 18 GHz and can help RCS to reduce 8.0 dB in most of the targeted frequency band. The Type-VII coating also has two absorption peaks at 3.5 and 14 GHz.

#### **V. CONCLUSION**

We develop a novel approach to reduce the RCS of targets by using multilayered composite absorbing materials. The first-layer material  $S_1$  has a superb impedance matching capability and the second-layer  $S_2$  has a good absorption characteristic, and their overlay constitutes the design of multilayered absorbers. In order to design more efficiently, we apply the TLT to analyze the performance of absorbers and employ the PSO to seek the optimal thicknesses of each layer, number of layers, and type of material of each layer. Seven designs with different thicknesses, materials, and numbers of layers are finally figured out and they have shown good performances. Particularly, when we change the incident angle  $\theta$  of incident wave from 0° to 45°, it is found that both Type-IV and Type-VII designs among the seven designs are insensitive to the incident angles. Also, they have a small thickness and a broad frequency band. We then coat the designed absorbers on the surface of a PEC cylinder and compare the reductions of RCS between without and with the coating. It is found that the Type-VII coating can provide much more reduction of RCS than the Type-IV coating, especially at low frequencies. In addition, both designs have at least 8.0 dB reduction of RCS in the most part of the frequency band from 2.0 to 18.0 GHz. To sum up, these two material coatings have wide working bandwidths and have high relative bandwidths. They have a high absorptivity when the EM waves are incident vertically. In addition, it can be seen that these materials are angle insensitive relatively in the simulation process of the cylinder. The excellent dielectric constants also make these materials have a certain industrial application ability. The simulation results demonstrate that the designed absorbers can effectively reduce the RCS of real objects and could be good candidates for the stealth designs of targets. More importantly, this method using TLT and PSO algorithms can greatly simplify the original complex design process, save a lot of simulation time, and can be widely used in the design of many kinds of materials.

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