# Combined Application of Partition Clustering Classification and Gerchberg-Papoulis Optimization Algorithm for Spherical Near Field Antenna Measurements

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Abstract – An adaptive sampling and optimized extrapolation scheme for spherical near-field antenna testing is proposed. The method relies on the partition clustering classification algorithm and Voronoi classification to divide a small amount of initial data into subclasses and cells. The sampling density and rates of variation between adjacent sampling points are used as an overall metric function to evaluate the sampling dynamics at each location. Appropriate interpolation is performed in the highly dynamic region to increase the effective data in the near-field samples. The Gerchberg-Papoulis algorithm extrapolates the unnecessary interpolation region to improve the near-field sampling accuracy. This method uses a small amount of initial nearfield sampled data for near-far field conversion to achieve the same precision as uniform oversampling. The feasibility and stability of the algorithm are proved from the actual measurement results.

*Index Terms* – adaptive sampling, cluster classification algorithm, extrapolation, spherical near-field testing.

## **I. INTRODUCTION**

Compared with plane and cylindrical near-field testing, spherical near field testing (SNFT) scans the entire 3D near-field spherical information of the antenna under test (AUT) with a uniform sampling interval through a single probe or multiple probes, and can obtain the complete information of the AUT in the entire 3D space. Spherical near-field to far-field (NF-FF) transformation techniques have been widely used to overcome the impossibility or impracticality of measuring antenna radiation patterns in the far field. The core of the SNFT is to use the characteristic that the spherical wave expansion coefficient remains unchanged in the near field (NF) and the far field (FF) to perform the spherical nearfar field conversion [1–7]. Recently, the SNFT transformation technique has been applied to loaded/unloaded reverberation chambers for antenna pattern reconstruction [8, 9]. Nevertheless, calculation of spherical wave expansion coefficients for NF data with incomplete or large errors will cause large deviations.

There have been different solutions to the problem of truncation error and to demonstrate the reliability of the method in small truncation regions [10–16]. The authors in [10] proposed an iterative extrapolation-based machine learning algorithm to extend the calculation of the far field to a more accurate region, which employed an analysis of variance test to check the overall feasibility of the regression model. The authors in [11] used the Gerchberg-Papoulis (GP) iterative algorithm to extrapolate the part outside the truncation region. The NF sampling points were extended using a Slepian sequence that is specially constructed to be orthogonal over a given truncated sweep circle, achieving more accurate results than the classical near-far-field transformation [12]. [13] adopted the truncation error in the measurement of the planar near-field aperture antenna by the alternate orthogonal projection method.

The large number of sampling points results in a long measurement time, which requires more flexibility in the sampling scheme. Measurements on the coarse grid were interpolated onto the finer grid using an optimal sampling interpolation (OSI) method to determine measurements for efficient recovery of non-uniform NF samples [17–18]. The compressed sensing (CS) method determines the minimum number of samples for nearfield sparse recovery, which allows reducing the number of measurements for all antennas while maintaining accuracy [19-20]. However, the sparse level of NF sampled data and the prior information of the system had a great impact on the test results and are not suitable for all antenna tests. Based on measurements with helical scans, the authors in [21] investigated the application of non-uniform fast Fourier transforms in SNFT. A recently proposed method based on recursive partitioning in a multi-level subdomain hierarchy of radiating surfaces is applied to arbitrary surface measurements [22]. The authors in [23–25] described the adaptive method to reduce the measurement burden spherical near-field measurements. The fast irregular antenna field transformation algorithm (FIAFTA) was used to post-process the near field collected on an irregular grid [26] and the source reconstruction method was used to calculate the equivalent current on the surface of the ellipsoid containing the AUT [23]. These techniques require more time than fast Fourier near-far field transform methods.

In this paper, a spherical near-field sampling optimization method based on partition clustering classification and GP joint optimization is proposed. Starting from a small amount of sampled data, the clustering method is used to quantify the dynamic changes of the AUT NF electric field. There is a trade-off between sampling density and variation between adjacent sampling points according to different criteria. The new data is interpolated in the high dynamic change area of the field to improve the accuracy of the near-field sampling data and the GP iterative algorithm extrapolates the data to the unnecessary interpolation area to reduce the truncation error.

The structure of the paper is as follows. Section II introduces the theory of spherical wave expansion and the optimization scheme of spherical near-field sampling. Measurement results are presented in section III. The superiority of the optimized scheme in improving the test efficiency is proved. Section IV concludes the paper.

#### **II. BACKGROUND THEORY**

This section presents the theory of antenna pattern reconstruction based on a small number of initial sampling points. Firstly, the theory of spherical wave expansion is described. Then, the clustering method is introduced to divide the initial sampling points into several subclasses, and the calculation process of introducing new sampling data by using the GP optimization algorithm is given. Finally, the near-field data is reconstructed to obtain the antenna pattern. The detailed measurement process is as follows.

According to the uniqueness theorem and the equivalence principle, the radiation field in the outer space of the closed surface can be calculated and determined through the tangential component of the electromagnetic field on the closed surface including all the radiation sources. In the SNFT, an equivalent spherical surface is used to completely surround the AUT, and a passive region is established outside the spherical surface, as shown in Fig. 1.

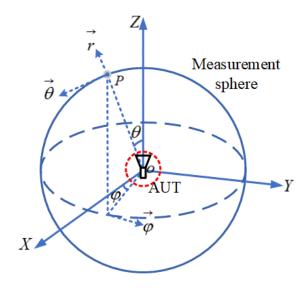


Fig. 1. Schematic of SNFT.

Outside the minimum sphere of the AUT, the electric field can expand as a weighted sum of spherical wave functions expressed as:

$$E(r,\theta,\phi) = \sum_{s=1}^{2} \sum_{n=1}^{N} \sum_{m=-n}^{n} Q_{smn} \vec{F}_{smn}^{(3)}(r,\theta,\phi), \quad (1)$$

where  $(r, \theta, \varphi)$  are the spherical coordinates,  $Q_{smn}$  are the SWCs of the AUT,  $\vec{F}_{smn}^{(3)}$  are the spherical wave expansion functions, s = 1 and 2 represent transverse electric (TE) and transverse magnetic (TM) wave modes, respectively, and m, n are the number of modes of AUT. N is a truncation number for the spherical wave expansion empirically obtained from  $N = [kr_0] + 10$ ,

where k is the wave number,  $r_0$  is the radius of the minimum sphere surrounding the antenna and the square brackets indicate the largest integer smaller than or equal to  $kr_0$ . In equation (1), the spherical wave expansion functions are known, the SWCs  $Q_{smn}$  can be solved and the field value at any distance can be obtained.

In order to obtain the dynamic change of the electric field data in the near field of the antenna, Mintial sampling data are randomly selected from the uniform spherical near field sampling dataset  $S_2$  as the initial samples set as  $S_1$ . The K-means clustering method is used to cluster the  $M_{intial}$  sampled data into k subclasses, and each subclass randomly selects a sample as the cluster center. Minkowski distance (p = 2 means Euclidean distance) is used to measure the deviation of each sample value from the cluster center and each sample is classified into the subclass where the cluster center with the closest distance is located. The cluster center of each subclass is updated to the average value of all points in the subclass, and the samples are reclassified until the cluster center of all subclasses no longer changes or the total clustering error in all subclasses is the smallest. The current total clustering error in all subclasses is:

$$d = \left(\sum_{j=1}^{k} \sum_{x_i \in C_j, c_j \in C_j} \left| x_i - c_j \right|^p \right)^{\frac{1}{p}},$$
 (2)

where  $x_i$  is the *i*-th sample and  $c_j$  is the cluster center belonging to the *j*-th subclass  $C_j$ .

After obtaining the cluster classification results, the initial near-field sampling data is sorted according to the sample sampling density and the rate of variation of adjacent samples, and the top ranking represents the area that needs to be interpolated. In order to calculate the sampling density, the initial sampling points are represented by a Voronoi diagram according to the nearest neighbor principle [27]. Each initial sampling point corresponds to a cell, and the sampling density is determined by the area of each cell. Each sampling point is associated with its nearest neighbor cell, and the sample variation rate is expressed as the gradient of the field between adjacent sampling points. So the overall evaluation parameter can be expressed as:

$$G(x_m) = \alpha \left(1 + \frac{S(x_m)}{\sum_{p=1}^{M_{initial}} S(x_p)}\right) + \beta \left(1 + \frac{V(x_m)}{\sum_{p=1}^{M_{initial}} V(x_p)}\right),$$
(3)

where  $S(x_m)$  is the area of the *m*th cell,  $V(x_m)$  is the sum of the absolute values of all gradients around the *m*th cell and  $\alpha, \beta$  (satisfying  $\alpha + \beta = 1$ ) are the weighting coefficients.  $\alpha$  and  $\beta$  are adjusted accordingly according to the cluster classification results. If the sampling variation rate in a subclass is too large, in order to better judge the interpolation requirements of the sampling area, it is necessary to increase the proportion of sampling density in the overall evaluation parameters, that is, increase the value of  $\alpha$ .

According to the judgment criteria, part of the data to be interpolated comes from the dataset  $S_2$ , and a small amount of data that is not located in the dataset  $S_2$  with uniform sampling interval. A modified Akima piecewise cubic Hermite interpolation method is used in this part.

In order to reduce the truncation error caused by the near-far field conversion after zero-filling the non-essential interpolation area with smooth dynamic changes, the GP algorithm is introduced to extrapolate the sampled values. It is a band-limited extrapolation algorithm that extrapolates the data outside the interval from the known interval, and it is iteratively implemented by using Fourier transform and inverse Fourier transform. Plane wave spectra (PWS) of spherical nearfield probe sampled data is obtained from truncated NF measurements using Fourier transforms:

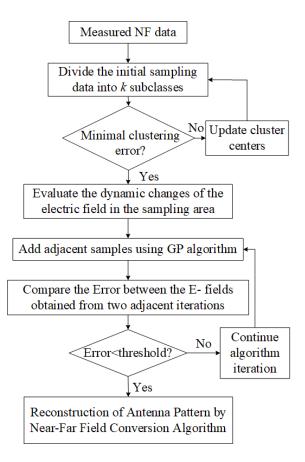


Fig. 2. Schematic diagram of the proposed method.

$$\mathbf{G}_0(\boldsymbol{\theta}_k, \boldsymbol{\varphi}_k) = fft[g_0(\boldsymbol{\theta}_k, \boldsymbol{\varphi}_k)], \qquad (4)$$

where  $g_0(\theta_k, \varphi_k)$  is the cluster-interpolated accessible near field data. The filter functions in the spectral and space domain are: (9)

$$H_{R}(\theta_{k},\varphi_{k}) = \begin{cases} 1, \ (\theta_{k},\varphi_{k}) \in \Omega_{0} \\ 0, \ (\theta_{k},\varphi_{k}) \notin \Omega_{0} \end{cases} , \qquad (5)$$

and

$$\mathbf{h}(\boldsymbol{\theta}_k, \boldsymbol{\varphi}_k) = \begin{cases} 1, \ (\boldsymbol{\theta}_k, \boldsymbol{\varphi}_k) \in \boldsymbol{\omega}_0 \\ 0, \ (\boldsymbol{\theta}_k, \boldsymbol{\varphi}_k) \notin \boldsymbol{\omega}_0 \end{cases}, \tag{6}$$

where  $\omega_0$  and  $\Omega_0$  are reliable regions of the space and spectrum. The electric field on the sampling surface obtained by extrapolation is given by the following equation:

$$g_{n+1}(\theta_k, \varphi_k) = \hat{g}_n(\theta_k, \varphi_k) + (g_0(\theta_k, \varphi_k) - \hat{g}_n(\theta_k, \varphi_k))h(\theta_k, \varphi_k),$$
(7)

where

$$\hat{g}_{n+1}(\theta_k, \varphi_k) = ifft[H_R(\theta_k, \varphi_k)G_n(\theta_k, \varphi_k)].$$
(8)  
The PWS of the reliable region is:

 $\mathbf{G}_n(\boldsymbol{\theta}_k, \boldsymbol{\varphi}_k) = f f t [\mathbf{g}_n(\boldsymbol{\theta}_k, \boldsymbol{\varphi}_k)],$ 

where fft and ifft means Fourier transform and inverse Fourier transform, *n* is the value of iteration times,  $(\theta_k, \varphi_k)$  is the *k*th sampling point on the spherical grid and  $g_n(\theta_k, \varphi_k)$  is the optimization extrapolation result for the *n*th iteration. The error of the near-field data obtained from two adjacent iterations is expressed as

$$Error = \sum_{k=1}^{M_{total}} |g_{n+1}(\boldsymbol{\theta}_k, \boldsymbol{\varphi}_k) - g_n(\boldsymbol{\theta}_k, \boldsymbol{\varphi}_k)|^2, \quad (10)$$

where  $M_{total}$  is the total effective NF data after extrapolation. After several iterations, the error reaches a stable convergence point and the iteration terminates.

A schematic diagram of the proposed method is shown in Fig. 2, where a small amount of sampling data is used to verify the effectiveness of the clustering technique and the GP extrapolation algorithm to estimate the electric field in the extended area.

### **III. MEASUREMENT RESULTS**

A commercial antenna operating at 2.6 GHz, which is invisible internally, was tested in the spherical near-field multi-probe anechoic chamber of the China Academy of Information and Communications Technology (CAICT). The radius of the SNFT system is 1.6 m, and the minimum spherical radius surrounding the antenna is 0.156 m, as shown in Fig. 3. Figure 4 shows the antenna pattern obtained by using commercial software to calculate the NF data, which is set as the reference radiation pattern.

In order to obtain the initial small amount of sampling data, the NF sampling interval is set to 15 degrees and there is a truncation in the range from  $\theta = 165^{\circ}$  to  $\theta = 180^{\circ}$  degrees due to the influence of the south pole. To improve the test accuracy, triple uniform oversampling ( $\Delta \theta = \Delta \varphi = 5^{\circ}$ ) is necessary. The uniformly sampled dataset and triple oversampled dataset are set as  $S_1$ and  $S_0$  respectively, and 150 sampling points are selected from  $S_1$  as the initial data set  $S_2$ .

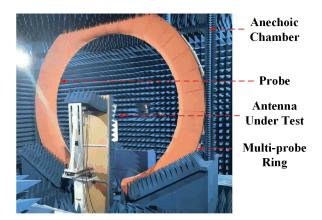


Fig. 3. The spherical NF measurement environment.

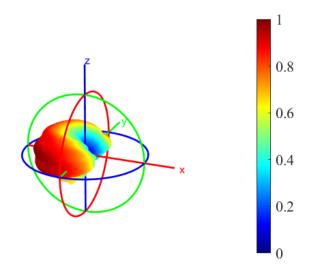


Fig. 4. Reference radiation pattern at 2.6 GHz.

The K-means clustering method divides the sampled values into k subclasses, and for each k value, the sum of the squared distances from every sample to the nearest cluster center is calculated as the total clustering error. As shown in Fig. 5 (a), the total cluster error converges to a stable value at k = 6 and Fig. 5 (b) shows the cluster classification results for k = 6. Figure 6 shows the Voronoi diagram cell classification results for the initial sampling of the NF. Using equation (3), the area of each cell and the variation rate of adjacent sampling points are calculated. The cell groups whose base sites are red represent highly dynamic areas requiring interpolation, and blue areas represent unnecessary interpolation region.

We use the interpolation method mentioned in the previous section to obtain the dataset  $S_3$  with truncated regions. Dataset  $S_4$  is extrapolated from dataset  $S_3$  by GP algorithm. Figure 7 (a) shows the error of two adjacent iterations of the co-polarization (CP) and

cross- polarization (XP) of the antenna. When the GP algorithm iterates 80 times, the error converges. Figure 7 (b) shows the nomalized iterative error of the oversampled electric field and the electric field obtained by the proposed method.

Figure 8 (a) shows the radiation pattern reconstructed from the dataset  $S_4$ . Figure 8 (b) shows the rel-

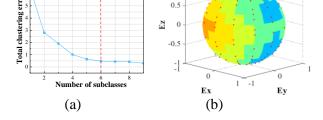


Fig. 5. K-means clustering method. (a) L-curve. (b) Clustering method, k = 6.

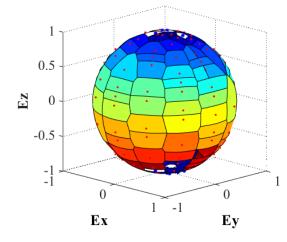


Fig. 6. Voronoi diagram classification for near-field sampling.

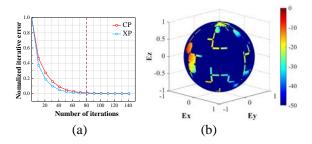


Fig. 7. (a) The nomalized iterative error of CP and XP components obtained from two adjacent iterations. (b) Relative error of  $S_4$  and  $S_0$  in all angles.

ative error of reference and reconstructed radiation pattern. The relative error can be obtained using:

*Relative Error* = 
$$20 \log ||E_1| - |E_2||$$
, (11)

where  $E_1$  and  $E_2$  are the two electric fields to be compared, respectively. Comparisons of CP and XP components in XOY plane and XOZ plane between reference pattern, the pattern reconstructed by triple oversampling and optimal sampling by the proposed algorithm are given in Fig. 9. As can be seen, the main lobe of

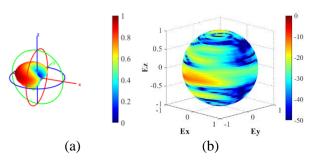


Fig. 8. (a) Reconstructed radiation pattern. (b) Relative error of reference and reconstructed radiation pattern in all angles.

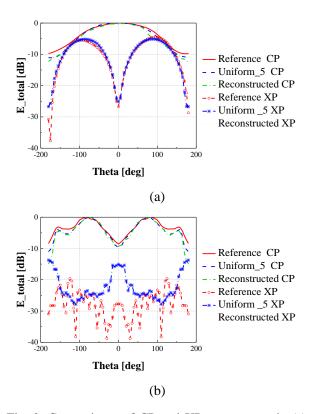


Fig. 9. Comparisons of CP and XP components in (a) XOY plane, and (b) XOZ plane between reference pattern, pattern reconstructed by triple oversampling and optimal sampling by the proposed algorithm.

the CP component of the pattern is in good agreement, but the reconstruction result of the XP has a large error compared with the reference pattern, especially in XOZ plane.

It is noted that the possible positioning error in the actual test affects the pattern recovery. Figures 10 and 11 show the interference errors in XOY plane and XOZ plane introduced when the radial errors are 5 mm, 10 mm and 15 mm, respectively, and the  $\theta$  angle errors are 0.01 deg, 0.5 deg and 1 deg, respectively. The radial position error in spherical NF scanning mainly affects the phase error in the near field, which is proportional to the radial error. The  $\theta$  angle error between the actual and the ideal alignment direction of the AUT makes the maximum gain direction of the probe antenna deviate from the center of the SNFT system, which changes the test distance and causes the change of the probe receiving strength to affect the recovery of the pattern.

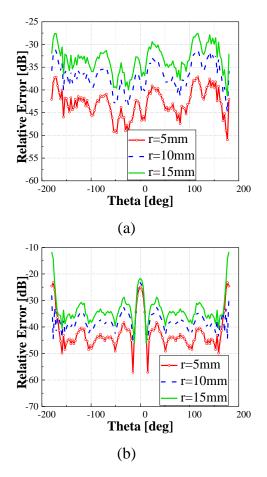


Fig. 10. The relative errors in (a) XOY plane, and (b) XOZ plane introduced when the radial errors are 5 mm, 10 mm, and 15 mm, respectively.

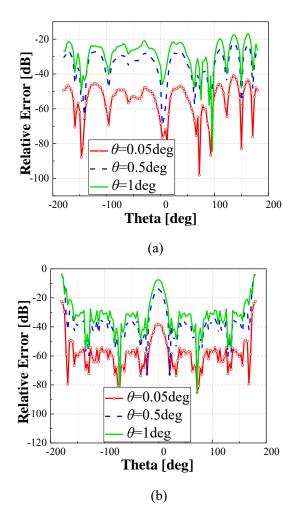


Fig. 11. The relative errors in (a) XOY plane, (b) XOZ plane introduced when the  $\theta$  angle errors are 0.01 deg, 0.5 deg, and 1 deg, respectively.

### **IV. CONCLUSION**

This paper proposes a method to improve the sampling efficiency of spherical near-field testing. Starting from a small number of near-field sampling points, the region with high dynamic variation of the electric field is located through the clustering classification theory for appropriate interpolation. The GP algorithm is used to extrapolate the unnecessary interpolation area to further improve the sampling accuracy and reduce the truncation error. The multi-probe spherical near-field anechoic chamber test was carried out on a commercial antenna working at 2.6 GHz. The feasibility of this scheme is demonstrated by comparing the reference radiation pattern with the radiation pattern reconstructed by three oversampling and optimized samplings. The influence of the test positioning error on the reconstructed pattern is further discussed.

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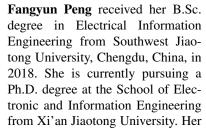
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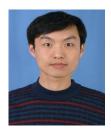
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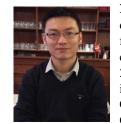
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