# FDTD Analysis of a Probe-Fed Dielectric Resonator Antenna in Rectangular Waveguide

Yizhe Zhang, Ahmed A. Kishk, Alexander B. Yakovlev\*, and Allen W. Glisson Department of Electrical Engineering Center of Applied Electromagnetic Systems Research The University of Mississippi, University, MS, 38677, USA zyz@olemiss.edu, ahmed@olemiss.edu, yakovlev@olemiss.edu, aglisson@olemiss.edu

**Abstract:** A probe-fed dielectric resonator antenna (DRA) element is investigated for operation in a waveguide environment with application to spatial power combining amplifier arrays. The method of analysis is based on the finite-difference time-domain (FDTD) approach, wherein a rectangular waveguide and DRA are discretized by using a traditional Yee cell griding and a coaxial line is modeled by a thin wire approximation. The input impedance and scattering parameters are studied by varying geometrical and material parameters of the DRA and the coaxial probe feed. The numerical results obtained by the proposed FDTD method are compared with those generated by using a commercial software and exhibit very good agreement.

**Keywords:** Dielectric resonator antenna, rectangular waveguide, finite-difference timedomain method

# 1. Introduction

In recent years, there has been an increasing demand for high-power and efficient solidstate microwave and millimeter-wave amplifiers, which resulted in extensive experimental and theoretical research in the area of quasi-optical and spatial power combining. A new generation of spatial/quasi-optical power combiners requires a development of integrated modeling environment in order to design systems with high output power levels and power combining efficiencies for operation at millimeter-wave frequencies. Thus, receive and transmit antenna elements used in the amplifier arrays must be carefully selected and accurately modeled.

Due to their attractive characteristics, DRA elements have received an increasing interest as radiating antenna elements. The DRA elements have many advantages such as wideband nature, small size, high power handling capability, and high radiation efficiency as compared with microstrip antennas [1]-[3]. The DRA is often made of high dielectric constant materials with very low loss tangent, which makes it attractive for high frequency applications where the conduction loss will be much smaller than that of microstrip antennas.

In this paper, a coaxial probe-fed DRA is studied for operation in a rectangular waveguide for potential application in spatial power combining amplifier arrays. The FDTD method is used for the full-wave analysis of the structure. Scattering parameters of

the waveguide-based DRA are studied by varying a position and length of the excitation probe and by changing the geometrical parameters of the DRA.

In the next section, a brief description of the analysis method is presented. In Section 3, the scattering parameters are computed using the FDTD method and are compared with the results obtained using commercial software. Conclusions and discussions are presented in Section 4.

#### 2. Theory

The structure to be analyzed here consists of a coaxial probe-fed DRA inside a rectangular waveguide as shown in Fig. 1. The geometry is modeled by using the FDTD method, where the PML absorbing boundary condition is used to terminate both the waveguide port and the coaxial line. For the waveguide calculation area, the traditional FDTD update equations are used. The inner conductor of the coaxial line is modeled by a thin wire approximation, when the radius is smaller than the FDTD cell dimensions [4]. With  $E_z$  (*i*, *j*, *k*) = 0 along the wire axis, the spatial dependence of the fields in the vicinity can be calculated by

$$H_{y}^{n+\frac{1}{2}}(i,j,k) = H_{y}^{n-\frac{1}{2}}(i,j,k) + \frac{\Delta t}{\mu\Delta z} \left[ E_{x}^{n}(i,j,k) - E_{x}^{n}(i,j,k+1) \right] + \frac{2\Delta t}{\mu\Delta x \ln\left(\frac{\Delta x}{r_{0}}\right)} E_{z}^{n}(i+1,j,k).$$
(1)

The time domain incident and total modal voltages can be calculated from the total electric field as

$$V_{\mathcal{S}}(z_0,t) = \iint \vec{E}(x,y,z_0,t) \cdot \vec{e}_{\mathcal{S}}(x,y) dx dy$$
<sup>(2)</sup>



Fig. 1. Waveguide-based coaxial probe-fed DRA geometry.

where  $V_S$  is the time domain modal voltage for the mode S at the transverse plane located at  $z = z_0$ ,  $\vec{E}$  is the time domain total electric field in a rectangular waveguide due to the excitation across a waveguide transverse plane,  $\vec{e}_s$  is the modal field vector [5] for the mode *S*, and the integral in (2) is over the transverse plane of the waveguide port.

The scattering parameters can be calculated as a ratio of port voltages normalized by the characteristic impedances, which for the waveguide section with a coaxial probe-fed DRA, are given by

$$S_{11} = \frac{V_{waveguide}^{-}}{V_{waveguide}^{+}} = \frac{V_{waveguide\_total} - V_{waveguide}^{+}}{V_{waveguide}^{+}} , \quad S_{21} = \frac{V_{coaxial}^{+}}{V_{waveguide}^{+}} \sqrt{\frac{Z_{waveguide}}{Z_{coaxial}}}$$
(3)

where  $V^-$  is the voltage calculated from the reflection field,  $V^+$  is the voltage calculated from the forward traveling wave, and the Z's are the characteristic impedances. The characteristic impedance of the coaxial line can be calculated in terms of currents and voltages as explained in [5].

## 3. Results and Discussion

The initial dimensions of the DRA structure are chosen so that the resonance frequency of the TE<sub>11δ</sub> mode is centered around 10 GHz [6]. First, commercial method of moments (MoM) software [7] was used for the approximate analysis of a single probe-fed DRA element placed on an infinite ground plane and radiating in free space as shown in Fig. 2(a), where  $a_d = 5.0 \text{ mm}$ ,  $h_d = 12.0 \text{ mm}$ ,  $\delta_d = 1.0 \text{ mm}$ ,  $\varepsilon_{rd} = 12$ , and the probe radius  $r_w$  is 0.3 mm. Then, the probe-fed DRA was placed into a semi-infinite standard X-band waveguide of cross-sectional dimensions a = 22.86 mm and b = 10.16 mm (with geometry shown in Fig. 2(b)). To take into consideration the effect of waveguide walls, the height of the DRA and the probe position were changed to  $h_d = 9.5 \text{ mm}$  and  $\delta_d = 1.5 \text{ mm}$ , respectively. Figs. 3 and 4 show dispersion behavior of the input impedance and the reflection coefficient for the geometries shown in Fig. 2 (a) and (b) (cases (a) and (b) in Figs. 3 and 4). Due to the interaction with waveguide walls, the dispersion behavior in case (b) is quite different from that in case (a) (notice two resonance frequencies and narrow bandwidth in case (b)).





Fig. 2. (a) Geometry of infinite conductorbacked, probe-fed DRA. (b) Geometry of probe-fed DRA inside semi-infinite waveguide.

Fig. 3. Input impedance for the geometry in Fig. 2 (a), (b).

Based on the parameters from Fig. 2(b), the geometry of a waveguide-based coaxial probe-fed DRA shown in Fig. 1 was analyzed with a custom FDTD technique discussed in Section 2. For the rectangular coax of radius 1.2 mm and filled with the dielectric of permittivity  $\varepsilon_r = 2.56$ , the characteristic impedance  $Z_0$  is 51.98  $\Omega$ , and only the TEM mode is supported as the cutoff frequency of the TE<sub>11</sub> coaxial line mode is approximately 110 GHz. The probe length  $l_d$  is 4 mm and the probe axis is offset by  $\delta_d = 1.5$  mm from the waveguide centerline in the vertical direction. Fig. 5 shows the dispersion behavior of the S-parameters for this case. A -10 dB bandwidth of 10% is achieved (compared to the 3% bandwidth of a microstrip patch antenna used in a similar configuration [5]). The results in Fig. 5 are verified with commercial FDTD software [8] and exhibit very good agreement.





Fig. 4. Reflection coefficient for the geometry in Fig. 2 (a), (b).

Fig. 5. S-parameters for the waveguide-based probe-fed DRA ( $\delta_d = 1.5$  mm,  $l_d = 4$  mm).

For the structure operating in the X-band, the length and position of the probe in the waveguide may be used as parameters to control the matching as well as the overall frequency response. The length of the excitation probe  $l_d$  also affects significantly the overall return loss of the structure. Fig. 6 shows the return loss of the structure with different values of  $l_d$ . One can notice that a short probe couples weakly to the coaxial line. As the probe length increases, the coupling is increased and a shift of the resonant frequency is observed. As the probe becomes longer than 4.5 mm, the coupling to the coaxial line starts decreasing.



0 -5 -10 S111 (dB) -15 -20 = 0.5 mm $\ddot{\delta_d} = 1.0 \text{ mm}$ = 1.5 mm = 2.0 mm-30 12 à 10 11 Frequency(GHz)

Fig. 6. Effect of varying the probe length  $l_d$  in the DRA on the return loss ( $\delta_d = 1.5$ mm).

Fig. 7. Effect of varying the probe position  $\delta_d$  with respect to the DRA centerline on the return loss ( $l_d = 4$ mm).

The effect of the probe position  $\delta_d$  with respect to the waveguide centerline is illustrated in Fig. 7, which shows the reflection coefficient of the structure for different values of  $\delta_d$ . It is clear that both the probe length and position can be used to tune and control the response in order to obtain a desired return loss over the band of interest.

## 4. Conclusions

A coaxial probe-fed DRA in a rectangular waveguide excited by the incident dominant mode was analyzed by using a custom FDTD method. This analysis provided the necessary information for the optimization of design parameters such as DRA dimensions and the position and length of the excitation probe. Consequently, 10% bandwidth was achieved over the frequency band of interest. This study is a useful step in the extension to the case of the DRA array for increasing the output power and the power combining efficiency of waveguide-based spatial power combiners.

#### 5. Acknowledgment

This work was partially supported by the National Science Foundation under Grant No. ECS-0220218.

#### References

- [1] G. P. Junker, A. A. Kishk, and A. W. Glisson, "Input impedance of dielectric resonator antennas excited by a coaxial probe," *IEEE Trans. Antennas Propagat.*, vol. 42, pp. 960-966, July 1994.
- [2] G. P. Junker, A. A. Kishk, and A. W. Glisson, "Input impedance of aperture coupled dielectric resonator antennas," *IEEE Trans. Antennas Propagat.*, vol. AP-44, pp. 600-607, May 1996.
- [3] A. Petosa, A. Ittipiboon, Y. M. M. Antar, D. Roscoe, and M. Cuhaci, "Recent advances in dielectric-resonator antenna technology," *IEEE Antennas and Propagation Magazine*, vol. 40, No. 3, pp. 35-47, June 1998.
- [4] K. S. Kunz, and R. J. Luebbers, "The Finite Difference Time Domain Method for Electromagnetics", CRC Press, 1993.
- [5] M. Ozkar, *Electromagnetic modeling for the optimized design of spatial power amplifiers with hard horn feeds*, Ph.D. Dissertation, North Carolina State University, 2001.
- [6] K. M. Luk, and K. W. Leung, *Dielectric Resonator Antennas*, Hertfordshire, England: Research Studies Press Ltd., 2002.
- [7] B. M. Kolundzija, J. S. Ognjanovic, and T. K. Sarkar, WIPL-D: Electromagnetic Modeling of Composite Metallic and Dielectric Structures, Software and User's Manual. Reading, MA: Artech House, 2000.
- [8] QuickWave3D: A general purpose electromagnetic simulator based on conformal finite-difference time-domain method, v. 2.2, QWED Sp. Zo.o, Dec. 1998.