A Broadband Reflectarray Antenna using the Triangular Array Configuration

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\textbf{Abstract}—A novel broadband reflectarray cell element is designed for use in several offset-fed reflectarray antennas based on square and triangular lattice. The proposed double-layer element consists of two stacked rectangular patches having two slots in non-radiating edges. Reflection phase curves are obtained by changing simultaneously the slot’s length of top and bottom patch. The designed element exhibits a large phase-shift range in excess of 360°. This wideband cell element is designed to be used in a triangular lattice that eliminates the grating lobes for wideband reflectarrays composed of unit-cell larger than half-wavelength. Two 529-element square reflectarrays and two 518-element triangular reflectarray antennas were designed and simulated using CST and HFSS, for producing 20° and 35° off-broadside E-plane beams using a 20° offset feed. The 1-dB gain-bandwidth is about 30% at the center frequency of 14 GHz, and the maximum simulated gain is about 31 dBi which is equivalent to 51.5% aperture efficiency for a 20° off-broadside reflectarray based on triangular lattice configurations.

\textbf{Index Terms} — Cell element, gain-bandwidth, off-broadside reflectarray, triangular lattice.

\section{I. INTRODUCTION}

Traditional reflector antennas are widely used in communication systems due to their high gain and good efficiency. However, this type of antenna is not desired for some applications due to its space occupation and non-planar configuration. A new class of low profile antenna, named reflectarray antenna, has been introduced. This antenna utilizes some benefits of both reflector and phased array antennas. Due to their flat surface and printed radiating elements, there is no need for crucial mechanical manufacturing; and as a result of spatial feeding of array elements, the design complexity and high loss of feeding network are eliminated, so a higher efficiency would be achievable compared to phased arrays [1]. Other attractive properties of reflectarrays antennas are their low-cost and manufacturing simplicity compared to reflectors and phased arrays, and the possibility to generate reconfigurable features [2]. The main shortcoming is the narrowband operation compared to reflector antenna that is mainly because of intrinsic narrow
bandwidth of radiator element [3-4]. To collimate the main beam in a given direction, the elements of the reflectarray antenna must apply a specific phase-shift to the incoming spherical wave front generated by the feed. With a given feed position at a certain frequency, the required phase delay on the reflectarray surface is calculated. Different methods have been used to perform phase variation of reflectarray elements, such as variable size patches [5], slot-loaded patch [6-7], and aperture-coupled delay lines [8-9]. Besides, various kinds of structures are treated as reflectarray elements, like simple patches, loops, multi-layer configurations [10], elements with different rotation angles [11], and dielectric resonators [12]. To enhance the gain bandwidth of reflectarrays sub-wavelength patch elements have been proposed [13-14]. Also, cross and square loop elements with remarkable bandwidth and phase range properties on single-layer structure have been proposed to enhance the bandwidth of large reflectarrays [15-16].

In this paper, we utilize a triangular array configuration in designing reflectarray to eliminate the potential of grating lobes generation for wideband reflectarrays composed of a unit-cell larger than half a wavelength. Larger cell size may be applicable when we want to decrease the number of elements especially for reconfigurable reflectarray elements, which the maximum scan angle is limited by increasing the cell size. In this paper a wideband unit-cell is used. In the next sections we explain the unit-cell design and characteristics, then two reflectarrays are investigated and their simulated results are discussed.

II. CELL ELEMENT DESIGN AND SIMULATION

A. Proposed unit-cell

The presented unit-cell as shown in Fig. 1 is composed of two rectangular stacked patches on the top and bottom of RT/duroid 5880 substrate with thickness of 62mil and \( \delta=0.0009 \). A 2mm thick foam layer backed by the ground plane is inserted beneath the dielectric layer. Each patch has two identical slots in non-radiating edges. The phase-shift mechanism is introduced by variation of slot length. There is a possibility to make this element reconfigurable by means of a combination of MEMS switches as proposed in [17]. The scaling factor for top and bottom slot-patches is 0.6. The slot width for two patches was adjusted to the same value of 0.5mm. Also, the aspect ratio \( L_1/W_i, i=1,2 \) for each patch is 0.8. For more reliability the phase curve sensitivity to the foam thickness was simulated. The dimensions of cell element are as follows:

\[
\text{cell size}=13\text{mm}, W_1=10\text{mm}, W_2=0.6W_1, L_1=0.8W_1, L_2=0.6L_1, L_{s1}: \text{Variable}, L_{s2}=0.6L_{s1}, W_s=0.5\text{mm}
\]

![Fig. 1. Proposed unit-cell: stacked rectangular patches with two slots, top, and side view.](image)

The reflectarray was simulated for two different lattice configurations of square and triangular using CST software [18] with periodic boundary conditions and normal plane wave excitation as shown in Fig. 2. The cell element dimensions were adjusted to achieve a linear phase-length performance. A wideband linearly phase variation with the mentioned dimensions for unit-cell was obtained where the cell size is \( 13\text{mm}=0.6067\lambda_0 \) at 14 GHz. Figure 3 shows the magnitude response (loss) of the proposed element at different frequencies which exhibits very low loss properties. The phase-slot’s length curves for rectangular stacked patches exhibit almost linear behavior. More than 360° phase variation was achieved by changing the slot length. Figure 4 demonstrates the reflection phase response of the element versus slot length over frequency range of 12.5-15.5 GHz, with normal plane-wave

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excitation. A relatively wide linear reflection phase for this frequency range is achieved. There is no considerable difference between these two unit-cell configurations and both of them have broadband properties as reflectarray elements.

Fig. 2. Modeling of infinite array in CST for normal plane wave excitation (a) simulated unit-cell for square array (b) simulated unit-cell for triangular array.

Fig. 3. Reflection magnitude (simulation) versus lower slot length at different frequencies, (a) square array (b) triangular array.

B. Discussion on advantages of proposed element compared with other wideband unit-cells

In classic two-layer reflectarrays e.g. the proposed element in [6], the phase variation is introduced by changing the size of two stacked patches simultaneously. Therefore, it is difficult to include the reconfigurability in such a cell element. In this work, as the phase is only controlled by the slots’ lengths, it can easily be modified for dynamic phase control, e.g. using MEMS switch. Furthermore, the proposed element is etched on the top and bottom surfaces of the dielectric (RT/duroid 5880) layer in our case as compared to the multi-layer case which elements
are etched on different layers which make the fabrication more complex in this case.

On the other hand, comparing several wideband single-layer cell elements (some of them have been investigated [15-16]) with some multi-layer structures shows that more linear phase variations could be achieved when a multi-layer configuration is used since there are more parameters and space to play with in multi-layer configurations. In this design, we got the advantage of multi-layer configuration to generate a good linear phase-length curve and at the same time make the fabrication complexity something between single-layer and multi-layer configurations.

III. REFLECTARRAY DESIGN AND SIMULATION

All the reflectarrays, designed in this paper are offset-fed with a dimension of 30cm×30cm and F/D=0.9 as shown in Fig. 5. The feed location was calculated to provide 10 dB amplitude tapering on the aperture of the reflectarray. There are 23 elements in each direction with the cell size of 13mm×13mm.

The phase distribution on reflectarray surface is given by:

\[ \phi_i = k_0 \left( d_i - \left( x_i \cos \theta_b + y_i \sin \theta_b \right) \sin \theta_b \right), \]  

where \((\phi_b, \theta_b)\) denote the main beam direction, \(d_i\) is the distance between the source point and \(i\)-th element, and \((x_i, y_i)\) are the coordinates of the element \(i\). To realize the required phase-shift on the reflectarray surface the length of slots were determined using the phase curve of previous section at center frequency of 14 GHz. After applying these lengths, the reflectarray is modeled by the full-wave electromagnetic software CST Microwave Studio and Ansoft HFSS to validate the design. In all the simulations, a linearly polarized waveguide horn antenna was used to illuminate the reflectarray with the E-plane and H-plane patterns are approximated by \(\cos^{12} \theta\), as shown in Fig. 6. The feed which is fed by WR62 waveguide has an aperture size of 55.8mm × 43.9mm, and length=73.3mm. As an example, the calculated phase distribution at 14 GHz on a square lattice reflectarray to produce a 35° off-broadside beam is shown in Fig. 7.
Four offset-fed reflectarrays with square and triangular lattices are designed for producing 20° and 35° off-broadside main beams. First, these reflectarrays are compared from the computational cost point of view then a discussion will be carried out on their radiation properties and bandwidth performance in the next section. Two commercial software CST [18] and HFSS [19] were used for simulating these reflectarrays. Ansoft HFSS software is based on a three-dimensional full-wave finite element (FE) method for solving the differential form Maxwell's equations in the frequency-domain. Ansoft HFSS software automatically converts the whole structure into a finite element mesh which consists of a large number of very small 3D tetrahedral shapes. Typically, meshing or discretizing operations done by Ansoft HFSS is very coarse in almost the whole structure and it is very fine at some regions which need more accuracy such as near wave port, metallic edges or discontinuities. After finalizing the mesh operation of the whole structure, the solution process starts with two-dimensional (2D) port solutions then followed by the field solution of the full 3D problem. The program exploits the computed 2D fields on ports to be used as boundary conditions to solve the 3D fields of the whole structure. The other simulation software is CST Microwave Studio (MWS). CST MWS is based on the finite integration technique (FIT) which is equivalent to FDTD. Unlike the FE method, FIT is a time-domain numerical technique for solving Maxwell's equations. Using the function of the parametric study in both Ansoft HFSS and CST MWS simulation programs, we can tune and optimize the structure physical parameters to improve the design before going to fabrication process. CST MWS has different kinds of solvers not only transient solver but also frequency domain solver, Eigen mode solver and integral equation solver. There are several differences between these two CAD tools in defining the structure, solution setup, and solution methods. For convergence purposes, the main factors that may be considered in CST and HFSS are mesh properties and solution setup, respectively.

Numerical simulations have been carried out using a computer with Intel i7-920 (8 cores) CPU and 12 GB of RAM. Considering the available hardware, the complete structure (horn in front of the reflectarray) is completely simulated in CST. However, for simulating the structure in HFSS, the feed horn was simulated separately and its far-field results were used as excitation for the reflectarray antenna. In this simulation the coupling between the horn feed and reflectarray is not taken into account which is negligible for offset-fed configuration [2]. In the considered 11-18 GHz band with 0.25 GHz step, for more solution accuracy over the wide simulating band and reliable results it is better to define more than one solution setup in HFSS. The convergence criterion in CST and HFSS are different.

In CST, the convergence is controlled with a parameter called "accuracy". The accuracy setting in CST defines the steady-state monitor. It influences the duration of the simulation. It is a value for the accuracy of the frequency domain signals that are calculated by Fourier transformation of the time domain signals. To get a value for the accuracy, the amplitudes of the time signals as well as the total energy inside the calculation domain are used. During the simulation, the total energy value is frequently calculated and related to the maximum energy that has been monitored thus far [18]. In our simulations this parameter was set to -30 dB to insure an almost damped reflected time domain signal at the waveguide input port.

In HFSS, the convergence is defined in terms of "maximum delta energy". It is a stopping criterion for the adaptive solution when ports have not been defined as applied to our case where the excitation is an incident field. The error is a measure of the solution’s accuracy. This convergence criterion is based on the change in a computed energy term. As the solution converges, this term approaches constant value and the delta energy approaches zero. To minimize the delta energy, the system refines the mesh in tetrahedral shapes that have the largest error. The delta energy that appears on screen represents the delta energy for all tetrahedral [19]. In our simulations this parameter was set to 0.02 due to memory limitation and to have an acceptable accuracy.

A comparison between CST and HFSS simulations can be useful from the computational
cost point of view, as presented in Table 1. As compared in Table 1, considering the available memory, time, and desired bandwidth the reasonable choice for simulating a wideband reflectarray seems to be CST compared to HFSS. Due to a different meshing scheme, the number of mesh cells is not comparable to each other as shown in the last column of Table 1.

Table 1: Comparison of HFSS and CST simulations

<table>
<thead>
<tr>
<th>Reflectarray lattice and main beam direction</th>
<th>Software</th>
<th>Memory usage (GB)</th>
<th>Total simulation time (hrs:mins)</th>
<th>Number of mesh cells</th>
</tr>
</thead>
<tbody>
<tr>
<td>Triangular array 20°</td>
<td>CST 2010</td>
<td>9.1</td>
<td>6:40</td>
<td>66719526 hexahedral</td>
</tr>
<tr>
<td></td>
<td>HFSS v.12</td>
<td>10.4</td>
<td>11:36</td>
<td>452347 tetrahedral</td>
</tr>
<tr>
<td>Triangular array 35°</td>
<td>CST 2010</td>
<td>8.8</td>
<td>6:56</td>
<td>63702060 hexahedral</td>
</tr>
<tr>
<td></td>
<td>HFSS v.12</td>
<td>9.4</td>
<td>5:20</td>
<td>435721 tetrahedral</td>
</tr>
<tr>
<td>Square array 20°</td>
<td>CST 2010</td>
<td>9.4</td>
<td>7:31</td>
<td>66549120 hexahedral</td>
</tr>
<tr>
<td></td>
<td>HFSS v.12</td>
<td>8.4</td>
<td>5:06</td>
<td>4095539 tetrahedral</td>
</tr>
</tbody>
</table>

To demonstrate the agreement between the CST and HFSS results, the radiation patterns at 15 GHz and 16 GHz for two square arrays are compared in Fig. 8 and Fig. 9, respectively. Therefore, with respect to this similarity and for the sake of brevity, the obtained radiation pattern from CST is merely compared for the triangular and square lattice as provided in the next section.

IV. THEORETICAL ANALYSIS AND DISCUSSION ON SIMULATION RESULTS

A. Grating lobe problem

With scanning, lobes that were originally in imaginary space may move into real space if the element spacing is greater than \( \lambda / 2 \). As the array is scanned away from broadside, each grating lobe (in \( \sin \theta \) space, \( i.e. \varphi = 90^\circ \)) will move a distance equal to the sine of the angle of scan and in a direction determined by the plane of scan [20]. To ensure that no grating lobes enter real space, the element spacing must be chosen so that for the maximum scan angle \( \theta_0 \) the movement of a grating lobe by \( \sin \theta_0 \) does not bring the grating lobe into real space which is expressed as follows:

\[
\frac{s}{\lambda} < \frac{1}{1+|\sin \theta_0|}, \tag{2}
\]

where \( s \) is the cell size. The highest frequency that satisfies this condition is 17.2 GHz for \( \theta_0 = 20^\circ \) and 14.65 GHz when \( \theta_0 = 35^\circ \).

Fig. 8. Radiation pattern at 15 GHz for square array 20°, CST, and HFSS comparison.

Fig. 9. Radiation pattern at 16 GHz for square array 35°, CST and HFSS comparison.
Fig. 10. Comparison of 20° off-broadside reflectarray radiation patterns (E-plane) at (a) 14 GHz (b) 16 GHz (c) 17 GHz.

B. Simulation results: radiation patterns
The simulated radiation patterns in E-plane at 14 GHz, 16 GHz, and 17 GHz for the reflectarray with main beam at 20° and 35° are shown in Fig. 10 and Fig. 11, respectively.

Regarding the above analysis, it can be seen in Fig. 10 that for 20° main beam, the radiation
patterns of square and triangular lattices are appropriate; although the grating lobe is appearing at 17 GHz for square lattice.

On the other hand, as demonstrated in Fig. 11 when the main beam is directed to 35° off-broadside, the grating lobe level for the square lattice is significantly higher than the triangular lattice due to the grating lobe generated in the square lattice reflectarray. It is to be noted that whereas the main beam is scanned in E-plane, consequently the grating lobe in H-plane does not exist and therefore most of results are presented in E-plane (φ=90°). However, regarding the ±45° plane, there are some side lobes but in much lower level than the grating lobe in E-plane. Also, radiation patterns at φ=45° and φ=0° (H-plane) have been compared for the square and triangular lattices at 17 GHz, as shown in Fig. 12.

Figure 13 shows the 3D radiation patterns for 35° off-broadside reflectarray designed on triangular configuration at 17GHz.

![3D radiation pattern](image)

C. Simulation results: gain curves

The calculated gain using CST and HFSS are compared in this section. The simulated gain versus frequency for four reflectarrays is shown in Fig. 14 to Fig. 17. Comparing these figures provides a better insight into the bandwidth performance of the reflectarray based on the triangular and square lattices.

Refering to radiation patterns shown in Fig. 10, the gain curves of Fig. 14 and Fig. 15 are obtained. As it can be seen for both CST and HFSS results the triangular reflectarray with main beam at 20° exhibits a simulated 1-dB gain-bandwidth of about 30% which is higher than the square array’s one. However, for 20° square reflectarray the grating lobe is slightly observed at higher frequencies.

Similarly, refering to radiation patterns presented in Fig. 11, the gain curves of Fig. 16 and Fig. 17 are derived. Comparing the gain results in these figures shows that the triangular reflectarray with main beam at 35° exhibits a simulated 1-dB gain-bandwidth of about 3.5 GHz which is much higher than the square array. In the case of square lattice for 35° main beam, a sharp drop in gain can be seen for frequencies higher than 14.5 GHz, which is mainly due to the grating lobe. However, using the triangular array configuration, the grating lobe is eliminated and consequently gain

![Gain curve comparison](image)

Fig. 12. Cut-plane patterns at 17 GHz, 35° off-broadside reflectarray, (solid) square lattice, (dashed) triangular lattice (a) H-plane, (b) 45° plane.
bandwidth increases due to a gain increment at higher frequencies. In other words, using triangular array leads to compensation and stability of gain curve especially at upper frequencies of operation. Furthermore, the grating lobe problem can be untangled in this way particularly when a large angle of scan is needed for a broadband reflectarray.

V. CONCLUSION

A novel broadband reflectarray cell element is presented. This unit-cell was used for designing several 30 cm × 30 cm offset-fed reflectarrays at Ku-band. A 20° offset-fed configuration was chosen to produce 20° and 35° off-broadside main beam. Whereas, the element spacing is greater than λ/2 and the main beam is scanned away from broadside the triangular array lattice is utilized to avoid grating lobe issue at higher frequencies. Results showed that we can design reflectarray based on triangular array where the unit cell size is more than half wavelength, especially when a large angle of scan is required in a broadband reflectarray. Comparing CST and HFSS results showed that CST is faster than HFSS for simulating wideband reflectarrays. The simulated results show a significant improvement in the radiation pattern and gain bandwidth of the reflectarray, when we utilize the advantages of the triangular lattice in designing reflectarray rather than the conventional square one, especially for main beam at 35°. Also, the triangular reflectarray with main beam at 20° exhibits the simulated 1-dBgain-bandwidth of 30% which is considerable for a reflectarray antenna.

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