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Mathematical Model for Calibration of Potential Detection of Nonlinear Responses in Biological Media Exposed to RF Energy

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Abstract — An efficient way to test for potential unsymmetrical nonlinear responses in biological tissue samples exposed to a microwave signal is to observe the second harmonic in a cavity resonant at the two frequencies, with collocated antinodes. Such a response would be of interest as being a mechanism that could enable demodulation of information-carrying waveforms. In this work, an electric circuit model is proposed to facilitate calibration of any putative nonlinear RF energy conversion inside a high quality-factor resonant cavity with a known nonlinear loading device. The first and second harmonic responses of the cavity due to loading with the nonlinear and lossy material are also demonstrated. The results from the proposed mathematical model give a good indication of the input power required to detect any very weak second harmonic signal in relation to the sensitivity of the measurement equipment. Hence, this proposed mathematical model will assist in determining the level of the second harmonic signal in the detector as a function of the specific input power applied.

Index Terms — Biological responses, nonlinearity, quality factor, resonant cavity, second harmonic.

I. INTRODUCTION

With the explosive growth of mobile communications, large numbers of researchers around the world have studied the interaction mechanisms between electromagnetic fields and biological tissues. The result has been the development of research streams in different aspects of bioelectromagnetic problems at various levels of definition such as tissue level, cell level and ionic level, with intensive effort worldwide [1-17].

However, most of the previous analyses have been performed treating bulk tissue effects as a linear problem. Recently, the tendency of research in this area has moved towards seeking evidence for the existence of nonlinear tissue responses, involving microscopic studies of cellular and molecular processes. Many experiments have been proposed in order to clarify the various nonlinearity hypotheses for biological tissue. Balzano [4-8] has suggested that the detection of the presence of nonlinear interactions can be investigated by exposing living cells to low-amplitude unmodulated RF carriers and observing the possible generation of second harmonics. Such harmonics would be inherent in any unsymmetrically-nonlinear medium; a property essential for demodulation of modulated waveforms. Demodulation has been postulated as a plausible mode for putative non-thermal effects of RF radiation on living organisms.

By implementing a doubly harmonic resonant cavity model, as proposed in [4-8], this paper presents an electric circuit model to verify second harmonic generation from a known nonlinear device and suggests the required level of input power needed to excite the
bio-preparation in order to maximize the chance of detection of a possible second harmonic signal.

II. METHODOLOGY

The proposed mathematical model is an extension of some earlier work [18]. It consists of two parts: cavity model design and electric circuit model. The cavity model will be first described and S-parameters of the model will be extracted by using CST Microwave Studio software [19]. Once these data are obtained, they will be adopted into the derived equations from the proposed circuit model to calculate the second harmonic power with known input power.

A. Cavity model design

The previously-reported practical work was undertaken with a carrier frequency in the 880-890 MHz band. To investigate whether biological cells exhibit unsymmetrical nonlinearity when exposed to such RF energy, a high quality-factor resonant cylindrical cavity was created, having diameter and height of 248 mm and 272 mm respectively. The cavity was built with two rectangular loop coupling antennas and a support structure for biopreparations, i.e., a butterfly-shaped Lexan lamina and Petri dish, as shown in Fig. 1. As can be seen, the antenna with size 14x105 mm$^2$ at the bottom of the cavity acts as a transmitter to excite the TE$_{111}$ cavity mode in the 880-890 MHz band; whereas the antenna with size 12.5 x 56.5 mm$^2$ on the side wall of the cavity was used to detect the energy of the TE$_{113}$ cavity mode in the range 1760-1790 MHz. It should be noted that the lengths of the transmit and receive antennas were fine tuned in order to achieve the TE$_{113}$ mode resonant at exactly double the frequency of the TE$_{111}$ mode.

B. Electric circuit model for calibrations

In order to more precisely quantify the amount of input power required in the excitation port to generate a detectable second harmonic signal, a mathematical technique is proposed here to calculate the second harmonic level with known input power.

The procedure of the proposed mathematical model will be demonstrated in the following context. Firstly, the same cavity model used in previous analyses will be implemented. A discrete floating port with metal leads of 1 mm length, resembling a dipole antenna, is placed inside the Petri dish in the cavity and oriented parallel to the transmit antenna, as depicted in Figs. 2 and 3. Then, two simulations will be performed separately at the resonant frequencies of the TE$_{111}$ and TE$_{113}$ modes, in order to extract the 3×3 Z-parameters at both frequencies. This is equivalent to the 3-port network as depicted in Fig. 4. Once the 3×3 Z-parameters are obtained at both frequencies, they will be employed in the proposed mathematical model as depicted in Fig. 5. According to Fig. 5, the input and output ports can be represented as transmit and receive antennas respectively in the cavity, while the nonlinear element is represented as the diode inside the cavity. The equivalent electric circuit of the diode model is illustrated in Fig. 6.
From Figs. 5 and 6, by applying Ohm’s law, the following equation can be derived:
\[
\begin{bmatrix}
V_1 \\
V_2 \\
V_3
\end{bmatrix} =
\begin{bmatrix}
Z_{11} & Z_{12} & Z_{13} \\
Z_{21} & Z_{22} & Z_{23} \\
Z_{31} & Z_{32} & Z_{33}
\end{bmatrix}
\begin{bmatrix}
I_1 \\
I_2 \\
I_3
\end{bmatrix}.
\]
(1)

From the input port in Fig. 5:
\[
I_1 = \frac{V_1 - V_i}{Z_0},
\]
(2)

where \(V_i\) is the input voltage to port 1 and \(Z_0\) is the characteristic impedance of 50 \(\Omega\). From the output port in Fig. 5, \(I_2\) is given by:
\[
I_2 = \frac{V_o}{Z_o}.
\]
(3)

From the diode model in Figs. 5 and 6:
\[
I_3 = I_c + I_d,
\]
(4)

where \(I_d\) is the current across the diode and \(I_c\) is the current across the capacitor in the diode model, as seen in Fig. 6.

From Equation (4), \(I_3\) can be further extended to the following equation:
\[
I_3 = \frac{V_i}{j \pi c} + I_d,
\]
(5)

where:
\[
I_d = I \left( e^{\frac{\pi e}{4kT}} - 1 \right),
\]
(6)

where \(e\) is the electron charge (\(e=1.60217\times10^{-19}\) coulombs):
\(T\) is the temperature in Kelvin (\(T=300\) K),
\(I_s\) is the reverse current (\(I_s=1.0\times10^{-14}\) A),
\(k\) is the Boltzmann Constant (\(k=1.38065\times10^{-23}\) JK\(^{-1}\)),
\(V_s = \frac{V_o}{\pi c} + I_d R_c\).
(7)

Substituting the Equations (2 to 7) into (1), the following expression can be obtained:
\[
\begin{bmatrix}
V_1 \\
V_2 \\
V_3
\end{bmatrix} =
\begin{bmatrix}
Z_{11} & Z_{12} & Z_{13} \\
Z_{21} & Z_{22} & Z_{23} \\
Z_{31} & Z_{32} & Z_{33}
\end{bmatrix}
\begin{bmatrix}
\frac{V_1 - V_i}{Z_o} \\
\frac{V_2}{Z_o} \\
\frac{V_3}{j \pi c} + I_d
\end{bmatrix}.
\]
(8)

where \(R_s=106.5\) \(\Omega\) and \(C_s=1.5\) fF, obtained from reference [20]. \(V_i\) is the input voltage to port 1.

Since \(e\), \(K\), \(T\) and \(I_s\) are known parameters, Equation (6) can be simplified as follows:
\[
I_d = I_s \left( e^{\frac{\pi e}{4kT}} - 1 \right) = 1.0\times10^{-14} \left( e^{38.681514} - 1 \right).
\]
(9)

By assuming the input voltage and substituting the \(Z\)-parameters of \(TE_{111}\) into Equation (8), the parameters \(V_1\), \(V_2\) and \(V_d\) can be found. Then, the input power of the mathematical model can be computed by \(P_{in} = 0.5 \text{Re} \left( V_i \times I_i^* \right)\).

Once \(V_d\) is obtained, it can be used as the excitation source to the previous input and output port, hence the electric circuit can be modified as shown in Fig. 7. From this figure, the following set of equations can be established:
By substituting $V_d$ from the solution of Equation (8) into Equation (10), $V_1$, $V_2$ and $V_3$ can be computed. Hence, the output power on port 2 can be calculated by $P_{out} = 0.5 \text{Re} \left( V_2 \times I_z \right)$.

Fig. 7. Proposed mathematical model for TE$_{113}$ mode.

**III. SIMULATION AND RESULTS**

The bands of operation of the two antennas are shown in Fig. 8. Here the dashed line represents the return loss of the bottom (excitation) antenna at its frequency of operation with an empty 3 cm Petri dish. The frequency has been multiplied by a factor of two to display the second harmonic performance in the same band as the high frequency antenna (receive antenna). The solid line in Fig. 8 illustrates the shift of operating frequency band when a 15μm lamina of lossy water is added to the Petri dish in the cavity, having properties $\varepsilon_r = 78.24$, $\sigma = 0.173 \text{ S/m}$ [2, 13].

Table 1 shows the results obtained from the proposed mathematical model. In order to cross-validate the result, ANSYS HFSS software was adopted for comparison [21]. Figure 9 illustrates the second harmonic power as a function of the input power as the input voltage was increased. As can be clearly seen, both simulation results were in good agreement. Further, it is observed that the relationship between input power and second harmonic output power, applying the Silicon diode model adopted here, is slightly nonlinear. Moreover, the presented results have also compared with the measured results achieved by [8] and it was found that both are agreed well in terms of the level of the second harmonic.

Table 1: Input power versus second harmonic power

<table>
<thead>
<tr>
<th>Input Voltage (Volts)</th>
<th>Input Power (Watts)</th>
<th>Second Harmonic Power (Watts)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.0025</td>
<td>1.1924e-008</td>
</tr>
<tr>
<td>2.5</td>
<td>0.0156</td>
<td>7.4573e-008</td>
</tr>
<tr>
<td>5</td>
<td>0.0625</td>
<td>2.9818e-007</td>
</tr>
<tr>
<td>7.5</td>
<td>0.1405</td>
<td>6.7098e-007</td>
</tr>
<tr>
<td>10</td>
<td>0.2499</td>
<td>1.1942e-006</td>
</tr>
<tr>
<td>12.5</td>
<td>0.3904</td>
<td>1.8929e-006</td>
</tr>
<tr>
<td>15</td>
<td>0.5622</td>
<td>2.5478e-006</td>
</tr>
<tr>
<td>17.5</td>
<td>0.7652</td>
<td>3.2223e-006</td>
</tr>
<tr>
<td>20</td>
<td>0.9994</td>
<td>3.9630e-006</td>
</tr>
<tr>
<td>22.5</td>
<td>1.2649</td>
<td>4.7811e-006</td>
</tr>
<tr>
<td>25</td>
<td>1.5616</td>
<td>5.6810e-006</td>
</tr>
<tr>
<td>27.5</td>
<td>1.8895</td>
<td>6.6632e-006</td>
</tr>
<tr>
<td>30</td>
<td>2.2487</td>
<td>7.7299e-006</td>
</tr>
</tbody>
</table>
IV. CONCLUSION
A simulated cylindrical cavity model has been presented, using two rectangular loop antennas for coupling and loaded with a support structure for testing of nonlinear materials. The simulated results show that the tuned $TE_{113}$ mode has double the resonant frequency of the $TE_{111}$ mode. A simple electric circuit model was proposed to calibrate and check the required sensitivity of the detection of the generated second harmonic signal. The nonlinear response of the experiment was tested using a simulated chip diode connected to very short dipole arms. For the diode modelled, a nonlinear relationship was demonstrated between fundamental input power and second harmonic output power. The methodology presented can thus be used to predict such relationships for other nonlinear devices and frequencies applied to the Balzano cavity method or, with some modification, to deduce properties of unknown materials from measured results.

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[21] ANSYS HFSS software, ANSYS Inc., Canonsburg, PA, USA.

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Time-Domain Electromagnetic Inversion Technique for Biological Tissues by Reconstructing Distributions of Cole-Cole Model Parameters

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Abstract — The Cole-Cole (C-C) models have been frequently used for a precise description of the dispersion characteristics of biological tissues. One of the main difficulties in the direct reconstruction of these dielectric properties from time-domain measurements is their frequency dependence. In order to overcome this difficulty, an electromagnetic (EM) inversion technique in the time domain is proposed, in which four kinds of frequency-independence model parameters, the optical relative permittivity, the static conductivity, the relative permittivity difference, and the relaxation time, can be determined simultaneously. It formulates the inversion problem as a regularized minimization problem, whose forward and backward subproblems could be solved iteratively by the finite-difference time-domain (FDTD) method and any conjugate gradient algorithm, respectively. Numerical results on two types of stratified C-C slabs, with smooth and discontinuous parameter profiles, respectively, confirm the performance of the inversion methodology.

Index Terms — Biological tissues, conjugate gradient methods, electromagnetic scattering by dispersive media, electromagnetic scattering inverse problems, finite-difference time-domain (FDTD) methods, regulators.

I. INTRODUCTION

The electromagnetic (EM) inverse scattering problems, which aim to estimate the EM properties from the measurements outside the object of interest, have attracted increasing attention recently, due to their extensive application fields, and some promising results [1-3]. Nevertheless, in general, there are two major difficulties for these problems: one difficulty is their nonlinearity, and the other is the non-uniqueness of their solution [4].

Methodologically, the EM scattering inverse problem may be solved in the frequency domain [5] or the time domain [6]. By contrast, the time-domain reconstructed results are better than those by applying any single-frequency technique in the amount of information and the resolution of images [1, 6, 7]. Currently, several inversion approaches in the time domain for nondispersive media have been developed, such as the forward-backward time-stepping (FBTS) method [8] and the Lagrange multipliers technique [9]. However, in the real world, the wideband dielectric properties of biological tissues are dispersive, which have been widely described by the Debye or Cole-Cole (C-C) models, but the precision of the former is not better than that of the latter [10]. One basic difficulty in the time-domain reconstruction of the electrical characteristics is their frequency correlation. To date, a few time-domain inversion methods for Debye media have been proposed [6, 11]. Unfortunately, for C-C frequency-dependent media, the existing methods are not suitable, and few inverse methods are available directly.

Recently, several finite-difference time-domain (FDTD) forward solvers suitable for C-C media have been presented [12, 13], which have laid the groundwork for the research of inverse solvers for this class of media. There are two novelties in this paper. One novelty is to present a new inverse EM scattering technique, which is to reconstruct the C-C model parameters by means of measurements in the time domain directly. And the other innovation is to introduce a regularization scheme to cope with the ill-posedness of the inverse problem, which was not used in references [1, 6, 11].

II. INVERSE SCATTERING TECHNIQUE IN THE TIME DOMAIN

A. Problem formulation

Suppose that a problem space $V$, occupied by some biological tissues, is surrounded by a region $D$, filled with a known background medium. Also, it is assumed that all the media are linear, isotropic, and nonmagnetic, and that the complex-valued relative permittivity, $\varepsilon_r$, of the media within $V$ is modeled by the single pole C-C electrical dispersion equation as [10]:

$$
\varepsilon_r(\omega) = \varepsilon_\infty - j\sigma_\omega/(\omega\varepsilon_\infty) + \Delta\varepsilon/[1+(\omega\tau)^\alpha].
$$

(1)

where $\Delta\varepsilon = \varepsilon_\infty - \varepsilon_\infty$, $\varepsilon_\infty$, and $\varepsilon_\infty$ are the static and optical relative permittivity, respectively, $\sigma_\omega$ is the static
conductivity, \( r \) and \( \alpha \) (0 \leq \alpha \leq 1) denote the relaxation time and the dispersion breadth, respectively, \( j^2 = -1, \varepsilon_0 \) is the dielectric constant of free space, and \( \omega \) represents the angular frequency.

For simplicity, we assume that \( \alpha \) is \textit{a priori} known (it is appropriate for most biological tissues since they are not distinctly different in a wide frequency range [10]).

Our objective is to determine four kinds of unknowns, \((\varepsilon_\alpha, \sigma_\alpha, \Delta \varepsilon, \text{ and } r)\), for every position within \( V \). These C-C model parameters can be explicitly shown in the following field equations when activating the \( m \)th incidence for the time interval \([0, T]\):
\[
\nabla \times \mathbf{E}_i + \mu_0 \frac{\partial}{\partial t} \mathbf{H}_i = 0, \quad (2)
\]
\[
\nabla \times \mathbf{H}_i - \varepsilon_0 \varepsilon_\alpha \frac{\partial}{\partial t} \mathbf{E}_i - \sigma_\alpha \mathbf{E}_i - \mathbf{J}_i - \mathbf{J}^*_i = 0. \quad (3)
\]
and a fractional auxiliary differential equation (ADE) [13]:
\[
\mathbf{J}_{ij} + \tau^a D^\alpha_{\tau} \mathbf{J}_{ij} - \varepsilon_\alpha \Delta \varepsilon \mathbf{E}_i = 0, \quad (4)
\]
where \( \mu_0 \) is the free-space permeability, \( \mathbf{E}_i, \mathbf{H}_i, \) and \( \mathbf{J}_i \) are the electric field intensity, magnetic field intensity, and dispersion current, respectively, \( \mathbf{J}_i \) is the current density, \( \nabla \) is the Hamilton operator, and \( \frac{\partial}{\partial t} \) and \( D^\alpha_{\tau} \) denote \( t^\alpha \)-order and \( \alpha^\text{th} \)-order temporal partial differential operators with respect to time variable, \( t \), respectively.

**B. Constrained minimization problem**

In order to cope with the nonlinearity of the aforementioned inverse problem, we formulate it as a constrained minimization problem:
\[
\mathbf{p} = \arg \min_{\mathbf{p}} \left[ F(\mathbf{p}) \right],
\]
\[
\text{s.t. } (2)-(4), \quad (5)
\]
where the estimated parameters \( \mathbf{p} = [\varepsilon_\alpha, \sigma_\alpha, \Delta \varepsilon, r] \), and the cost functional \( F \) is given by:
\[
F = \frac{1}{2} \sum \sum \int_0^T \left[ \mathbf{E}_{ij}(\mathbf{p}) - \mathbf{E}_{ij}^{\text{mea}} \right]^2 dt + \frac{1}{2} \sum \int_0^T \left[ \nabla p_m \right]^2 dv. \quad (6)
\]

In the right hand side of (6), the first term formulates inversion error, in which \( \mathbf{E}_{ij} \) and \( \mathbf{E}_{ij}^{\text{mea}} \) represent the calculated and measured electric fields at the \( j \)th receiving position due to the \( i \)th incident wave, respectively, and \( I \) and \( J \) denote the total number of transmitters and receivers, respectively. While the second term, which is not contained in references [1, 6, 11], is incorporated to regularize the ill-posedness of the inverse problem, in which \( \gamma_m (m = 1, 2, 3, 4) \) are four positive Tikhonov regularization factors.

**C. Unconstrained minimization problem**

Based on the method of the Lagrange penalty function, the above constrained minimization problem is turned into an unconstrained minimization one, whose augmented cost functional \( F^a \) is represented as:
\[
F^a = \sum \int_0^T \left[ \mathbf{e}_i \cdot \left( \nabla \times \mathbf{H}_i - \varepsilon_0 \varepsilon_\alpha \frac{\partial}{\partial t} \mathbf{E}_i - \sigma_\alpha \mathbf{E}_i - \mathbf{J}_i - \mathbf{J}^*_i \right) + \mathbf{h}_i \cdot \left( \nabla \times \mathbf{E}_i + \mu_0 \frac{\partial}{\partial t} \mathbf{H}_i \right) + \mathbf{q}_i \cdot \left( \mathbf{J}_i + \tau^a D^\alpha_{\tau} \mathbf{J}_i - \varepsilon_\alpha \Delta \varepsilon \mathbf{E}_i \right) \right] dv dt + F, \quad (7)
\]
where \( \mathbf{e}_i, \mathbf{h}_i, \) and \( \mathbf{q}_i \) are the Lagrange vector multipliers.

**D. Fréchet derivatives**

Solving (7) by the variational method [14], we have \( \delta F^a = 0 \), where \( \delta \) denotes the first-order variation operator. After some calculus of variations similar to [1, 6, 11], it can be derived that the fields \( \mathbf{e}_i, \mathbf{h}_i, \) and \( \mathbf{j}_i \) \((\mathbf{j}_i = -\varepsilon_\alpha \Delta \varepsilon \mathbf{q}_i)\) must satisfy the following equations for the time interval \([T, 0] \):
\[
\nabla \times \mathbf{E}_i - \mu_0 \frac{\partial}{\partial t} \mathbf{H}_i = 0, \quad (8)
\]
\[
\nabla \times \mathbf{H}_i + \varepsilon_0 \varepsilon_\alpha \frac{\partial}{\partial t} \mathbf{E}_i - \sigma_\alpha \mathbf{E}_i - \mathbf{j}_i + \sum \left[ \mathbf{E}_{ij} - \mathbf{E}_{ij}^{\text{mea}} \right] = 0, \quad (9)
\]
\[
\mathbf{j}_i - \tau^a D^\alpha_{\tau} \mathbf{j}_i + \varepsilon_\alpha \Delta \varepsilon \mathbf{e}_i = 0. \quad (10)
\]
and that the Fréchet derivatives (gradients) of \( F^a \) with respect to \( p_m \) are denoted as:
\[
g_{\varepsilon_\alpha} = \frac{\delta F^a}{\delta \varepsilon_\alpha} = -\varepsilon_0 \sum \int_0^T \left( \mathbf{e}_i \cdot \frac{\partial}{\partial \varepsilon_\alpha} \mathbf{E}_i \right) dt / \gamma_1 \sqrt[2]{\varepsilon_\alpha}, \quad (11)
\]
\[
g_{\sigma_\alpha} = \frac{\delta F^a}{\delta \sigma_\alpha} = -\varepsilon_0 \sum \int_0^T \left( \mathbf{e}_i \cdot \mathbf{E}_i \right) dt / \gamma_2 \sqrt[2]{\sigma_\alpha}, \quad (12)
\]
\[
g_{\Delta \varepsilon} = \frac{\delta F^a}{\delta \Delta \varepsilon} = -\left[ \sum \int_0^T \left( \mathbf{j}_i \cdot \mathbf{E}_i \right) dt / \Delta \varepsilon \right] / \gamma_3 \sqrt[2]{\Delta \varepsilon}, \quad (13)
\]
\[
g_{r} = \frac{\delta F^a}{\delta r} = \left[ \alpha \tau^a r \sum \int_0^T \left( \mathbf{j}_i \cdot \mathbf{E}_i \right) dt / \varepsilon_0 \Delta \varepsilon \right] - \gamma_4 \sqrt[2]{r}, \quad (14)
\]
where \( D^\alpha_{\tau} \) indicates a fractional differential operator, whose numerical treatment could be found in [15], the direct fields \( \mathbf{E}_i, \mathbf{H}_i, \) and \( \mathbf{j}_i \) and the adjoint fields \( \mathbf{e}_i, \mathbf{h}_i, \) and \( \mathbf{j}_i \) can be calculated by using the FDTD method based on approximation of the Grünwald-Letnikov fractional derivative, from (2)–(4) and (8)–(10), respectively [13].

**E. Inversion algorithm**

In this work, we select the Polak-Ribiére-Polyak conjugate gradient algorithm [16] to solve the derived problem. Let the discretized forms of the C-C model parameters and gradients be represented by:
\[
\mathbf{x} = [\varepsilon_\alpha^1, \varepsilon_\alpha^2, \sigma_\alpha^1, \sigma_\alpha^2, \Delta \varepsilon^1, \Delta \varepsilon^2, \tau^1, \tau^2]^T, \quad (15)
\]
and
\[ \mathbf{g} = \left[ g_{a_1}, \ldots, g_{a_n}, g_{b_1}, \ldots, g_{b_m} \right]^T, \]  
\[ g_{\Delta d}, \ldots, g_{\Delta d'}, g_{\Delta d''}, \ldots, g_{\Delta d'''} \right]^T, \]  
respectively. Given that the estimated value of \( \mathbf{x} \) at the \( k \)th iteration, \( \mathbf{x}_k \), is achieved, the next estimated \( \mathbf{x}_{k+1} \) is updated by:
\[ \mathbf{x}_{k+1} = \mathbf{x}_k + \Delta_k \mathbf{d}_k, \]
where \( \Delta_k \) is the step size, and the direction \( \mathbf{d}_k \) is given by [16]:
\[ \mathbf{d}_k = \begin{cases} -g_k, & (k = 1), \\ -g_k + \frac{g_k^T (g_k - g_{k-1})}{g_{k-1}^T g_{k-1}}, & (k \geq 2), \end{cases} \]
where \( g_k \) denotes the estimated value of \( \mathbf{g} \) at the \( k \)th iteration.

At the \( k \)th iteration, the relative mean square error \( e \) between the true parameters \( \mathbf{x} \) and estimated ones \( \mathbf{x}_k \) is defined as:
\[ e(k) = \frac{\| \mathbf{x} - \mathbf{x}_k \|_2}{\| \mathbf{x} \|_2}. \]

The above inverse problem is solved iteratively until a predetermined error threshold \( e_{th} \) is reached or a predefined iteration number \( k_{pre} \) is finished. The basic steps of the inversion algorithm are illustrated in Fig. 1.

Fig. 1. Basic flow-chart of the proposed inversion technology.

### III. NUMERICAL RESULTS AND DISCUSSION

In this section, two simple one-dimensional (1-D) numerical examples, similar to [1, 6], are provided to examine the performance of the newly-elaborated approach. The geometry of the examples is shown in Fig. 2, in which either side of a \( 4d \)-width objective region is surrounded by a known background medium (air) where \( d = 10 \) mm, and all their electrical properties depend only on \( z \) coordinate, where the positive direction of \( z \) axis is from left to right, and \( z = 0 \) is on the left plane of the left background medium.

The objective region consists of layered C-C medium with a parameter of \( a = 0.8 \). In the background medium, a bistatic detection system is applied where two transmitters (\( I = 2 \), denoted by T, are symmetrically placed at distance equal to \( d/2 \) from both sides of the objective region, while two receivers (\( J = 2 \), denoted by R, are placed at symmetrical distance equal to \( d/4 \) from both sides of the objective region. An ultra-wideband pulse of the excitation source for transmitters is selected the same as [12]:
\[ s(t) = \sin\left(2\pi f_e (t - 4/\alpha)\right) \exp\left(-\alpha^2 (t - 4/\alpha)^2\right). \]

where \( \alpha = 1.26 \times 10^4 \), and central frequency \( f_e = 3 \) GHz.

Fig. 2. Geometry model of 1-D problem.

The FDTD method is applied to compute the direct and adjoint fields [13]. The FDTD solution space, which is bounded by the five-cell convolution perfectly matched layer (CPML) [17], consists of 120 homogeneous cells with spatial size \( \Delta z = 0.5 \) mm and time step \( \Delta t = 0.5 \Delta z / c_0 \), where \( c_0 \) is the speed of light in free space. Therefore, the total number of unknowns is 320. In this work, the necessary measurement data came from the similar FDTD simulation with \( T = 1500 \Delta t \), but its cell size is twice finer than the one used in the inverse solver to avoid the “inverse crime”.

Besides, it is assumed that the location and width of the reconstruction region are \textit{a priori} known, that a set of values (6.0, 0.5 S·m\(^{-1}\), 20.0, and 7.0 ps), which are the average values of the C-C model parameters (\( \varepsilon_r \), \( \sigma \), \( \Delta \), and \( \tau \)) within the objective region, is selected as an initial guess of the inversion algorithm, and that the specific stopping condition for the iterative algorithm is that the reconstruction errors are not declining or \( k_{pre} = 30 \).

In the first example, the spatial distribution profiles of the four parameters within the entire objective region are smooth (sinusoidal or cosinusoidal), whose (peaks, valleys) for \( \varepsilon_r \), \( \sigma \), \( \Delta \), and \( \tau \) are (10.0, 2.0), (0.9 S·m\(^{-1}\), 0.1 S·m\(^{-1}\)), (30.0, 10.0), and (8.0 ps, 6.0 ps), respectively.

Firstly, the regularization term is not applied in the noiseless case (i.e., \( \gamma = 0 \) with \( m = 1, 2, 3, 4 \)). After 30 iterations, the estimated optical relative permittivity, static conductivity, relative permittivity difference, and relaxation time are obtained as shown in subfigures (a)–(d) of Fig. 3. In these subfigures, the solid black lines, small red dots, and small blue circles depict the true distributions, start values, and end values, respectively (similarly for the later cases).
Fig. 3. The reconstructed distributions of: (a) optical relative permittivity, (b) static conductivity, (c) relative permittivity difference, and (d) relaxation time for a stratified Cole-Cole slab with smooth model parameter profiles, using noiseless data without regularization, at the 30th iteration. For comparison purpose, its corresponding original distributions with smooth profiles, and homogeneous initial guess are given, too (similarly for later cases).

As can be seen in Fig. 3, the proposed method for the non-regularized 1-D problem is convergent when noise is not considered, and that all the model parameters of the C-C dispersive media are reconstructed precisely.

Secondly, it is assumed that the measured fields are corrupted by the additive white Gaussian noise (AWGN) with a signal-to-noise ratio (SNR) of 20 dB. The same procedures as the previous case are repeated, where no regularization scheme is adopted yet. Numerical experiments show that the reconstruction errors are not decreased just after 14 iterations. The estimated optical relative permittivity, static conductivity, relative permittivity difference, and relaxation time are obtained as illustrated in subfigures (a)–(d) of Fig. 4 at the 14th iteration, where the estimated relative mean square error is about 0.25.

From Fig. 4, it is obvious that all the estimated distributions are poor, especially for the optical relative permittivity and relaxation time.

Finally, suppose that the simulated measurement field data are corrupted by the AWGN with a SNR of 20 dB, too. To test the performance of the regularized inversion algorithm, four of regularization factors ($\gamma_1$, $\gamma_2$, $\gamma_3$, and $\gamma_4$) are chosen to be (0.01, 0.001, 0.01, and 0.0001), respectively. It is noteworthy that these factors could be not optimal. The estimated optical relative permittivity, static conductivity, relative permittivity difference, and relaxation time are obtained as given in subfigures (a)–(d) of Fig. 5 at 30th iteration.

Fig. 4. The reconstructed distributions of: (a) optical relative permittivity, (b) static conductivity, (c) relative permittivity difference, and (d) relaxation time for a stratified Cole-Cole slab with smooth model parameter profiles, applying noisy data (SNR = 20 dB) without regularization, at the 14th iteration.

Fig. 5. The reconstructed distributions of: (a) optical relative permittivity, (b) static conductivity, (c) relative permittivity difference, and (d) relaxation time for a stratified Cole-Cole slab with smooth model parameter profiles, using noisy data (SNR = 20 dB) with regularization, at the 30th iteration.

Figure 5 shows that the recreated model parameters of the C-C dispersive media are satisfactory, even based on the noise-contaminated data with a SNR of 20 dB, which could benefit from the additional regularization terms.

In addition, the relative mean square errors versus the number of iterations, for the first and last cases, are presented in Fig. 6, where the final values of the errors are approximately 0.052 and 0.057, respectively.
Figure 6 indicates clearly that the proposed method is convergent, and the relative mean square errors are decreased with the increase of the number of iterations in two cases, and that the final error in the last case is slightly larger than that in the first case.

Fig. 6. In the iterative inversion methodology, relative mean square errors versus the number of iterations.

The second example is to reconstruct an inhomogeneous C-C slab with discontinuous (step-shaped) model parameter profiles, consisting of six layers. The width of the second and fifth layers is all 10 mm, and that of other layers is all 5 mm. The parameters ($\varepsilon_1$, $\sigma_3$, $\Delta\varepsilon$, and $\tau$) of the first and third layers are all (8.0, 0.3 S·m$^{-1}$, 25.0, and 6.5 ps), those of the second layer are (10.0, 0.9 S·m$^{-1}$, 30.0, and 6.0 ps), those of the fourth and sixth layers are all (4.0, 0.7 S·m$^{-1}$, 15.0, and 7.5 ps), and those of the fifth layer are (2.0, 0.9 S·m$^{-1}$, 10.0, and 8.0 ps).

After 30 iterations of the algorithm with regularization (regularization factors are the same as the first example) based on a noisy scenario (SNR is the same as the first example, too), the estimated optical relative permittivity, static conductivity, relative permittivity difference, and relaxation time are obtained as shown in subfigures (a)–(d) of Fig. 7. The error at the 30th iteration is approximately 0.063.

Fig. 7. The reconstructed distributions of: (a) optical relative permittivity, (b) static conductivity, (c) relative permittivity difference, and (d) relaxation time for a stratified Cole-Cole slab with discontinuous model parameter profiles, using noisy data (SNR = 20 dB) with regularization, at the 30th iteration.

The reconstructed distributions are presented in subfigures (a)–(d) of Fig. 8. The error at the 30th iteration is approximately 0.063.

Fig. 8. The reconstructed distributions of: (a) optical relative permittivity, (b) static conductivity, (c) relative permittivity difference, and (d) relaxation time for a stratified Cole-Cole slab with smooth model parameter profiles, using noisy data (SNR = 20 dB) with regularization, at the 30th iteration.

Figure 8 shows that the reconstructed C-C model parameters are also acceptable, based on the new initial guess. Thus, the proposed method is robust to initial guess.

The whole solution program codes written in MATLAB (R2011b, win64-bit) are iteratively executed
on a PC with a four-core i5-2320 CPU, each iteration taking, on average, about 2.87 s.

As previously mentioned, the nonlinearity and ill-posedness are two major difficulties in the solution of the inverse problem. Indeed, in order to bridge over the first difficulty, two similar multi-frequency time-harmonic imaging approaches, the frequency-hopping approach [18] and the simultaneous inversion one [19], have been proposed. While the time-domain technique presented in this paper is a natural extension from several frequencies to an entire frequency range, which could produce imaging results with higher resolution and accuracy. When this time-domain technique is, however, applied to large scale problems such as high-dimensional ones, their high computational cost will become a new difficulty, which may be overcome by either of the multi-frequency methods.

For the second difficulty, the Tikhonov regularization scheme used in this work is one of remedies, in which the reasonable regularization parameters (factors $\gamma_n$) for a particular problem can be determined by several regularization parameter-choice techniques such as the L-curve method [20]. Naturally, it will add additional computational cost to the problem. Besides, other regularization schemes, such as the total variation (TV) regularization [21], can also be adopted to remedy the ill-posedness of the inverse problem.

IV. CONCLUSION

This paper estimates four frequency-dependent parameters in the single pole Cole-Cole electrical dispersion equation via a time-domain optimization method. The first contribution in the developed inversion technique is direct reconstruction of four sorts of parameters for the C-C dispersive media from the time-domain measured data. The second one is that comparative studies on the same 1-D problem in three different cases are carried out. The numerical results demonstrate that the proposed technique is feasible for quantitative determination of the parameters of the 1-D example, and it provides a valuable tool for microwave imaging of biological tissues. The further work is to investigate multidimensional reconstruction problems as well as else regularization schemes.

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Novel Extraction Method of Inductance Parameter for Nonuniform Transmission Line in Anisotropic Dielectric

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Abstract — Since the parameters of transmission line can affect the signal integrity and electromagnetic compatibility directly in high frequency circuit, and there is lack of researches in the field of solving the inductance parameter of nonuniform transmission line in anisotropic dielectric, a novel method has been proposed in this paper to solve this problem. The new method uses filament division to establish the dispersion model of nonuniform transmission line, and formulates the filament division principle based on Biot-Savart Law and skin effect. Then it develops the Ampere loop integral dyadic equations and the closed circuit dyadic impedance matrix equation with direction factor in frequency domain based on electromagnetic quasi-static (EMQS). To obtain the corresponding magnetic field direction factor, the relative position of filaments in geometric space is analyzed. Finally, the inductance parameters are obtained by the impedance matrix equation. The correctness of proposed method is verified by applying to uniform transmission line model. Then the new method is applied to the calculation of two nonuniform transmission line models which filled in free space and anisotropic dielectric respectively. The inductance parameters and frequency dependency solved by different methods are compared, showing accuracy and validity of the proposed method. Besides, the new method can be applied to various transmission line structures and different anisotropic dielectric.

Index Terms — Anisotropic dielectric, inductance parameter, nonuniform transmission line, tensor dielectric constant.

I. INTRODUCTION

Nonuniform transmission line has been widely used in high speed circuit systems and affected the circuit performance and reliability [1-4]. So the extraction of distributed parameter for nonuniform transmission line is particularly important. Many electromagnetic numerical methods have been extensively used to solve this problem, such as finite-difference time-domain (FDTD) and moment of method (MOM) [5-9]. Afrooz and his fellows have used FDTD to analyze the electromagnetic field and extract the inductance parameter from the time-domain difference transmission line equations [5]. However, it cannot take the skin effect into consideration when current is in high frequency, so that the parameter value is inaccurate. Paul extracted the capacitance matrix by using MoM, and then the inductance matrix can be obtained from it [8]. Although this method can effectively solve the inductance matrix of transmission line, the analysis process is complex and needs to be solved many times. For this problem, the researchers of MIT have developed a FastHenry software to extract the parameters of integrated circuit based on the network analysis method. This software can solve the parameter fast, exactly, and universally. However, this software can be invalidated when the circuits are under the condition of electromagnetic quasi-static (EMQS) [10]. Besides, with the development of engineering technology, the performance of the circuit filled in general medium can no longer meet the demand of circuit design. So anisotropic dielectric has been more widely used because of the special electromagnetic characteristics [11-13]. For the research of anisotropic dielectric, many achievements focus on the influence of electromagnetic wave radiation, while few researches focus on inductance extraction of nonuniform transmission line in anisotropic dielectric [14-15].

In this paper, a novel extraction method of inductance parameters for nonuniform transmission line in anisotropic dielectric is proposed. It establishes the filament physical model according to Biot-Savart Law and skin effect, and derives the Ampere circuit dyadic integral equations and closed circuit dyadic impedance matrix equation with direction factor in frequency domain. Finally, the inductance parameter can be solved. The new method can be applied to various complex nonuniform transmission line structures and has some theoretical significance and engineering value.

This paper is organized as follows. In Section II, the filament dispersion of nonuniform transmission line is introduced and Ampere loop integral dyadic equations are summarized. The closed circuit dyadic impedance
matrix equation with direction factor is obtained in Section III. The proposed method is finally verified by numerical examples in Section IV, showing the correctness, accuracy and validity. The conclusions are given in Section V.

II. NONUNIFORM TRANSMISSION LINE MODELING

A. Filament division of nonuniform transmission line model

A physical division structure is established and shown in Fig. 1 to solve the inductance parameter of nonuniform transmission line. It consists of a lossy nonuniform signal line and a ground plate. The direction of signal line is Z. Its section radius is $r(z)$.

![Fig. 1. The nonuniform transmission line model.](image)

The structure in Fig. 1 can be discretized into some filaments with an approximate cross section. The number of filaments can be determined based on skin effect and the filament condition of Biot-Savart Law. So the side length of filament section $g$ should meet the condition:

$$g \leq \frac{1}{5} \delta,$$  

where skin depth $\delta$ can be described as $\delta = 1/\sqrt{\pi f \mu \sigma}$. $f$ is frequency, $\mu$ is permeability, $\sigma$ is conductivity. So filament number $N$ should meet the condition:

$$N \geq \frac{s(z)}{g},$$  

where $s(z)$ is the effective section which is described as:

$$s(z) = \pi \left[ r(z)^2 - (r(z) - \delta)^2 \right] = \pi \delta^2 + 2\pi r(z) \delta, \delta < r(z).$$  

When the frequency is enough high, $s(z)$ can be approximately described as:

$$s(z) = 2\pi r(z) \delta = 2r(z) \cdot \sqrt{\pi f \mu \sigma}, \delta \ll r(z).$$  

The final update equation can be written as:

$$N \geq 50 \pi r(z) / \sqrt{\pi f \mu \sigma}.$$  

Equation (5) is the condition of the filament division.

According to the condition of filament division, the model in Fig. 1 is discretized as Fig. 2. The filament numbers of signal line and ground plate are $N_C$ and $N_D$. The total filament number is $N_{tot}$. When the section of filament is small enough, it can be considered that the current here is evenly distributed. So the current of filament $n$ at $z$ point can be expressed as $i_n(z) = J_n(z) S_0$, where $J_n(z)$ is the current density of filament $n$ at $z$ point, $S_0$ is the area of filament section.

![Fig. 2. Filament division of nonuniform transmission line: (a) XOY plane and (b) XOZ plane.](image)

B. Filaments circuit modeling

Figure 3 is the instruction of filaments circuit $a \to b \to c \to d \to a$, in which the filaments $k$ and $s$ are chosen any from the filaments of signal line and ground plate. The length of filament is $\Delta z$. The circuit is in Electromagnetic quasi-static (EMQS).

![Fig. 3. The instruction of filaments circuit.](image)

According to Faraday electromagnetic law, the closed circuit integral equation in frequency domain can be written as:

$$\int_0^l E_k(x, y, z) dz + \int_0^l E_s(x, y, z + \Delta z) dx$$

$$\int_0^l E_s(x, y, z) dz + \int_0^l E_k(x, y, z + \Delta z) dx$$

$$= -j \omega \mu \int_0^\infty H_k(x, y, z) dx dz,$$  

The left part of (6) can be expressed as:

$$\int_0^l E_k(x, y, z) dz = i_k(z) R_k \Delta z,$$  

$$\int_0^l E_s(x, y, z + \Delta z) dz = i_s(z + \Delta z) R_s \Delta z,$$  

$$\int_0^l E(x, y, z) dz = i(z) - i_s(z),$$  

where $E(x, y, z)$ is spatial electric field strength; $E_k(x, y, z)$ and $E_s(x, y, z)$ are electric field strength of filaments $k$ and $s$ respectively; $v_k(z)$ and $v_s(z)$ are the voltage of filaments $k$ and $s$ at point $z$; $R_k$ and $R_s$ are the unit resistance of filaments $k$ and $s$.

The right part of (6) can be described as follows:
\[
\mu_s \int_{-\Delta z}^{\Delta z} H_n(x, y, z) \, dz = \mu_s \sum_{n=1}^{N} \int_{-\Delta z}^{\Delta z} H_n(x, y, z) \, dz, \quad (11)
\]
where \( H_n(x, y, z) \) is the magnetic field component of filament \( n \) which vertically through the area of \( a \rightarrow b \rightarrow c \rightarrow d \rightarrow a \).

So the magnetic field component of filament \( n \), is the unit matrix. So the right part of (19) can be further derived as:
\[
\int_{s} J_k \cdot ds + j \omega \int_{s} D_k \cdot ds = j \omega \int_{s} (\sigma E + \varepsilon) \cdot ds, \quad (19)
\]
where \( \sigma \) is the conductivity and \( \varepsilon \) is the dielectric constant tensor. And the right part of (19) can be further derived as:
\[
\int_{s} J_k \cdot ds + j \omega \int_{s} D_k \cdot ds = j \omega \int_{s} (\sigma E + \varepsilon) \cdot ds, \quad (20)
\]
in which \( \xi = \frac{\sigma}{\omega} + \varepsilon \). Then the Ampere loop integral dyadic equation in frequency domain can be written as:
\[
\int_{s} H_k \cdot dl = j \omega \int_{s} \xi E_k \cdot ds, \quad (21)
\]

Therefore, \( H_k \) can be solved by this equation. The magnetic field strengths \( H_k \) produced by the other filaments can also be obtained by this equation. To obtain \( H_{k_1} \), a new parameter has been defined here, that is the direction factor \( \beta \). It shows the relationship between effective magnetic \( H_{k_1} \) and total magnetic \( H_k \) through the particular rectangular loop. And this relationship cannot be expressed in simple mathematical expressions. The expression and usage of direction factor will be described in next section.

III. FORMULATION OF CLOSED CIRCUIT DYADIC IMPEDANCE MATRIX EQUATION

A. Expression of direction factor

Direction factor \( \beta \) can be solved according to the relative geometric position of filaments and rectangular loop. To solve the corresponding direction factor of \( H_{k+1} \), the rectangular loop of filament \( k \) and \( s \) is taken as the example.

The section center point coordinates of filament \( k, s \), and \( n \) are \((x_k, y_k), (x_s, y_s)\), and \((x_n, y_n)\). The right part of (12) can be represented as:
\[
\mu_s \sum_{n=1}^{N} \int_{-\Delta z}^{\Delta z} H_n \, dz =
\]
where \( \varepsilon \) is the dielectric constant tensor.

In this paper, the electric anisotropic dielectric is taken as the example, whose three principal axes coincide with the coordinate axes and the dielectric constant tensor is symmetric. So the dielectric constant tensor can be written as:
\[
\varepsilon = \begin{bmatrix}
\varepsilon_{11} & 0 & 0 \\
0 & \varepsilon_{22} & 0 \\
0 & 0 & \varepsilon_{33}
\end{bmatrix}, \quad (17)
\]

By applying the new constitutive relations to (13), the following expression can be obtained as:
\[
\int_{s} J_k \cdot ds + j \omega \int_{s} D_k \cdot ds = \int_{s} \sigma E_k \cdot ds + j \omega \int_{s} (\varepsilon \cdot E_k) \cdot ds, \quad (18)
\]
which leads to:
\[
\int_{s} J_k \cdot ds + j \omega \int_{s} D_k \cdot ds = \int_{s} \sigma E_k \cdot ds + j \omega \int_{s} (\varepsilon \cdot E_k) \cdot ds, \quad (19)
\]
where \( A \) is the unit matrix.
\[
\int_{-\Delta}^{\Delta} H_z \, dx + \frac{j \omega \mu}{8\pi} i_n \Delta x + \frac{j \omega \mu}{2\pi} i_n \Delta x \ln \sqrt{(x_n-x_d)^2+(y_n-y_d)^2} - g.
\]

The third part of (22) is the magnetic flux induced by the current of filaments except \( k \) and \( s \), and can be written as:
\[
\sum_{n \neq k, s} \int_{-\Delta}^{\Delta} H_n \, dx \Delta x = \sum_{n \neq k, s} \int_{-\Delta}^{\Delta} H_n \cdot \Delta x \, dzdx
\]
\[
= \sum_{n \neq k, s} \int_{-\Delta}^{\Delta} H_n \cdot \Delta x \, dzdx
\]
\[
= \sum_{n \neq k, s} \int_{0}^{\Delta} H_n \cdot \Delta x \, dzdx
\]
\[
= \sum_{n \neq k, s} \int_{0}^{\Delta} H_n \cdot \Delta x \, dzdx
\]
\[
\alpha \text{ is the angle between magnetic flux and rectangular loop of filaments } k \text{ and } s. \text{ Based on above process, the closed circuits which constituted by all signal line filaments with the first filament (namely filament } k \text{ of signal line are selected too.} \]

So the closed circuit dyadic equations with direction factor can be concluded as follows:
\[
\Delta z = -\lambda'(i_n-i_{N+n}) + \frac{\omega \mu}{
\sum_{n=0}^{N_s} \int_{0}^{\Delta} H_n \cdot \Delta x \, dzdx
\]
\[
= -\lambda'(i_n-i_{N+n}) + \frac{\omega \mu}{
\sum_{n=0}^{N_s} \int_{0}^{\Delta} H_n \cdot \Delta x \, dzdx
\]

Therefore, the corresponding direction factor \( \beta \) of \( H_z \) has been simplified as a relationship between the filament section center point coordinates and angle \( \alpha \). These variables can be obtained directly. So the corresponding direction factor can be represented as a relationship:
\[
\beta = \frac{\sum_{n=0}^{N_s} \int_{0}^{\Delta} H_n \cdot \Delta x \, dzdx}{\sum_{n=0}^{N_s} \int_{0}^{\Delta} H_n \cdot \Delta x \, dzdx}
\]

The direction factor of other filaments can also be obtained based on above process.

B. Closed circuit dyadic equations with direction factor

The total number of filament circuits is \( C_{N_s}^2 \). They are similar to the filaments circuit of \( k \) and \( s \). Taking the convenience and realization for calculation into account, the closed circuits which constituted by all signal line filaments with the first filament (namely \( Nc+1 \) of ground plate are selected. Moreover, the closed circuits constituted by all ground plate filaments with the longest one (namely filament \( k \) of signal line are selected too. Therefore, the corresponding direction factor can be concluded as follows:
\[
\Delta z = -\lambda'(i_n-i_{N+n}) + \frac{\omega \mu}{
\sum_{n=0}^{N_s} \int_{0}^{\Delta} H_n \cdot \Delta x \, dzdx
\]
\[
= -\lambda'(i_n-i_{N+n}) + \frac{\omega \mu}{
\sum_{n=0}^{N_s} \int_{0}^{\Delta} H_n \cdot \Delta x \, dzdx
\]

There is a duplicate closed circuit dyadic equation in above equations. So we should remove it and add the
current conservation equation which can be written as:

\[ \sum_{n=1}^{N_{\text{tot}}} i_n = 0. \] (30)

Therefore, there are \( N_{\text{tot}} \times N_{\text{tot}} \) coefficient matrix which can be obtained by the closed circuit equations and written as:

\[ \mathbf{S}(m,n) = \begin{cases} \frac{\mu \pi}{4} \ln \left( \frac{(\alpha \cos \theta_m' - \nu_x')^2 + (\alpha \sin \theta_m')^2}{(\alpha \cos \theta_n' + \nu_x')^2 + (\alpha \sin \theta_n')^2} \right), & 1 \leq m \leq N_{\text{tot}}, 1 \leq n \leq N_{\text{tot}}, m = n, \\ \frac{\mu \pi}{4} \ln \left( \frac{(\alpha \cos \theta_{m+1} - \nu_x')^2 + (\alpha \sin \theta_{m+1})^2}{(\alpha \cos \theta_{n+1} + \nu_x')^2 + (\alpha \sin \theta_{n+1})^2} \right), & 1 \leq m \leq N_{\text{tot}}, 1 \leq n \leq N_{\text{tot}}, m = n+1, \\ \frac{\mu \pi}{4} \ln \left( \frac{(\alpha \cos \theta_{m-1} - \nu_x')^2 + (\alpha \sin \theta_{m-1})^2}{(\alpha \cos \theta_{n-1} + \nu_x')^2 + (\alpha \sin \theta_{n-1})^2} \right), & 1 \leq m \leq N_{\text{tot}}, 1 \leq n \leq N_{\text{tot}}, m = n-1, \\ 0, & \text{otherwise}. \end{cases} \]

Another relationship can be concluded as:

\[ \mathbf{I}(z) = \mathbf{Q} \mathbf{M} \] (32)

where \( \mathbf{Q}(1,m) = \begin{cases} 1, & 1 \leq m \leq N_{\text{tot}}, \\ 0, & \text{otherwise}. \end{cases} \)

By applying the matrix transformation, the updated relationship can be written as:

\[ \mathbf{D} = -(\mathbf{Q} \mathbf{S}^{-1} \mathbf{F})^{-1} \mathbf{I}(z) \] (33)

This equation is the closed circuit impedance dyadic matrix equation with direction factor. Thus, the impedance matrix can be expressed as:

\[ \mathbf{Z} = (\mathbf{Q} \mathbf{S}^{-1} \mathbf{F})^{-1} \] (34)

According to the transmission line impedance equation \( \mathbf{Z} = \mathbf{R} + j \omega \mathbf{L} \), the resistive parameter can be obtained form the real part of Equation (34), and the inductance matrix can also be concluded from the imaginary part as:

\[ \mathbf{L}(z) = \frac{\text{Im}[Z]}{2\pi f} = \frac{\text{Im}[\mathbf{Q} \mathbf{S}^{-1} \mathbf{F}]^{-1}}{2\pi f} \] (35)

IV. NUMERICAL RESULTS

A. Uniform transmission line model in free space

In this section, the uniform transmission line model shown in Fig. 4 is considered to verify the validity and correctness of the new method. The two kind of different radius of signal line we used here are \( r_1 = 0.5 \text{ mm} \) and \( r_2 = 0.4 \text{ mm} \). The size of cross section of ground plate is 3 mm×1 mm. The nearest distance between signal line and ground plate is 1 mm. The conductivity of transmission line is \( \sigma = 5.98 \times 10^7 \text{ S/m} \). The magnetic permeability is \( \mu = \mu_r \). New method and traditional method are used to solve the inductance parameter of this model.

![Fig. 4. The uniform transmission line model.](image)

To verify the correctness of proposed method, the per unit length inductance of uniform transmission line has been obtained by three different methods: proposed method, traditional method and measurement. In traditional method, the skin effect of transmission line in high frequency has been neglected, which can decrease the area of effective cross section and affect the value of inductance parameter [16]. While the new method can take it into consideration. Besides, the measurement has also been used to prove the validity of proposed method. The schematic of measurement is shown in Fig. 5. It uses the vector network analyzer to measure the impedance of equipment under test (EUT), namely, the transmission line, and the inductance parameter can be obtained from it.

![Fig. 5. Measurement setup schematic.](image)

Table 1 shows the filament numbers and computing time of new method to calculate the inductance parameter in various frequency.

Figure 6 shows the inductance distribution of uniform transmission line in free space and 100 MHz frequency. As shown in the figure, we can conclude that the per unit length inductance does not change with the coordinate \( z \). Moreover, the inductance values of the line...
with different radius are different, and they increase with the decrease of radius when the frequency of current is constant. Compare the traditional method and the proposed method, the changing trend of the new method is more close to the measurement one. So the correctness of proposed method has been verified, and it is more accurate than traditional one.

The frequency dependency of inductance parameter for uniform transmission line is shown in Fig. 7, which indicates the inductance calculated by new method and the measurement are vary with frequency, while the traditional method does not. Because traditional method cannot consider the skin effect in high frequency. Besides, comparing the results with measurement, the error between new method and measurement is less than 5%, namely 15nH. So the validity and correctness of new method can be verified, and it has a high precision.

<table>
<thead>
<tr>
<th>f/MHz</th>
<th>N_C</th>
<th>N_D</th>
<th>N_tot</th>
<th>t/s</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>381</td>
<td>871</td>
<td>1252</td>
<td>0.52</td>
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<tr>
<td>100</td>
<td>1206</td>
<td>2972</td>
<td>4178</td>
<td>2.6</td>
</tr>
<tr>
<td>1000</td>
<td>3815</td>
<td>9615</td>
<td>13430</td>
<td>30.45</td>
</tr>
</tbody>
</table>

In order to further illustrate the influence that the skin effect bring to the calculation of inductance parameter in high frequency, Fig. 8 shows the frequency dependency for unit inductance parameters expressed by the ratio of radius to skin depth. When the radius of conductor is less than twice the skin depth, the unit inductance parameter of new method is approximately equal to the value of traditional method (341nH/m). The reason is that the current can be considered as uniform distributed in low frequency. However, the radius of conductor is twice larger than skin depth, the unit inductance parameter is gradually decreased with the increased frequency. So the skin effect in high frequency cannot be ignored.

Figure 9 shows the current distribution within the cross section of the uniform transmission line at different frequency. It shows the variation of current density along the radial direction at 1 MHz, 10 MHz and 100 MHz frequency respectively. Compare the curves, we can further validate the effect of skin effect and get the conclusion; as the frequency increases, the skin depth of the wire decreases, and the smaller the effective area of the current along the wire. Thus, the greater the resistance loss of the wire.
B. Nonuniform transmission line model in free space

For better investigation of accuracy and availability of proposed method, the nonuniform transmission line model introduced in Fig. 1 is used in this section. The medium is free space. The two kind of different radius of signal line we used here are \( r_3=0.5-0.1(z/l) \) mm and \( r_4=0.5-0.05(z/l) \). The size of ground plate and distance between signal line and ground plate are the same to Fig. 4. The length of signal line is 3000 mm, namely that coordinate \( z \) is from 0 to 3000 mm. New method and traditional method are used to solve the inductance parameter of this model.

Table 2 shows the filament numbers and computing time of the new method to calculate the inductance parameter in various frequency.

Table 2: Filament numbers and computing time in various frequency

<table>
<thead>
<tr>
<th>( f/\text{MHz} )</th>
<th>( N_C )</th>
<th>( N_D )</th>
<th>( N_{\text{tot}} )</th>
<th>( t/s )</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>419</td>
<td>871</td>
<td>1290</td>
<td>0.6</td>
</tr>
<tr>
<td>100</td>
<td>1327</td>
<td>2972</td>
<td>4299</td>
<td>2.71</td>
</tr>
<tr>
<td>1000</td>
<td>4196</td>
<td>9615</td>
<td>13811</td>
<td>31.72</td>
</tr>
</tbody>
</table>

Figure 10 shows the inductance distribution of nonuniform transmission line in free space and 100 MHz frequency, which indicates that the unit inductance parameter is gradually increased with the increased coordinate \( z \). So we can conclude that the unit inductance parameter of nonuniform transmission line in free space is increased with the decreased radius when the frequency of current is constant. Moreover, the traditional method has been used to prove the validity of the proposed method [17]. In the traditional method, the nonuniform transmission lines are considered to be equivalent to a cascaded chain of many multiport subnetworks which are made of short sections of uniform lines. Compare the two methods, the changing trend of the new method is more pronounced than the traditional one.

![Inductance distribution of nonuniform transmission line in free space.](image)

For analysis of frequency dependency of unit inductance parameter of nonuniform transmission line in free space, the unit line in \( z=150 \) mm is calculated. The result is shown in Fig. 11, which indicates the unit inductance parameter is decreased with the increased frequency. It is caused by skin effect, which makes the current distribute near the surface of line so that the effective section can be decreased. Besides, when the frequency is 0.1 GHz, the inductance value in Fig. 10 is 344\( \text{nH/m} \), which also is the value corresponding to \( z=150 \) mm in Fig. 10.

![Frequency dependency of inductance parameter for nonuniform transmission line in free space.](image)

C. Nonuniform transmission line model in anisotropic dielectric

Because the traditional method cannot solve the inductance parameter of nonuniform transmission line in anisotropic dielectric, in this section, the new method is applied to calculating the model of Fig. 1. The anisotropic dielectric we choose here is the uniaxial anisotropic medium, which is widely used in the microwave field of aviation industry. In this paper, we take the two kind of anisotropic dielectric as the example to analyze the influence of anisotropic dielectric on the inductance parameters. The tensor dielectric constant of anisotropic dielectric 1 is \( \varepsilon_{11}=1.44\varepsilon_0, \varepsilon_{22}=1.12\varepsilon_0, \varepsilon_{33}=1.44\varepsilon_0 \), and the tensor dielectric constant of anisotropic dielectric 2 is \( \varepsilon_{11}=2.88\varepsilon_0, \varepsilon_{22}=2.24\varepsilon_0, \varepsilon_{33}=2.88\varepsilon_0 \).

Table 3 shows the filament numbers and computing time of the new method to calculate inductance parameter in various frequency. Comparing the data in Table 3 with Table 2, we can conclude that the computing time of the model in anisotropic dielectric is longer than in free space. That is caused by the tensor dielectric constant with three-degree matrix, which leads to a more complex matrix processing process and increased computing time.

Table 3: Filament numbers and computing time in various frequency

<table>
<thead>
<tr>
<th>( f/\text{GHz} )</th>
<th>( N_C )</th>
<th>( N_D )</th>
<th>( N_{\text{tot}} )</th>
<th>( t/s )</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>419</td>
<td>871</td>
<td>1290</td>
<td>0.9</td>
</tr>
<tr>
<td>100</td>
<td>1327</td>
<td>2972</td>
<td>4299</td>
<td>3.12</td>
</tr>
<tr>
<td>1000</td>
<td>4196</td>
<td>9615</td>
<td>13811</td>
<td>39.72</td>
</tr>
</tbody>
</table>
Figure 12 is the inductance distribution of nonuniform transmission line in different medium and 100 MHz frequency. The figure shows the inductance parameter increases with the decrease of transmission line’s radius. Compared with Fig. 10, the value in Fig. 12 is bigger than in Fig. 10, which is caused by the principal axis of tensor dielectric constant. Besides, the isotropic dielectric of $\varepsilon=1.44\varepsilon_0$ is compared with the anisotropic medium. It shows the inductance parameter is reduced in anisotropic dielectric when other conditions are the same. Because both the real part and the imaginary part of the magnetic field intensity are reduced in anisotropic dielectric. And it can decrease with the increase of coefficient of tensor dielectric constant.

For better analysis of new method, the frequency dependency of unit inductance parameter for nonuniform transmission line model in anisotropic dielectric is solved. The process of simulation is the same to Fig. 11 and shown in Fig. 13. It indicates that the inductance parameter is decreased with frequency. And when frequency is more than 1 GHz, the unit inductance parameter is decreased in exponential form. Therefore, anisotropic dielectric has a great influence on inductance parameter, and it should not be ignored in solving electric parameter of transmission line.

V. CONCLUSION

A novel method has been proposed for extracting inductance parameter of nonuniform transmission line in anisotropic dielectric. The proposed method can take the nonuniform distributed resistance and current caused by skin effect in high frequency and complex form of tensor dielectric constant into consideration. The correctness, validation, and accuracy of proposed method are demonstrated by several examples. The results show that the new method can be applied to solving inductance parameter when the model medium is anisotropic dielectric and transmission line is nonuniform. Moreover, it can be applied to solving various nonuniform transmission line structures and different anisotropic dielectric conditions.

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REFERENCES


The Investigation of Substrate’s Dielectric Properties for Improving the Performance of Witricity Devices

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Abstract — In designing a better Witricy device, there are several parameters that contribute to the improvement of efficiency. In this article, the substrate characteristics, which gaining less attention despite their potential for the improvement of Witricity performance are thoroughly studied. The investigation has proven that RO 3010 substrate composed of ceramic-filled Polytetrafluoroethylene (PTFE) composites is the best material for the optimal Witricity performance, independent of the spiral coil’s number of turns. This is due to its high-energy storage capacity obtained from the real permittivity, and roughly low loss factor and tangent loss. Hence, the Rogers RO 3010 substrate is proposed in this study as it performs reliable 50% to 74% coupling efficiency with the varied number of spiral coil turns.

Index Terms — Inductive power transfer, strongly coupled magnetic resonance, substrate, wireless power transfer, Witricity.

I. INTRODUCTION

The first experiment on wireless electrical transmission has been conducted by Nikola Tesla since 1890’s [1]. However, the work on this wireless power transfer (WPT) was not taken up by scientific community except for some significant experiments [2], such studying a variation of electric potential and its casual fluctuation on a transformer [3]. Then, a more significant and modern experiment has been initiated by a group of researchers in Massachusetts Institute of Technology (MIT), by introducing the name of ‘Witricity’ as a method of WPT that focuses on non-radiative mid-range power transmission. Witricity, which based on reliable and strongly coupled magnetic resonance technique is efficiently lighting up 60 watts light bulbs using 50 cm diameter coils over 2 meter distance in 2007 [4], has gained interests from worldwide researchers. In addition, Intel has also proven the method by an experiment at 60 cm distance with 75% efficiency [5]. Besides Witricity, there are several other methods of wireless power transfer (WPT) including energy harvesting, inductive coupling and capacitive coupling.

A few parameters such as impedance matching [6], coupling [7] and Q-factors [8] are reported to improve WPT efficiency. Study of the substrate thickness, the dimension of the capacitors and the number of turns of the coils is demonstrated in [9] to align the design with a given resonance frequency. However, this work is merely focused on the changing of the substrate thickness of the device concerning only Flame Retarded 4 (FR-4). In addition to thickness, permittivity is one of the important substrate characteristics to be considered in determining the best material that could contribute to the performance improvement of Witricity devices. Therefore, this characteristic needs to be carefully studied and thoroughly discussed. Referring to [10], varying the substrate dielectric property is expected useful in characterizing the resonance frequency of the Witricity device; whereby the lower values of permittivity correspond to higher resonance frequency and vice versa. Furthermore, a study in [11] proves that the increases of the material permittivity result in the increases of the antenna gain for a given resonance frequency. As the gain of antenna related to its efficiency, thus, it is interesting to apply this concept to the Witricity design by studying the effect of the parameter towards its performance, especially in coupling efficiency.

Furthermore, capacitance, \( C \) is one of the factors in designing Witricity device as it provides electrical energy storage [9]. The electrostatic energy stored in a parallel plate capacitor measured in the unit of Joules as given by \( W = \frac{1}{2}CV^2 \); where \( V \) is the voltage difference between two parallel plates. However, the value
of capacitance strictly depends on the substrate permittivity, $\varepsilon$, the thickness of substrate, $d$ and the area of parallel plates, $A$ as $C = \varepsilon A/d$. Therefore, a significant increase in energy density can be made by either increasing the permittivity, $\varepsilon$ of the substrate or the applied field strength, $E$ [12].

In this article, the substrate’s dielectric properties are investigated for improving Witricity device performance. A few types of substrates with different permittivity, including Flame Retardant 4 (FR-4), RO4003C, TMM-4 and RO3010 have been measured and compared to CST simulated data. Then, a similar Witricity device design is applied on each substrate to study the permittivity effect towards Witricity performance. The best material is chosen, and the proposed prototype is verified practically.

II. WITRICITY DESIGN AND THEORETICAL CONCEPT

The proposed Witricity device consists of a transmitter and a receiver, which resonates at similar frequencies. Figure 1 depicts a transmission scheme from the first port to the second port. While, Fig. 2 shows the CST generated layout of the proposed Witricity device and the arrangement in the three-dimensional (3D) simulation tool of CST Microwave Design Studio.

In Figs. 1 and 2, each transmitter and receiver consist of two conducting layers: top and bottom are separated by the air gap. The top layer consists of a rectangular spiral coil inductor (Tx and Rx coil), while the bottom layer has two slotted capacitor plates that are arranged and attached to a single turn coil (Tx and Rx loop). To achieve a simple design workflow, an identical design is implemented in both transmitter and receiver to ensure both devices are always resonating at the same frequency.

The device is designed accordingly to meet the best coupling efficiency, $\eta$ and impedance matching. Each transmitter and receiver design consists of a substrate with a thickness of 0.635 mm and copper layers on top and bottom layer. On the top layer, a spiral coil of conductive copper, which consists of several numbers of loops that is varied from 10 to 30 turns. The limit of the number of turns is fixed to 30 due to a further increase of turns will lead to a more complicated design and may compromise the precision of the design in fabrication stage. According to the Biot-Savart law in [14], the amount of the induced magnetic field at receiver, $H_{\text{avg}}$ is proportional to the spiral coil’s number of turns, $n$ as (1):

$$H_{\text{avg}} = \frac{I \cdot n}{4\pi} \int \frac{dl \times r}{r^3},$$

where, $I$, $n$ and $r$ are the respective input current, number of turns and distance between the transmitter coil to the receiver. Whilst, $dl$ is the tangential vector around a single loop coil. Accordingly, the spiral coil’s number of turns, $n$ is directly influencing the inductance, $L$ value as shown by the modified Wheeler formula in (2) [18]:

$$L = \frac{K_1 L_{\text{avg}}}{K_1 + K_2 \rho},$$

where, $K_1$ and $K_2$ are the spiral shape dependent coefficients, which equal to 2.34 and 2.75 respectively. Meanwhile, $D_{\text{avg}}$ is the average diameter of the rectangular spiral; and $\rho$ is the fill ratio, which defined to 1 for the design. Thus, by varying the spiral coil’s number of turns, $n$ will proportionally affect the inductance, $L$, which then alter the induced magnetic field, $H_{\text{Rx}}$ analogously at the receiver. Consequently, the unloaded quality factor, $Q$ of the spiral coil that analogous to $\omega L/R$ will change accordingly.

The overall coupling efficiency of the Witricity device, $\eta$ can be written as the following Equation (3) [15-16]:

$$\eta = \frac{k^2 Q_1 Q_2}{1+(1+k^2 Q_1 Q_2)^{1/2}},$$

where, $Q_1$ and $Q_2$ are unloaded quality factors of the transmitter and receiver coils, respectively, which are equal to $\omega L/R$. While, $k$ is the mutual coupling constant, which has a value ranging from 0 to 1, that closely depending on the distance between transmitter and receiver. Therefore, it is proven in the Equations (1), (2) and (3) that by increasing the spiral coil’s number of turns upsurge in the induced magnetic field at the receiver, $H_{\text{Rx}}$, the inductance value of $L$ as well as the overall efficiency of the Witricity device.

As presented in Fig. 2 (b), the bottom layer of the designed Witricity device consists of a single source/load loop is linked to the two 14 x 8 mm² slotted rectangular capacitors, which stores electrical charges supplied to the device. The advantages of slotted capacitors over traditional capacitors are the improvement in reflection coefficient and bandwidth [13]. The used substrates in the proposed Witricity are changed to observe the effect of different substrates of FR-4, RO4003C, TMM4, RO3006 and RO3010 that having the permittivity, including Flame Retardant 4 (FR-4) to study the permittivity effect towards Witricity performance. The best material is chosen, and the proposed prototype is verified practically.

Fig. 1. Witricity device transmission scheme.
III. RESULTS AND DISCUSSION

The simulation and experimental results, and discussion are divided into two parts; A and B. Section A discusses the respective results obtained related to complex permittivity. Meanwhile, Section B presents the effect of permittivity towards coupling efficiency and the verification of Witricity design with the best substrate.

A. Complex permittivity

The dielectric property is derived from the effective complex permittivity, $\varepsilon^*$ of the substrate, which determines its electromagnetic (EM) ability such as the polarization, dielectric losses and conductivity. Compared to $\varepsilon^*$, its complex relative permittivity, $\varepsilon_r^*$ as expressed in (4) is used more often as the value is dimensionless and simpler [16]:

$$
\varepsilon_r^* = \frac{\varepsilon^*}{\varepsilon_0} = \frac{\varepsilon - j\varepsilon'}{\varepsilon_0} = \varepsilon_r - j\varepsilon_r',
$$

(4)

where, $\varepsilon_0$, $\varepsilon_r'$ and $\varepsilon_r''$ are the permittivity of free space ($8.85 \times 10^{-12}$ F/m), the real and imaginary part of the complex relative permittivity, accordingly. The real part of $\varepsilon^*$, which is $\varepsilon'$ that denotes the ability of a material to store the incident EM energy through the wave propagation. Whilst, the imaginary part of $\varepsilon^*$ noted by $\varepsilon''$ represents the degree of EM energy losses in the material. Thus, the respective $\varepsilon_r'$ and $\varepsilon_r''$ are also known as the dielectric constant and loss factor. The real and imaginary relative permittivity values of four different types of dielectric materials; RO 4003, FR-4, TMM-4 and RO 3010 are depicted in Table 1.

As shown in Table 1, the measured data of real relative permittivity between the dielectric materials have no significant differences with either simulated data obtained from CST and data sheet. Thus, it can be drawn that the Rogers RO4003 has the lowest $\varepsilon_r'$ comparative to FR-4, TMM-4 and RO 3010. The FR-4 $\varepsilon_r'$ is slightly higher than RO 4003 but almost similar to TMM-4 followed by RO 3010 that has the highest $\varepsilon_r'$ with more than two-time values of the others. Considering from this aspect only, thus, the lowest energy transfer efficiency is expected from RO 4003 due to the less EM energy storage ability that related to lowering real permittivity and followed by FR-4, TMM-4 and RO 3010.

 Nonetheless, there is another factor that contributes to the efficient energy transfer, which is substrate’s loss tangent, $\tan \delta$ can be expressed as (5) [17]:

$$
\tan \delta = \frac{\omega \varepsilon_r'' + \sigma}{\omega \varepsilon_r'},
$$

(5)

where, $\omega$ and $\sigma$ are angular frequency and conductivity loss, respectively in conditions of $\varepsilon_r'' \geq 0$ and $\varepsilon_r' \gg \varepsilon_r''$. At high frequency as considered in this proposed work, the substrate’s loss tangent, $\tan \delta$ can be simplified to $\varepsilon_r'' / \varepsilon_r'$. It is also known as the dissipation factor that describes the angle difference between capacitance current and voltage. As noted from Table 1, the highest value of the loss tangent belongs to FR-4, followed by RO 3010, RO 4003, and the lowest belongs to TMM-4. Thus, concludes the FR-4 and TMM-4 have the respective highest and lowest loss.

By having the information of the loss tangent, the imaginary relative permittivity, $\varepsilon_r''$ in Table 1 is obtained by multiplying the real relative permittivity, $\varepsilon_r'$ and the loss tangent. The imaginary relative permittivity, $\varepsilon_r''$ presents the loss factor that portraying the efficiency of energy transfer. Therefore, higher loss factor (imaginary
relative permittivity, \( \varepsilon''_r \)) leads to the least efficient energy transfer. The results show a significant difference between FR-4 and other substrates. It can be deduced that FR-4 have the largest loss factor with almost three-time values of RO 3010 and more than six-time of the other substrates. However, RO 4003 that has the lowest \( \varepsilon''_r \) will have the smallest loss factor that expected to contribute for better energy transfer.

By considering both real and imaginary relative permittivity, it can be deduced that a substrate must have small loss factor (imaginary relative permittivity) and large real relative permittivity to store more energy from incident EM wave. As a result from both real and imaginary relative permittivity, the smaller value of loss tangent is important in determining the best material for Witricity device.

### Table 1: The substrate properties obtained from the data sheet, CST and measured relative permittivity

<table>
<thead>
<tr>
<th>Substrate</th>
<th>Material Composition</th>
<th>Real Relative Permittivity ((\varepsilon'_r))</th>
<th>Loss Tangent</th>
<th>Real Relative Permittivity ((\varepsilon'_r))</th>
<th>Real Relative Permittivity ((\varepsilon'_r))</th>
<th>Imaginary Relative Permittivity ((\varepsilon''_r))</th>
</tr>
</thead>
<tbody>
<tr>
<td>FR-4</td>
<td>Epoxy resin</td>
<td>4.4-4.7</td>
<td>0.014-0.017</td>
<td>4.41</td>
<td>4.30</td>
<td>0.06-0.07</td>
</tr>
<tr>
<td>RO4003C</td>
<td>Glass reinforced ceramics</td>
<td>3.55</td>
<td>0.0021</td>
<td>3.56</td>
<td>3.55</td>
<td>0.0075</td>
</tr>
<tr>
<td>TMM-4</td>
<td>Ceramic thermoset</td>
<td>4.70</td>
<td>0.002</td>
<td>4.51</td>
<td>4.50</td>
<td>0.0090</td>
</tr>
<tr>
<td>RO3010</td>
<td>Ceramic-filled PTFE</td>
<td>11.20</td>
<td>0.0022</td>
<td>10.22</td>
<td>10.20</td>
<td>0.0224</td>
</tr>
</tbody>
</table>

### B. Coupling efficiency

The concerned coupling efficiency of the Witricity device, \( \eta \) expressed in (3) is analogous to \( |S_{21}|^2 \). The comparison of the proposed Witricity device’s coupling efficiency performance that designed using different dielectric materials, including FR-4, RO4003, TMM 4, and RO 3010 are obtained via CST Microwave Studio simulation. It is to study the relationship between the complex permittivity and loss tangent toward coupling efficiency performance. The effect of varying the spiral coil’s number of turns in the Witricity design for the different dielectric materials is shown in Fig. 3, while the corresponding coupling efficiency of their optimal design is shown in Fig. 6.

![Fig. 3. Coupling efficiency of Witricity device with different substrates and varied number of spiral coil turns between 10 and 30.](image)

Based on Fig. 3, at the low number of turns, there are significant results shown between each material with RO 3010 has the best coupling with approximately 50% followed by TMM 4, RO 4003 and FR-4. The result complies with the sequence of \( \varepsilon'_r \) from the highest to the lowest as shown in Table 1, except for FR-4, which has greater \( \varepsilon'_r \) compared to RO 4003 but has lower coupling efficiency performance. This result deduces that the real part of complex relative permittivity is important in achieving high capacitance value of the Witricity device, which enabling high-energy storage at the transmitter and receiver. Likewise, the imaginary part of the complex relative permittivity is also an important factor as it represents the energy loss in the material. The lower value reflects a low-energy loss due to absorption of the material. Therefore, the performance of FR-4 is the worst among all the substrates as it has low real relative permittivity, but highest imaginary, which results in lower coupling efficiency. At the highest number of turns, most of the substrates show a significant drawback, especially by RO 3010 yet better than FR-4, which has the largest imaginary relative permittivity and tangent loss. However, RO 4003 performs almost similar result with 25 turns even at higher turns as it has the lowest loss factor. Both phenomena prove a stronger dependency of imaginary permittivity compared to the real permittivity for the number of turns higher the optimal 25. This is, on the contrary, for a number of turns that less than optimal 25, which shows stronger dependency on the real permittivity compared to the imaginary.

Referring to the obtained results, Witricity device with RO 3010 substrate and optimal 25 number of turns is fabricated. The fabricated prototype is shown in Fig. 4. The 25 number of turns is chosen as an optimum as most of the substrates show best coupling at this number.
The measurement setup used to validate the performance of this proposed Witricity device is shown in Fig. 5. The results of the coupling efficiency of their optimal design are shown in Fig. 6.

Fig. 4. Prototype of Witricity device with optimal 25 number of spiral coil turns using RO3010 substrate.

Fig. 5. Measurement setup using Keysight Vector Network Analyzer (VNA).

Fig. 6. Coupling efficiency results Witricity device using different materials having optimal 25 number of spiral coil turns.

At the optimal 25 number of turns, the coupling efficiency results in Fig. 6 show the lead taking by the design using RO 3010 with comparable simulated and measured performance of 72.3% and 76.2%, respectively at approximately 24 MHz. While, the design using FR-4 has performed worse coupling efficiency with 53.4% at a higher frequency of 31.5 MHz. However, other materials perform at the almost similar level between 70.5% to 71.0% due to the nearly close loss tangent about 0.002-0.0022, which is about eight times lower than FR-4 of 0.014-0.017.

By considering different substrates of various real relative permittivities, the distinct values of capacitances are expected in each design as the number of spiral coil turns are kept at a constant of 25 turns. This has led to different operating frequency for each design, where the lowest frequency obtained by the highest real relative permittivity substrate. This contrasts to the design with the lowest real relative permittivity material that has the highest operating frequency. Consequently, the operating frequency of the designed Witricity device is inversely proportional to capacitance and real relative permittivity of the chosen substrate.

IV. CONCLUSION

The performance of the Witricity device can be improved by selecting an appropriate dielectric material or known as a substrate in the design process. The dielectric properties of substrate involve in designing Witricity device is shown by investigating the effect of complex permittivity to the device performance. The study shows that the high real relative permittivity, which also branded as dielectric constant results in great coupling performance, especially for the spiral coil’s number of turns from 10 to 25. RO 3010 has the widest range of the tunable number of coil turns as it has been greater than 50% efficiency for 10-30 turns, followed by TMM-4 and RO 4003 that achieve more than 50% efficiency at 15-30 turns. Meanwhile, FR-4 needs at least 25 turns to perform well. The study also has shown a great performance of Witricity device with a high real relative permittivity substrate from a low number of coil turns up to the optimal of 25. Afterward, the performance has strongly affected by the value of imaginary permittivity as been noted by the design using RO 3010 substrate compared to others at 30 number turns.

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Assessment of Kapton-based Flexible Antenna for Near Field Wireless Energy Transfer

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Abstract — This letter presents the design of a flexible highly efficient antenna for Wireless Energy Transfer (WET) at 13.56 MHz. The proposed antenna uses very thin kapton, with a thickness of 25 μm as a substrate, and an 18 μm layer of copper as the conductive material. The 40 mm x 40 mm 6 loop antenna produces almost 90% ETE (energy transfer efficiency) and a bandwidth (BW) of almost 4 MHz for inductive wireless communications. This flexible antenna is suitable for use in small mobile devices, for wireless charging and communication purposes at the NFC operating frequency. In addition, kapton offers very high durability, high mechanical strength, and unique distortional resistance to harsh environments and corrosive aqueous etchants, in this way increasing the reliability of the antenna.

Index Terms — Flexible antenna, high efficiency, kapton, Near Field Communication (NFC), Wireless Energy Transfer (WET).

I. INTRODUCTION

Near Field Communication (NFC) enables data transfer between devices. Since it is facilitated through inductive coupling, NFC can also be used to enable the transfer of energy between these devices. Due to NFC’s unique ability, many high- and mid-end smartphones come with embedded NFC features. However, with the current technology, NFC antennas embedded in smartphones are only used for data transfer, rather than wireless charging.

Various substrate materials have been investigated for use in energy transfer applications. Some studies have achieved insensitivity to distance and strong magnetic coupling using low-cost glass reinforced epoxy laminated boards (FR 4) [1-3]. A Nickel-Zinc-based ferrite substrate has also been used to implement near-field antennas with high efficiency at 13.56 MHz [8]. However, the growing demand for flexible electronic devices necessitates further research into the implementation of antennas on flexible substrates. Some of the more popular flexible substrates found in literature include kapton polyimide film, polydimethylsiloxane (PDMS) and polyethylene (PET). Yu has proposed a multi-layer spiral antenna for wireless power transfer at 300 kHz using copper coils separated by kapton films [4]. The author manages to transfer 5 Watts of power over a distance of two times the coil diameter. Choo has designed a flexible antenna for near-field communication at the UHF frequency of 912 MHz [5]. The author used printed copper strip line on flexible polyethylene (PET) to couple a reader and a microchip, solely for wireless communication [5]. However, except for a few examples of the application of flexible PDMS substrates in telemetry systems [6], not much research has been carried out on flexible antenna substrates for wireless energy transfer.

To the best of our knowledge, there are no papers on the study and design of flexible antennas for simultaneous wireless communication and energy transfer at 13.56 MHz. Therefore, this research proposes a design of a flexible antenna for wireless energy transfer, which supports wireless data transfer as well. A frequency of 13.56 MHz is chosen to fit the standard operation frequency of NFC. Kapton is assessed as the substrate because of its...
flexibility, the possibility to use very thin layers (in contrast to PDMS), the rather low cost (in comparison with graphene), and the very high durability and mechanical strength.

II. ANTENNA GEOMETRY

In order to fit into a smartphone, the antenna is sized at 40 mm x 40 mm. The antenna topology is shown in Fig. 1 and its dimensions are given in Table 1. For a perfect circular loop, the best operation distance with the strongest magnetic field flux is \( r = d\sqrt{2} \) [7], where \( d \) is the operating distance and \( r \) is the antenna’s radius. Assuming that changing the shape to a square will not change this characteristic drastically, the operating distance for the wireless energy transfer link is set at 14.14 mm.

![Antenna topology](image)

(a) Front view and (b) back view, connected by vias.

**Fig. 1.** Antenna topology: (a) front view and (b) back view, connected by vias.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Outer loop length, ( l_{\text{out}} )</td>
<td>41 mm</td>
</tr>
<tr>
<td>Inner loop length, ( l_{\text{in}} )</td>
<td>4 mm</td>
</tr>
<tr>
<td>Strip width, ( w_e )</td>
<td>1 mm</td>
</tr>
<tr>
<td>Gap width, ( w_g )</td>
<td>2 mm</td>
</tr>
</tbody>
</table>

The transfer efficiency of a pair of antennas in an energy transfer link is calculated by [8]:

\[
\eta = \frac{k^2 Q_1 Q_2}{1 + \sqrt{1 + k^2 Q_1 Q_2}}. \tag{1}
\]

where \( Q_1 \) and \( Q_2 \) are the quality factors of the transmitting and receiving antenna respectively:

\[
Q_1 = \frac{\omega L_1}{R_1} \tag{2}
\]

\[
Q_2 = \frac{\omega L_2}{R_2} \tag{3}
\]

\( \omega = 2\pi f \), \( k \) is the coupling coefficient between both antennas and can be determined using:

\[
k = \frac{M}{\sqrt{L_1 L_2}}. \tag{5}
\]

Since the kapton layer is extremely thin, the inductance of each antenna can be computed as [9]:

\[
L_{1,2} = 0.635\mu_l a_{\text{avg}} \left[ \ln\left( \frac{2.07}{l_p} \right) + 0.18l_p + 0.13 l_p^2 \right], \tag{6}
\]

where \( \mu \) is the permeability of the background medium and,

\[
l_p = \frac{l_{\text{out}} - l_{\text{in}}}{l_{\text{out}} + l_{\text{in}}}, \tag{7}
\]

\[
l_{\text{avg}} = \frac{l_{\text{out}} + l_{\text{in}}}{2}. \tag{8}
\]

The mutual inductance between both antennas, \( M \) can be obtained using [10]:

\[
M = \left( \frac{4}{\pi} \right)^2 2 \sum_{i=1}^{N} M_i \quad \text{and}
\]

\[
M_i = \frac{\mu_o \pi a_i^4}{2(2a_i^4 + d_i^2)^{3/2}} \left( 1 + \frac{15}{32} \gamma^2 + \frac{315}{1024} \gamma^4 \right). \tag{9}
\]

\[
\gamma = \frac{2a_i^2}{2a_i^2 + d_i^2}, \tag{10}
\]

where \( N \) is the number of turns and \( a_i = l_{\text{out}} - (N - 1)(w_e + w_g) - \frac{w_e}{2} \). The skin depth, \( \delta \) and the resistance of each antenna are determined by using:

\[
R_{\text{DC}} = \frac{\rho l}{A}, \quad \delta = \frac{\sqrt{\rho}}{\sqrt{\pi f} \mu_o}, \tag{11}
\]

\[
R = \frac{R_{\text{DC}}}{4\delta} \left( \frac{t_e}{1 - e^{-\frac{t_e}{\delta}}} \right), \tag{12}
\]

where \( \rho \) is the resistivity of copper (1.7 \times 10^{-8} \text{ Wm}) , \( A \) is the cross-sectional area of the strip, and \( t_e \) is the thickness of the copper conductor.

With reference to Fig. 1, \( l \) and \( A \) can be defined as:

\[
l = 6(w_e + w_g) + l_{\text{back}} + l_{\text{out}} + \sum_{i=1}^{N-1} \left( l_{\text{out}} - \left( i - 1 \right) w_w - i w_e \right) \tag{13}
\]

\[
A = w_e \cdot t_e. \tag{14}
\]

The bandwidth of the antenna is defined as the frequency interval in between the two -3 dB points with respect to the value at the resonant frequency.

III. RESULTS AND DISCUSSION

Using described model in previous section, transfer efficiency of the antennas is calculated using Matlab. Based on the mathematical model, transfer efficiency obtained is 81.28\%. However, this computation does not take the dielectric effects into consideration. Hence, full-wave simulations are employed to examine the transfer efficiencies obtained using different dielectric substrates.

There are various kapton substrates in the market, as given in Table 2. Since the kapton itself is extremely thin, it will have a negligible effect on the energy transfer
link. The copper thickness does have an effect on the efficiency of this transfer link, but it will be shown that a thickness of 18 μm already yields efficiencies near 90%. The energy transfer system uses identical antennas for transmitter and receiver at an operating distance of 14.14 mm, as shown in Fig. 2.

<table>
<thead>
<tr>
<th>Substrate</th>
<th>Dielectric Constant (µ)</th>
<th>Loss Tangent</th>
<th>Substrate Thickness</th>
<th>Copper Thickness</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kapton</td>
<td>3.6</td>
<td>0.031</td>
<td>12.5 μm</td>
<td>18 μm</td>
</tr>
<tr>
<td>Kapton</td>
<td>3.5</td>
<td>0.030</td>
<td>25 μm</td>
<td>18 μm</td>
</tr>
<tr>
<td>Kapton</td>
<td>3.5</td>
<td>0.030</td>
<td>25 μm</td>
<td>35 μm</td>
</tr>
<tr>
<td>Kapton</td>
<td>3.5</td>
<td>0.030</td>
<td>75 μm</td>
<td>35 μm</td>
</tr>
</tbody>
</table>

The antenna was fabricated and measured, see Fig. 5. S-parameters were recorded and analyzed, and both antennas were impedance matched using lumped elements. The capacitor values available in the market nearest to the optimal values were selected, see Table 3.

It is easily shown that the efficiency of the energy transfer link \( \frac{P_{\text{received}}}{P_{\text{transmitted}}} \) is given by \( |S_2|\). This parameter is shown in Fig. 6.

<table>
<thead>
<tr>
<th>Capacitor Values</th>
<th>C1 (pF)</th>
<th>C2 (pF)</th>
<th>C3 (pF)</th>
<th>C4 (pF)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Simulation</td>
<td>100</td>
<td>60</td>
<td>62</td>
<td>100</td>
</tr>
<tr>
<td>Actual</td>
<td>98.61</td>
<td>58.89</td>
<td>61.23</td>
<td>95.71</td>
</tr>
</tbody>
</table>

![Fig. 2. Energy transfer topology.](image)

Both antennas have been matched using the lumped element technique, see Fig. 3. Based on a compromise between efficiency, flexibility, and mechanical strength, the kapton is chosen 25 μm thick and the copper is chosen 18 μm thick. The resulting efficiency is given in Fig. 4. All simulations were done with CST Microwave Studio.

![Fig. 3. Wireless link with matching networks for both antennas.](image)

![Fig. 4. Efficiency of the antenna using 25 μm kapton and 18 μm copper thickness.](image)

![Fig. 5. Fabricated antenna and measurement setup.](image)

![Fig. 6. Realized transfer efficiency.](image)

At a distance of 14.14 mm, the energy transfer
efficiency achieved is as high as 86.61% and 83.82% in simulations and measurements, respectively. The difference of 2.79% with the simulated value is caused by the tolerances on the etching process, and slightly deviating distance from the simulated distance in real life.

Based on this result, it can be clearly concluded that kapton is a suitable material to be used for wireless energy transfer. Kapton can offer transfer efficiencies as high as rigid materials like FR4, with the huge advantage of adding flexibility.

Figure 7 shows that the optimal frequency of the transfer system decreases slightly when the operating distance is increased. This happens because changing the distance will alter the mutual inductance between transmitter and receiver antenna. Hence, both antennas will not be perfectly matched anymore. Therefore, at the NFC frequency, the efficiency of the wireless energy transfer is significantly changed, see Fig. 8.

When the distance between both antennas is smaller than the optimum distance, a multi-resonance appears, as shown in Fig. 7. Multi-resonance condition will result two maximum transfer efficiencies at two different frequencies. This phenomenon is caused by an over-coupling condition, which occurs when the transmitter is too close to the receiver and creates frequency splitting phenomenon. As a result, the transfer efficiency at operating frequency will reduce significantly. The discrepancy in the trend of the change of transfer efficiency with distance between antennas for measurement and simulation is recorded. The different is contributed by the non-exist exact capacitor value for matching circuit in market. The 5% capacitors tolerance also causes the difference between measurement result and simulation result.

Since we are considering a flexible substrate, bending may be an issue, since it may occur, accidentally or on purpose, in practical situations. The bending situation studied is given in Fig. 9. One of the two antennas is bent with a radius of 20 mm. Results for bending are given in Fig. 10. It is shown that bending the antenna will slightly reduce its efficiency. However, the drop of 4.5% in efficiency (from 83.6%) is acceptable.

Fig. 7. Transfer efficiency as a function of frequency, simulation (Sim) and measurement (Mea) for several distances, \(d\).

Fig. 8. Change in measurement of transfer efficiency with varying distance between antennas.

Fig. 9. Bending situation with bending radius \(r = 20\) mm.

Fig. 10. Measurement for effect of bending on transfer efficiency.
Figure 11 shows that the antenna has a large bandwidth of 3.86 MHz around the operating frequency of 13.56 MHz at matching distance, 14.14 mm. This is sufficient for inductive signal transmission. This proves that antennas using kapton substrates are suitable for wireless communications as well.

![Measured Bandwidth of the Antenna](image)

**Fig. 11. Measured bandwidth of the antenna.**

**IV. CONCLUSION**

It is shown that kapton is suitable to be used as an antenna substrate for WET purposes. Results show that this flexible material can produce high performance in terms of ETE and bandwidths, comparable to rigid substrates such as FR4. In addition, kapton is flexible, and that can increase the robustness of the antenna by enabling it to fit with any device shape.

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Determination of Reverse-Current Coil Turns Layout to Mitigate Over-Coupling in Resonant Inductive Power Transfer Links

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Abstract — The transfer efficiency of two-coil resonant inductive power transfer links is known to significantly degrade with a reduction of the coil distance, due to an over-coupling at shorter distances. In this work, a simple technique is introduced to determine the spatial layout of reverse-current coil turns, which suppresses the over-coupling-induced transfer efficiency drop. By employing the spatial layout of reverse-current turns as a design parameter, the proposed method provides more generality in its implementation compared to other reverse-current turn methods. Simulation and experimental results validate the method, suggesting a potential for distance-insensitive implementations.

Index Terms — Inductive power transfer, mutual inductance, over-coupling.

I. INTRODUCTION
Two-coil resonant inductive power transfer links have been widely studied in recent times as wireless power transfer implementations [1]. These links typically operate within the low- and high-frequency spectral ranges, with 13.56 MHz being one of the more popular frequencies. Energy is transferred from transmitting to receiving terminals through inductive coupling. Consequently, tuned coil structures are used at the transmitter and receiver terminals to facilitate wireless power transfer. Typical applications of inductive power transfer include wireless chargers for portable household devices, power delivery to biomedical implants, in addition to numerous industrial applications [2].

Inductive coupling-based wireless power transfer links are sensitive to variations in coil positioning [3, 4]. Specifically, bringing a pair of coupled resonant coil terminals closer is known to lead to over-coupling, which is characterized by a drop in the transfer efficiency at the original link frequency, and the appearance of split resonance frequencies [4-7].

High transfer efficiency levels in the over-coupled regime may be maintained through an arrangement to track the new split-resonance frequencies [5, 6], which unfortunately increases link complexity. Alternatively, coil terminals themselves could be designed to mitigate over-coupling. Over-coupling can be controlled by introducing reverse-current turns in the coil structures, thereby providing a reverse mutual inductance to limit the increase in mutual inductance associated with the over-coupled regime [8, 9]. In [8], the required reverse mutual inductance is generated through an appropriate ratio of forward- and reverse-current turns. Nonetheless, this approach requires a rational turns-ratio in order to be physically implementable. Alternatively, the approach in [9] employs one each of forward- and reverse-current turns in a transmit coil, with a lumped capacitance controlling the ratio of currents through these turns. However, the practical performance of the realized energy transfer link using this technique may be constrained by the availability of commercial off-the-shelf (COTS) capacitors with the level of precision determined by the design process. The limitations of these reverse-current turn methods can be surmounted by a more general approach, which uses the spatial layout of reverse-current turns as the over-coupling mitigating parameter.

Consequently, this paper proposes a simple method
for determining a spatial layout of reverse-current turns to be included in a transmit coil to mitigate overcoupling. The rest of the paper is organized as follows. Section II describes the design method, while results obtained from applying the proposed method to a test scenario are discussed in Section III. The paper is concluded in Section IV.

II. DESIGN METHOD

A key aspect of the proposed method to mitigate over-coupling is the determination of mutual inductances between coupled coils. The mutual inductance between a pair of multi-turn circular transmit and receive coils separated by a distance \( z \) can be calculated using [10]:

\[
M = \sum_{i=1}^{n_a} \sum_{j=1}^{n_a} \frac{\mu_0 \pi a_i^2 b_j^2}{2 \left( a_i^2 + b_j^2 + z^2 \right)^{3/2}} \left( 1 + \frac{15}{32} \gamma^2 + \frac{315}{1024} \gamma^4 \right),
\]

(1)

\[
\gamma_{ij} = \frac{2a_i b_j}{a_i^2 + b_j^2 + z^2},
\]

(2)

where \( a_i \) and \( b_j \) are the radii of the \( i \)-th and \( j \)-th turns of the \( n_a \)-turn transmit and \( n_a \)-turn receive coils, respectively. Equations (1) and (2) can be rewritten by replacing the \( n_a \) and \( n_a \) turn-radii in the transmit and receive coils by average radii, such that,

\[
\sum_{i=1}^{n_a} a_i = n_a a^{(a)},
\]

(3)

\[
\sum_{j=1}^{n_a} b_j = n_a b^{(a)},
\]

(4)

where the superscript \((a)\) denotes an average. Consequently, Equation (1) and Equation (2) become:

\[
M = \frac{n_a n_a \mu_0 \pi a^{(a)} b^{(a)} z^2}{2 \left( a^{(a)} + b^{(a)} + z^2 \right)^{3/2}} \left( 1 + \frac{15}{32} \gamma^2 + \frac{315}{1024} \gamma^4 \right),
\]

(5)

\[
\gamma = \frac{2a^{(a)} b^{(a)}}{a^{(a)} + b^{(a)} + z^2}.
\]

(6)

The transfer efficiency of the inductive link realized by coupling the transmit and receive coils can be characterized using the s-parameter transmission coefficient as [4, 11]:

\[
\eta(\% ) = 100 \times \frac{|s|}{|s|}. 
\]

(7)

For a given configuration of the receive coil, the first step in the proposed design method is to determine an appropriate transmit coil to realize an adequate transfer efficiency at the operating distance from the transmit coil \( z_1 \). Bi-conjugate matching of the coupled coils at this distance imposes a critical coupling condition on the link [3, 5]. The next step is to assume an envisaged shortest separation distance between the pair of coupled coils when put into operation, and designate this as \( z_2 \). Over-coupling between a pair of coils increases the mutual inductance. Consequently, the mitigation of over-coupling requires the introduction of a reverse mutual inductance to counteract the increase in mutual inductance for shorter separation distances [8, 9].

With the incorporation of reverse-current turns, the mutual inductance at the critical coupling distance \( z_1 \) is a superposition of forward \( (M_f) \) and reverse \( (M_r) \) mutual inductances, namely,

\[
M_1 = M_f - M_r.
\]

(8)

\[
M_f \text{ and } M_r \text{ can be calculated with Equations (5) and (6), using the appropriate average radii in the expressions, namely } a^{(a)} \text{ for the forward turns and } a^{(r)} \text{ for the reverse turns. Similarly, at the envisaged shortest distance } z_1 \text{ and a chosen intermediate distance } z_2, \text{ the mutual inductances are:}
\]

\[
M_3 = M_f - M_r,
\]

(9)

\[
M_2 = M_f - M_r.
\]

(10)

To mitigate over-coupling, the average radius of reverse-current turns \( a^{(r)} \) is determined, such that the function,

\[
f \left( a^{(r)} \right) = (M_2 - M_1) - (M_3 - M_2) = 0,
\]

(11)

while using the same number of reverse-current turns as there are forward-current turns in the transmit coil. The value of \( a^{(r)} \) which satisfies Equation (11) is determined by substituting Equations (5)-(6) and (8)-(10) in Equation (11).

A good choice of intermediate distance \( z_2 \) provides a value of \( a^{(r)} \) small enough such that the inner diameter of the receive coil just overlaps the inner diameter of the reverse-current turns of the transmit coil. This ensures that the receive coil is always under the influence of a superposition of mutual inductances from the forward- and reverse-current turns throughout the envisaged range of operating distances.

Although the widths and spacings of the reverse-current turns are not used in the approximate expressions given above, they have an impact on the coil quality factor, and thus on the transfer efficiency. A significant spacing between the additional reverse-current turns and the existing forward-current turns conceptually leads to a distributed turns coil, which may lead to a lower coil quality factor [12, 13]. Hence, it may be necessary in a second stage to adjust the spacing and width of the reverse-current turns in a full-wave electromagnetic (EM) solver in order to maintain high transfer efficiency levels. Furthermore, less variation in the transfer efficiency over the range of operating distances can be realized by slightly detuning the link at the critical coupling distance, such that the impedance match
conditions are realized at a slightly shorter distance than the critical coupling distance.

III. RESULTS AND DISCUSSION

To test the proposed design method, an initial configuration of a square transmit printed spiral coil (PSC) was modelled in CST Microwave Studio to provide a transfer efficiency above 80% at 13.56 MHz, when coupled to a square receive PSC at an axial distance of 35 mm. The PSCs were designed on low-cost FR4 substrate boards, with a dielectric constant of 4.7, and copper conductor thickness of 0.035 mm. The design parameters are described in Table 1. Note that both coils are square, which makes this a more stringent test for the technique proposed.

Figure 1 shows the full-wave EM simulation results. As the paired coils were brought closer together, the 13.56 MHz transfer efficiency of 82.63% at a 35 mm separation dropped to 25.32% at 1 mm, due to the over-coupling. The resulting percentage variation \( \left( \eta_{\text{max}} - \eta_{\text{min}} \right) / \eta_{\text{max}} \) is 69.36%. Also, splitting of the resonance frequency is observed in the transfer efficiency profiles at distances less than 35 mm, with an increase in the gap between resonance frequencies as the coils are brought closer together.

To mitigate over-coupling the square coils were conceptually substituted with theoretically equivalent circular coils with the same enclosed area, with \( b^{(a)} \) and \( a^{(a)} \) being the average radii of the equivalent circular receive and transmit coils, respectively. An appropriate value of the average radius of reverse-current turns \( a^{(a)} \) was then determined using Equations (5)-(6), and (8)-(11).

Table 1: Coil parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Transmit PSC equivalent average radius</td>
<td>36.95 mm</td>
</tr>
<tr>
<td>Receive PSC equivalent average radius</td>
<td>19.30 mm</td>
</tr>
<tr>
<td>Width of transmit PSC forward-current turns</td>
<td>4 mm</td>
</tr>
<tr>
<td>Width of receive PSC turns ( w_{\text{rn}} )</td>
<td>0.9 mm</td>
</tr>
<tr>
<td>Transmit PSC forward-current turn-spacing ( s_{f} )</td>
<td>0.5 mm</td>
</tr>
<tr>
<td>Receive PSC turn-spacing ( s_{r} )</td>
<td>0.5 mm</td>
</tr>
<tr>
<td>Number of forward-current turns in transmit PSC ( n_{a} )</td>
<td>2</td>
</tr>
<tr>
<td>Number of turns in receive PSC ( n_{b} )</td>
<td>10</td>
</tr>
<tr>
<td>Operating distance ( z_{i} )</td>
<td>35 mm</td>
</tr>
<tr>
<td>Closest distance ( z_{i} )</td>
<td>1 mm</td>
</tr>
</tbody>
</table>

Figure 2 is a study of Equation (11), showing the variation of the function \( f \left( a^{(a)} \right) \) with the average reverse-current turn radius \( a^{(a)} \), at various values of intermediate distance \( z_{2} \). It is observed that with \( z_{2} = 2 \) mm, Equation (11) is satisfied with an average reverse-current radius of \( a^{(a)} = 12.46 \) mm. This is small enough to ensure that, using the same spacing as the forward-current turns, the inner diameter of the reverse-current turns is slightly overlapped by the inner side-length of the receive coil.

For demonstration purposes, \( d^{(a)} \) was directly used to model circular reverse-current turns in the transmit coil in CST Microwave Studio for full-wave EM simulations. In order to maintain high-transfer efficiency at the critical coupling distance of 35 mm, the width and spacing of the reverse-current turns were then adjusted to achieve a convenient threshold transfer efficiency of 77%, without altering the calculated average radius. The final designed transmit coil, hence consisted of square forward-current turns and circular reverse-current turns, as illustrated in Fig. 3.
Fig. 3. Physical models of the: (a) transmit and (b) receive coils. The dotted lines show the connection between coil turns behind the substrate board.

Figure 4 shows results of a full-wave EM simulation of the designed transmit coil coupled to the receive coil in CST Microwave Studio. The link resonance condition was realized by bi-conjugate matching the coupled coils using capacitive L-match circuits, as illustrated in Fig. 5. The capacitance values are listed in Table 2. As compared to Fig. 1, the results in Fig. 4 show a marked improvement. Although some frequency splitting can still be observed at distances between 5 mm and 30 mm, the depth of the trough is significantly less than in Fig. 1. The best 13.56 MHz transfer efficiency value of 78.35% occurs at an axial distance of 30 mm, while the lowest value of 52.73% occurs at a distance of 10 mm, implying an improved percentage variation in transfer efficiency of 32.70%. The mitigation of over-coupling has, however, been achieved with a trade-off in the transfer efficiency at the original critical coupling distance of 35 mm. The initial 13.56 MHz transfer efficiency of 82.63% has dropped to 77.29%.

The over-coupling mitigation obtained in Fig. 4 was further improved by slightly detuning the link at the critical coupling distance of 35 mm. As shown in Fig. 6, this adjustment further reduces percentage variation in link transfer efficiency to 20.67%.

To experimentally validate the over-coupling mitigation arising from the inclusion of the analytically determined reverse-current turns in the transmit PSC, s-parameters were measured at different separation distances of the fabricated PSCs using a vector network analyzer, as shown in Fig. 7. The measured s-parameters were used to determine the link transfer efficiency using Equation (7). Due to measurement constraints the shortest measured distance was 5 mm.

Fig. 4. Link transfer efficiency profile using modified transmit coil.

Fig. 5. Schematic representation of impedance match arrangement.

Table 2: Impedance matching capacitance values

<table>
<thead>
<tr>
<th>Capacitance</th>
<th>Value (pF)</th>
</tr>
</thead>
<tbody>
<tr>
<td>C1</td>
<td>57</td>
</tr>
<tr>
<td>C2</td>
<td>167</td>
</tr>
<tr>
<td>C3</td>
<td>22</td>
</tr>
<tr>
<td>C4</td>
<td>2</td>
</tr>
</tbody>
</table>

Fig. 6. Link transfer efficiency with adjustment of the critical coupling distance.

Fig. 7. Measurement set-up.
In Fig. 8, the measured 13.56 MHz transfer efficiency values are compared with the simulated results shown in Fig. 1 and Fig. 6. Trends in measured transfer efficiency using forward and reverse-current turns are in good agreement with the predicted over-coupling mitigation demonstrated by the simulation results. However, the measured transfer efficiency values at each distance were lower than the simulated values, mainly due to losses arising from fabrication inaccuracies.

IV. CONCLUSION

This paper has discussed a method to suppress the over-coupling that occurs as the distance between coupled coils in a resonant inductive power transfer link reduces. The simulation and experimental results clearly show that the incorporation of reverse-current turns mitigates over-coupling effects in a resonant inductive power transfer link. The central issue addressed in this paper is the determination of the appropriate coil-turn configuration to provide adequate suppression of over-coupling. By employing the spatial layout of turns as the design parameter, the method proposed in this paper provides more generality than other contemporary reverse-current turn methods, which are either dependent on rational turns-ratios or realizable capacitive current-control.

ACKNOWLEDGMENT

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REFERENCES

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A Data Collection Method Based on the Region Division in Opportunistic Networks

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Abstract — The popularity of wearable devices and smart phones provide a great convenience for large-scale data collection. Owing to the non-uniform distribution of mobile sensors, the data quantity collected from different regions has a wide variation. So we design the region division algorithm that divides area into different density grades and sets appropriate sampling frequency on different regions. Furthermore, we propose Circle of Time Slice (CoTS) and Cardinal Number Timing Method (CNTM) to solve the sampling error when nodes move from one area to another. On this basis, we propose the Data Collection Algorithm Based on the Sampling Frequency (DC-BSF) to reduce the data redundancy. Simulations demonstrate that the method proposed in this paper can reduce data redundancy under the condition of achieving high coverage.

Index Terms — Data collection, region division, sampling frequency, time slice cycle.

I. INTRODUCTION

With the rapid development of mobile communication and sensing technology, a number of innovative applications and services have emerged. In particular, the popularity of portable devices (e.g., smart phones, wearable devices, etc.) and vehicle sensors (e.g., GPS), provide efficient ways to sense physical objects and environmental conditions on a large scale. It greatly expanded the dimensions of human perception and changed the way people perceive the world [1].

Mobile Crowd Sensing (MCS), where individuals with sensing and computing devices collectively share data and extract information to measure phenomena of common interest [2]. Sensor nodes collect data adaptively in the mobile process. It forms a Mobile Opportunistic Networks (MONs) when data is transferred between sensor nodes [3]. The data transmission depends on the cooperation of nodes to fulfill a “store – carry – process – forward” mode.

Sensors are embedded in a taxi and collect data periodically. Since different taxis always have heterogeneous mobility regions with some randomness, they could make different contributions to the coverage. The mobile trajectory is more intensive in hot regions, like shopping malls, stations and so on. So there are a large number of sensors in these regions. If they collect data at the same sampling frequency as sensors in sparse region, it may lead to serious data redundancy. On the contrary, the mobile trajectory is relatively sparse in remote areas. The data coverage is low in the sparse area. Sensors in these regions need to be set a higher sampling frequency. So we divide the region according to the density of taxi trajectory. Then we set the sampling frequency of sensors in regions of different density. At last, we propose an effective sensing mechanism that can reduce data redundancy in the premise of high coverage. The main contributions of this paper are shown as follows.

1) We design the Region Division algorithm (D-RG) to divide the entire area into regions of different grades, according to density of nodes' trajectory.
2) We propose the Circle of Time Slice and Cardinal Number Timing Method to solve the sampling error resulted from nodes moving from one region to another.
3) We propose the Data Collection Algorithm Based on the Sampling Frequency that can reduce data redundancy in the premise of high coverage.

The remainder of this paper is organized as follows. Section 2 reviews the related work. Section 3 describes the system model and two algorithms. In Section 4, we evaluate the performance of our model by real mobile traces. Finally, we conclude the paper in Section 5.

II. RELATED WORK

Recently the concept of mobile crowd sensing has
attracted the attention of many researchers. Challenges in this research include localized analytics, resource limitation, privacy, security, data integrity, architecture and so on [1]. The 4W1H characterize the major research issues in the MCS life cycle [4]. The noise-mapping system can intuitively present the urban noise level by encoding levels with colors [5]. COUPON is a cooperative framework for building sensing maps in mobile opportunistic network [6]. The CarTel is a distributed mobile sensor computing system [7].

As more and more sensors are integrated on mobile devices, the application field of mobile crowd sensing is constantly expanding [8]. In the paper [9], smart parking was used as a case study to investigate features of crowdsourcing that may apply to other mobile applications. Participatory sensing can be applied in environmental monitoring [10]. The Intelligent Traffic System (ITS) is based on mobile crowd sensing [11]. Smart P2P model can optimize the search process [12].

Due to the different scenarios and purposes, the type of data needed is different. So many scholars have studied the methods of data collection. ITAMP is a new sparsely adaptive algorithm with high recovery rate and fast reconstructing speed [13]. In paper [14], the data collection method of wireless sensor networks in gateway was proposed. Another data acquisition method was proposed in paper [15], heterogeneous multi-source multi-mode sensory based on data quality.

The data sensing mechanism is the key to obtaining valid data in the process of data collection. Researchers have proposed some sensing mechanisms. Researchers designed two cooperative schemes to optimize the system performances in terms of sensing quality, delivery delay and energy consumption [16]. Researchers proposed a city hot spot event sensing method based on mobile crowd sensing. This method can discover and classify hot spots [2]. Previous studies have considered the characteristics of nodes mobility and the spatiotemporal correlation among sensory data. But they ignored the moving speed of sensors, residence time in each area and the sampling error resulted from nodes moving from one region to another. In view of the above problems, we propose a new data collection algorithm. It can reduce data redundancy under the condition of achieving high coverage.

**III. PERCEPTION PROCESS**

In this part, we divide the entire sensing area into different grades according to the data of pre-sampling firstly. Furthermore, we propose the Circle of Time Slice and Cardinal Number Timing Method to solve the sampling error resulting from nodes moving from one region to another. Finally, we propose the Data Collection Algorithm Based on the Sampling Frequency (DC-BSF).

### A. Division of sensing area

Although the movement trajectory possesses some randomness, it has characteristics of dense or sparse. The data of taxi movement trajectory is provided by Korea Advanced Institute of Science and Technology (KAIST) [17]. The graph of movement trajectory is shown in Fig. 1.

![Fig. 1. The graph of taxi movement trajectory.](image)

In order to further analyze the characteristics of the trajectory of sensors, we divide the entire sensing area into the same size grid cells \( G = \{ g_1, g_2, \ldots, g_n \} \), and sensors \( s_1, s_2, \ldots, s_n \) are embedded in mobile vehicles [7], as illustrated in Fig. 2.

![Fig. 2. The sensing area with same size grid cell.](image)

The cell-grid \( g_i \) shown in Fig. 2 is the smallest unit of region division. In order to divide the sensing area according to the density of the vehicle trajectory, we need to calculate the density of trajectory firstly. The statistical method is shown in Algorithm 1. It counts the number of trajectories in each grid cell according to the data of pre-sampling.

Statistical results are stored in a table like Table 1. The \( a_i \) in the \( i \)-th row represents the number of trajectory in a grid cell. The \( u_i \) in \( i \)-th row represents the total number of grids that include \( a_i \) trajectories.
Algorithm 1: Statistical method of sampling times

**Input:**
vecData; // Pre sampled data
tabsize; // Grid size
Xnum; // the number of grid on the X axis
Ynum; // the number of grid on the Y axis

**Output:**
vecTabData; // Sampling times
mapSumData; //the number of grid sampled n times

**Initialize** vecTabData is NULL;
for i ← 0 to vecData.size do
    index_x ← floor(vecData[i].x / tabsize) + 1;
    index_y ← floor(vecData[i].y / tabsize) + 1;
    // floor() is a Integral Formula.
    vecTabData[index_x][index_y] ← vecTabData[index_x][index_y] + 1;
repeat
for i ← 0 to vecTabData.size do
    for j ← 0 to vecTabData[i].size do
        if (mapSumData.find(vecTabData[i][j]))
            mapSumData(vecTabData[i][j]) ← mapSumData(vecTabData[i][j]) + 1;
        else
            mapSumData(vecTabData[i][j]) ← 1;
        endif
    end for
end for

<table>
<thead>
<tr>
<th>Number of tracks ((a_i))</th>
<th>Number of grids ((u_i))</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a_0) = 0</td>
<td>(u_0)</td>
</tr>
<tr>
<td>(a_1) = 1</td>
<td>(u_1)</td>
</tr>
<tr>
<td>(\vdots)</td>
<td>(\vdots)</td>
</tr>
<tr>
<td>(a_n) = n</td>
<td>(u_n)</td>
</tr>
</tbody>
</table>

We set a information table stored at each node and the table is dynamic. The information table includes the current time, data (collected and transmitted), sampling frequency \((f(l_k))\) and current location, as illustrated in Table 2. Current location is stored in a two-dimensional array. \(tab[i][j]\) represents the location of a cell-grid is the i-th row and j-th column of the area. \(level_k\) represents that the grade of the grid is \(k\). The formula \(level_k = f(l_k)\) in Table 1 means that the sampling frequency of sensors located in \(level_k\) is \(f(l_k)\).

<table>
<thead>
<tr>
<th>Current Location</th>
<th>Frequency</th>
<th>Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>(tab[i][j] = level_k)</td>
<td>(level_k = f(l_k))</td>
<td>Collect</td>
</tr>
</tbody>
</table>

The traditional K-means algorithm [18] is a typical distance-based clustering algorithm. Distance between the surrounding sensors and the center sensor was used as the evaluation index of similarity. Therefore, we propose a method based on the number of trajectory in each cell-grid to divide sensing area. We divide the entire area into three levels according to the data of Table 1. The steps are shown bellow, and the algorithm is shown in Algorithm 2:

\[
sum = \frac{1}{3} \sum_{i=0}^{n} (a_i \times u_i),
\]

where \(sum\) represents one-third of the total number of trajectory in all grids. There is a constant \(p\) that satisfies the Equation (2):

\[
\begin{align*}
& a_0 + a_1 + \cdots + a_p \leq sum \\
& a_0 + a_1 + \cdots + a_p + a_{p+1} > sum, \quad p \in [0,n).
\end{align*}
\]

We divide the grids that satisfy the above conditions into the region of low sampling frequency \((level_1)\). As shown in Fig. 3, the different textures represent different region grades. Similarly, there is a constant \(q\) that satisfies the Equation (3):

\[
\begin{align*}
& a_{p+1} + a_{p+2} + \cdots + a_q \leq sum \\
& a_{p+1} + a_{p+2} + \cdots + a_q > sum, \quad q \in [p+1,n).
\end{align*}
\]

We divide the grids satisfying the above conditions into the region of intermediate sampling frequency \((level_2)\), as shown in Fig. 3. The rest of the grids are divided into the region of high sampling frequency \((level_3)\).

**Algorithm 2: D-RG algorithm**

**Input:** \(a_i, u_i\)

**Output:** \(a_p, a_q\)

**Initialize** \(s ← 0\);
for \(i ← 0\) to \(n\) do
    \(s ← s + a_i \times u_i;\)
    //Determine the boundary value of the level region.
    if \((s >= sum)\) then
        Get a boundary value: \(a_i;\)
        \(s ← 0;\) // get the next boundary value.
    end if
end repeat

Fig. 3. The graph of region grades represented by different textures.
B. The algorithm of data collection

The sensor performs the sampling task, when the sampling time is reached and the sensor does not contain the data of the current grid. Due to the limited transmission range of sensors, the transmission delay is relatively serious. So we set different sampling frequency for sensors in different regions. Sensors can collect data according to their own sampling frequency, rather than entirely relying on collaboration with other sensors. Therefore, it can reduce the interdependence between sensors.

In the pre-sampling process, sampling period is $T_1$ (30 seconds). Considering the number of grids that are over-sampled and the region grade, we set the different sampling frequency for sensors in different grade regions. The time interval of sampling in $level_k$ is shown below:

$$T_k = 2^i T_1 \times \sum \left( a_i \times u_i \right),$$

$i \in [0, p)$ or $[p + 1, q)$ or $i \in [q + 1, n]$, $k = 1, 2, 3$. (4)

So the sampling frequency in $level_k$ is shown below:

$$f(l_k) = \lambda \times \frac{1}{T_k}, \ (k = 1, 2, 3; \lambda \text{ is a constant}).$$ (5)

In the sensing process, sensors may move from one region to another. However, the sampling frequency of sensors in these regions is different. If sensors stay in one region for a short time, it may miss some data. From the trajectory of the sensor in Fig. 4, we can see that the sensor moves to the $level_2$ region and then leaves here. Under the condition of the same speed, the sensor stays in the $level_2$ region for a short time. If the dwell time is much shorter than the sampling interval of the sensor, the data in that region may be missed.

![Fig. 4. Moving trajectory in different grade regions.](image)

So we propose the Circle of Time Slice (CoTS) and Cardinal Number Timing Method (CNTM) to solve the sampling error resulted from sensors moving from one area to another. The Time Slice aims to divide the time axis into many short time periods. The sampling interval is much longer than the time slice. CoTS means that sensors check information at the beginning of each time slice. The sensor requires checking its current location, whether it contains the data of current grid and whether it has reached the sampling time. CNTM is a method of calculating time length, as shown in Equation (6):

$$\text{cur\_time} = \text{cur\_time} - \frac{\text{const\_init\_time}}{\text{time\_k}},$$ (6)

where $\text{cur\_time}$ indicates how long it takes to reach the sampling instants. The $\text{time\_k}$ represents the sampling interval in $level_k$ region. The $\text{const\_init\_time}$ is the lowest common multiple of $\text{time\_k}$ ($k = 1, 2, 3$). After a time slice, the $\text{cur\_time}$ is shortened by $\text{const\_init\_time} / \text{time\_k}$. This also ensures that the longer the sampling interval, the more times that sensors check information during the sampling interval. The data collection algorithm based on the sampling frequency is shown as follows.

Algorithm 3: DC-BSF

**Input:** $time_k, \text{const\_init\_time}, \text{transmit\_length}$

**Output:** the data required;

**Initialize** $\text{cur\_time} \leftarrow \text{const\_init\_time}$;

while (during the sampling time) do

\[ \text{if( current location is included in level}_k \text{ then) } \]

\[ \text{cur\_time} = \text{cur\_time} - \frac{\text{const\_init\_time}}{\text{time\_k}}; \]

// the circle of time slice

end if

for $i \leftarrow 0$ to $n$ do

 Traverse all nodes;

 if (dis <= transmit\_length) then

 // dis is the distance between two nodes.

 Process and forward the collected data;

 end if

repeat

if (cur\_time <= 0 &&

 Data of current grid is not included in the node.)

 then Perform sampling task;

 end if

repeat

C. Analysis of algorithm

In algorithm DC-BSF, $T, x*y, n$ and $m$ respectively represent the sampling period, the number of grids in the entire area, sensors and grids that have been sampled. The algorithm is mainly completed in a while circulation and the total number of circulation is $t$. The following three steps are performed in each cycle.

1) Sensors check the grade of the region that the sensor is located and the sampling interval in this grade. So the time complexity in this part is
2) Sensor nodes transmit data between each other. The time complexity in this part is $\Theta\left(n \times x \times y \times (\log_x x) \times (\log_y y)\right)$.

3) Sensor nodes check whether it contains the data of current grid. The time complexity in this part is $\Theta\left((\log_x x) \times (\log_y y)\right)$.

So the time complexity of algorithm DC-BSF is $\Theta\left(n \times x \times y \times (\log_x x) \times (\log_y y)\right)$.

IV. PERFORMANCE EVALUATION

In order to verify the feasibility and superiority of DC-BSF, we carry out the following evaluation based on the real mobility traces provided by Korea Advanced Institute of Science and Technology [17]. The simulation platform we used is Opportunistic Network Environment (ONE) [19]. ONE is a free simulation platform developed in Java language. It can be used to simulate Opportunistic Network and Delay Tolerant Network. The simulation parameter is shown in Table 3.

Table 3: Simulation parameter

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time</td>
<td>35ks (about 10 hours)</td>
</tr>
<tr>
<td>Area</td>
<td>30km x 30km</td>
</tr>
<tr>
<td>The number of nodes</td>
<td>92</td>
</tr>
<tr>
<td>Communication range</td>
<td>100m</td>
</tr>
<tr>
<td>Size of level_k</td>
<td>500m</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>0.5; 0.8; 1; 1.5; 2; 5</td>
</tr>
<tr>
<td>Size of grid</td>
<td>100; 200…; 900; 1000m</td>
</tr>
</tbody>
</table>

We evaluate the feasibility of DC-BSF algorithm in terms of coverage and data redundancy as follows.

In Fig. 5, we compare the coverage with various values of $\lambda$ by ten sizes of grid from 100 to 1000 m. The legend in this figure represents different grid size. We can obviously find that the coverage rate increases with the increase of $\lambda$ regardless of the size of grid. When the coefficient of sampling frequency ($\lambda$) increases from 0.2 to 0.8 the coverage rate increase greatly, but the coverage level is low. When $\lambda > 0.8$, the coverage rate reaches a high level and keeps stable. So the optimum range of $\lambda$ is from 0.8 to infinity considering the coverage rate only.

Data redundancy is an inevitable problem under the condition of high coverage rate. In order to reach the best compromise between coverage rate and data redundancy, we compare the data redundancy with various values of $\lambda$ by ten sizes of grid from 100 to 1000 m. And the simulation parameter is shown in Table 3. From Fig. 6, we can see that the DC-BSF can achieve a lower data redundancy and the data redundancy increases slowly when $\lambda$ is less than 2. On the contrary, the data redundancy is large and increases rapidly when $\lambda > 2$. So the optimum range of $\lambda$ is from negative infinity to 2 considering the data redundancy only.

Therefore, considering the best compromise between coverage rate and data redundancy, we take the intersection of the two parts. From the two sets of simulation above, we can get a conclusion that the optimum range of $\lambda$ is from 0.8 to 2. It means that the data collection method based on the sampling frequency can reduce data redundancy in the condition of achieving...
high coverage when the range of $\lambda$ is from 0.8 to 2.

The simulation results above verified the feasibility of the method we proposed. In order to verify the efficiency of DC-BSF proposed in this paper, we compare it with Cooperative Sensing (CS) [6] in terms of coverage and redundancy. The Cooperative Sensing method is based on spatial-temporal correlation among sensory data.

We have $\lambda=1$ in our DC-BSF and set the parameter $k=1$ in CS. Other parameters in the simulation are the same as in Table 2. As shown in Fig. 7, we compare the DC-BSF with CS about the coverage rate by using ten kinds of grid size. These two methods both get a high coverage rate and the gap between them is small. And then from Fig. 8, we can see that compared to the data redundancy of CS, it is significantly less of DC-BSF. So the method we proposed in this paper outperforms the CS relatively, although the DC-BSF does not achieve its best performance.

V. CONCLUSION AND FUTURE WORK

In this paper, we propose the Division of Region Grade algorithm to divide the entire area into three regions of different grades. Furthermore, we put forward two concepts: CoTS and CNTM. These two methods can solve the sampling error resulting from nodes moving from one area to another. Last but not least, we proposed the Data Collection Algorithm Based on the Sampling Frequency that can reduce data redundancy in the premise of high coverage.

The model proposed in this paper has strict constraints. In the future, we plan to further study and improve it.

ACKNOWLEDGMENT

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Design of Parabolic Reflector Antenna with Two Directional Cosecant-Squared Pattern Using Curve-Deformation Equations

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Abstract — A Ka-band doubly curved reflector antenna for a warning radar system for the road was designed based on the curve-deformation equations. This antenna requires a cosecant-squared radiation pattern in the vertical and horizontal planes. Using curve-deformation equations, the shaped reflector antenna was designed to satisfy the desired beam pattern. The curve-deformation equations include the parameters which determine the shape of the curve, and these parameters are obtained by the optimization process. The simulated result shows the designed antenna satisfies the specifications of the antenna for the road radar system.

Index Terms — Cosecant squared pattern, parabolic antenna.

I. INTRODUCTION

Radar is widely used to detect the obstacles and to avoid collisions on the road and airport surfaces [1]-[2]. In order to survey a wide range, the power received from the reflector antenna needs to be uniform for a fixed height. The relationship between the uniform received power and the distance between the object and the antenna can be defined by the cosecant-squared function [3]. The cosecant-squared pattern can be achieved by displacing the reflector surface from the original parabolic shape [4]-[7]. Recently, the analytical regularization method (ARM) [5] was used to produce the cosecant square pattern in the vertical plane. This method solves a two-dimensional integral equation with Dirichlet boundary condition corresponding to the reflector’s surface. The geometry of a reflector is generated by continuous segments that are defined using parameterization of different length and bending angles. This contour is a two-dimensional closed curve, from which the cosecant-squared pattern is obtained in the vertical plane. In this paper, the equations of the cosecant-squared pattern are derived using the ARM’s parameterization process. Instead of solving differential equations, the parameter optimization method is used to synthesize the desired reflector. Invasive weed optimization is one method that determines the optimum values of the coefficients of a distribution polynomial using the optimization process [2]. In this optimization process, if the coefficients of the distribution polynomial are given, then the radiation pattern can be obtained using commercial software, and this pattern is compared to the cosecant-squared pattern. This procedure continues until the desired pattern is obtained. Here, the optimization process will be used to acquire the optimum values of the parameters corresponding to the bending angle and length of a curve. These parameters determine the curvature in the direction of the vertical and horizontal planes.

II. DESIGN OF ANTENNA

A. Curve-deformation equations

The formula is based on the parameterization equations of ARM [5]. In order to define the formula concerning the geometry of a cosecant-squared pattern reflector, each interval of the geometrical curve is divided as follows:

\[
\frac{2L_{k+1}\pi}{L} - \pi < \theta < \frac{2L_{k}\pi}{L} - \pi, 
\]

where \( L_0 = 0 \), \( L_1 = 2\tan(\alpha/2) \), \( \alpha = \alpha_2 - \alpha_1 \), \( L_{k+1} = L_k + r_k \), \( r_0 = r_1 = 0 \), \( k = 0, ..., N_{\text{max}} \), and \( L = \sum_{k}^{N_{\text{max}}} L_k \).

As shown in Fig. 1, \( \alpha_1 \) and \( \alpha_2 \) are the angles between the \( x \)-axis and the end points of the non-shaped section, and \( \alpha \) is the focal length of the parabolic reflector. In (1), \( N_{\text{max}} \) indicates the number of splitting of \([−\pi, \pi]\) and a parameter \( r_k \) determines the length of the \( k \)-th section. The non-shaped section is defined as the function of a parameter \( \theta \) and is as follows:

\[
x_1(\theta) = -\frac{2\cos(\psi)}{1 + \cos(\psi)}, \quad (2)
\]

\[
y_1(\theta) = \frac{2\sin(\psi)}{1 + \cos(\psi)}, \quad (3)
\]

where \( \psi = \psi(\theta) = \alpha_1 - \alpha(\theta + \pi)L/(4\pi \alpha \tan(\alpha/2)) \), and \( \theta \in [−\pi, 2L_{1}\pi/L - \pi] \). Note that, if \( \psi \) is cancelled...
from (2) and (3), then we have the original parabolic equation with respect to parameters x, y:

$$x = \frac{y^2}{4a} - a.$$  \hspace{1cm} (4)

![Diagram of the shaped reflector with the cosecant-squared pattern directed at a positive angle, and (b) at a negative angle.](image)

Fig. 1. (a) Geometry of the shaped reflector with the cosecant-squared pattern directed at a positive angle, and (b) at a negative angle.

The graph of Equation (4) is plotted as indicated by the red dotted line in Fig. 1. The k-th section of the shaped curve of an antenna with cosecant-squared pattern can be represented by a function of parameter $\phi$, which is defined on the interval $\phi \in [2L_{k-1} \pi/L - \pi, 2L_k \pi/L - \pi]$, and the line when $\phi$ is varying is as follows:

$$x_k(\phi) = -2\cos(\alpha_k)/(1 + \cos(\alpha_k)) + \frac{(\phi + \pi)L}{2\pi} - L_{k-1}\cos(\alpha_k) + \sum_{i=1}^{k} r_i \cos(\alpha_i), \hspace{1cm} (5)$$

$$y_k(\phi) = 2\sin(\alpha_1)/(1 + \cos(\alpha_1)) - ((\phi + \pi)L/2\pi - L_{k-1})\cos(\alpha_k) - \sum_{i=1}^{k} r_i \sin(\alpha_i), \hspace{1cm} (6)$$

where $\alpha_k > 0$, $k = 2, 3, ..., N_{\text{max}}$, and the last summation $\Sigma_{i=3}^{k}$ is zero when $k = 2$.

In Equations (5) and (6), $\alpha_k$ is the bending angle of the k-th section. Using Equations (2) to (6), the shaped reflector of the cosecant-squared pattern in the vertical plane can be obtained by determining $\alpha_i$ and $r_i$. As shown in Fig. 1 (a), the sections of the shaped parabolic curve are located on the lower part of the non-shaped section. Thus, the cosecant-squared pattern appears at positive angle. However, in order to detect an object on the road, the cosecant beam should be directed at a negative angle. For this purpose, modifications of (5) and (6) are needed. First, the parameters for the translation are defined as:

$$x_{\text{max}} = \max\{x_i(\phi) | \phi \in [-\pi, 2L_i \pi/L - \pi], y_i(\phi) \geq 0\},$$

$$x_{\text{max}2} = \max\{x_i(\phi) | \phi \in [-\pi, 2L_i \pi/L - \pi], y_i(\phi) < 0\},$$

$$y_{\text{max}} = \max\{y_i(\phi) | \phi \in [-\pi, 2L_i \pi/L - \pi]\},$$

$$y_{\text{min}} = \min\{y_i(\phi) | \phi \in [-\pi, 2L_i \pi/L - \pi]\},$$

and

$$x_{\text{move}} = \begin{cases} x_{\text{max}} & \text{if } \alpha_1 \geq 0 \\ x_{\text{max}2} - x_{\text{max}} & \text{if } \alpha_1 < 0 \end{cases}, \hspace{1cm} y_{\text{move}} = y_{\text{max}} - y_{\text{min}}.$$

The function that determines the curve of the reflector with the cosecant-squared pattern directed at a negative angle can be expressed as:

$$x_k'(\phi) = x_2(\phi) + \sum_{i=3}^{k} r_i \cos(\alpha_i) + x_{\text{move}}, \hspace{1cm} (7)$$

$$y_k'(\phi) = y_2(\phi) + \sum_{i=3}^{k} r_i \sin(\alpha_i) + y_{\text{move}}. \hspace{1cm} (8)$$

Using (7)-(8), the geometry of an elevation direction of reflector can be obtained. The deformation process of an azimuth direction of reflector is carried out on each fraction of partition of the z range. For a fixed point $(x_0, y_0)$ of the shaped curve shown in Fig. 1, the right side of a curve on the transverse section of a $x-z$ plane through $y_0$ is expressed as a coordinate system $(x, z)$:

$$x = c_j \frac{z^2}{4a} + x_0, \hspace{1cm} (9)$$

where a parameter $c_j$ determines the deformation level of the j-th section, and is less than 1. The left section of the curve can be symmetrically obtained from the right section.

**B. Design of reflector using curve-deformation equations**

The antenna for the detection radar system requires the specifications presented in Table 1. As shown in Fig. 2, this antenna was installed at a height of 6 m, and was
designed to detect within a band of road 20 m wide.

Table 1: Specifications of antenna

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Horizontal</th>
<th>Vertical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequency</td>
<td>34.5 GHz</td>
<td>34.5 GHz</td>
</tr>
<tr>
<td>Maximum gain</td>
<td>32 dBi</td>
<td>32 dBi</td>
</tr>
<tr>
<td>Cosecant-squared region</td>
<td>1.14°~7.62°</td>
<td>0.34°~2.29°</td>
</tr>
<tr>
<td>Size of antenna</td>
<td>0.20×0.217 m²</td>
<td></td>
</tr>
</tbody>
</table>

The measurable distance from the antenna to the target by this radar system is between 150 and 1000 m. In order to obtain the desired cosecant-squared pattern, the values of $\alpha_i$, $r_i$, and $c_j$ have to be determined. The first step of the process is to determine the region of the curve that is deformed. Considering the half-power of the radiation pattern of the feed horn, the outside of the half-power angle of the feed pattern was selected as the area of deformation, as shown in Fig. 1.

The shaped curve is approximated by $N_{\text{max}}$ sections. In this paper, $N_{\text{max}}$ was set to 8. The next step was to select the initial parameters ($\alpha_i$, $r_i$, and $c_j$) randomly. These parameters were inserted into the deformation Equations (7)-(9), and the three-dimensional geometric data was obtained. These data were imported into CATIA (commercial software), and the surface of the reflector was designed and saved as a CATIA file. This surface file was imported into CST (commercial software), and the radiation pattern of the reflector was obtained using CST. Then, this pattern was compared to the desired cosecant-squared pattern. If the difference error between the simulated pattern and the desired pattern is greater than the tolerance limit, then the parameters have to be corrected. The tolerance limit means the acceptable difference error between the desired pattern and the selected pattern. The tolerance limit function can be defined in the same way as introduced in [2]. This process continues until the pattern is well fitted to the desired patterns. Figure 3 (a) shows the geometry of the designed reflector antenna. The focal length was 0.15 m and the offset angle was 35°. The size of the reflector was 0.20×0.217 m². Because the cosecant deformation of a reflector is performed in the azimuth and elevation directions, the upper edge of the reflector is inclined toward the aperture along the vertical direction, and the lower edge is bent back along the azimuthal direction, as shown in Figure 3 (b). Table 2 shows the optimized values of the parameter in the curve-deformation equations. The parameter $r_i$ determines the length of shaped curve and, we set the parameter $r_i$ as the same value 0.0189 for all $i > 1$. 

---

![Fig. 2. Range of the detection by the radar system.](image-url)

![Fig. 3. Shaped reflector antenna and comparison with the non-shaped parabolic reflector.](image-url)
Table 2: Parameters of curve-deformation equations

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value [degree]</th>
<th>Parameter</th>
<th>Parameter</th>
</tr>
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<td>$c_1$</td>
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</tr>
<tr>
<td>$\alpha_2$</td>
<td>37</td>
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<td>$\alpha_3$</td>
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<td>$\alpha_4$</td>
<td>65</td>
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<tr>
<td>$\alpha_5$</td>
<td>62</td>
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<td>$\alpha_6$</td>
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<td>$\alpha_7$</td>
<td>57.5</td>
<td>$c_7$</td>
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<td>$\alpha_8$</td>
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<tr>
<td>$\alpha_9$</td>
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<tr>
<td>$\alpha_{10}$</td>
<td>51.5</td>
<td>$c_{10}$</td>
<td>0.48</td>
</tr>
</tbody>
</table>

III. RESULTS OF SIMULATION

A. Measurement of radar system

The newly designed antenna was simulated by CST in order to obtain the radiation patterns. To be agreed with the cosecant-squared pattern using the curve-deformation equations, designing a cosecant antenna is performed in the early stage of the optimization. The results of the radiation patterns of the main beam are displayed at Fig. 4. The beamwidths of the radiation patterns are $2.1^\circ$ and $4.2^\circ$ in the azimuthal and elevation directions respectively and the gain is 33.2 dBi. To achieve the desired pattern of Fig. 4, around five to eight optimization procedures are enough. We calculated errors between the desired pattern and the designed pattern using CST. The parameters of the deformation Equations (7)-(9) are corrected to optimized values. But in this case, only the pattern at zero angle was obtained, and in order to get the broad beam, the beamwidth, gain and patterns at each angle must be considered. Moreover, the monopulse beam pattern at each angle also have to be considered because it is used to detect the exact location of the debris on the road. The optimization process have to continue until the desired gain distribution at the detection area as shown at Fig. 5 are obtained, and 8–10 optimization steps were carried out.

The gain of Fig. 5 was obtained proportional to the square of the distance, which means the gain loss of the antenna.

Figure 5 shows that the designed antenna has a wide broad cosecant beam directed in a downward direction, which is suitable for detecting objects on the road. Figure 6 displays the power distributions of a sum and a delta pattern of the final designed cosecant antenna. In Fig. 7, these patterns are compared with the desired cosecant-squared patterns. The dual-mode horn antenna for a monopulse feed system was used to obtain the sum and difference beams. The beamwidth used as the edge taper was 14 dB and 18 dB, in the azimuth and elevation planes, respectively. Because the range of the degree satisfying the cosecant-squared pattern is very narrow, the shaped curve was designed to have a wide beamwidth in order to achieve the cosecant-squared pattern. Even though the pattern did not agree well with the cosecant-squared curve, the antenna had higher gain, and the difference monopulse pattern had wider beamwidth, than would an antenna with a pattern well-fitted to the cosecant-squared region over the wide region. As shown in Table 1, the cosecant regions of horizontal and vertical directions were $1.14^\circ$–$7.62^\circ$ ($\leq 3.81^\circ$) and $0.34^\circ$–$2.29^\circ$, and the radiation patterns of the main beam presented in Fig. 7 satisfied the desired cosecant-squared level. Figure 8 shows the horizontal sections of the radiation pattern of the reflector antenna when the elevation angles varied from $0^\circ$ to $-5^\circ$. In the case of the sum patterns, the maximum gain of the main horizontal section was 32 dBi, and the beam peak decreased according to the main vertical section of the pattern. The difference between the maximum gain of $0^\circ$ sum pattern and that of a $4^\circ$ sum pattern was only 3 dBi. The sum patterns also maintained the shape and the beamwidth, and satisfied the desired cosecant-squared level. This means that the antenna is designed to be suitable for detecting the debris all over the surface. The difference pattern can be used to determine accurately the angular location of the target. The gap between the null point and the peak point of the difference pattern was almost $5^\circ$, and it is sufficient to determine the angular location of the target because the maximum angle in the azimuthal direction within the detection area.
is ±3.81°.

Figure 9 shows the monopulse curve that represents the difference between the gain of the sum pattern and the gain of the difference pattern.

Fig. 6. Power distribution of the final designed cosecant antenna along the range of detection.

Fig. 7. Comparison of a designed pattern with an ideal csc² pattern.

Fig. 8. Azimuthal section of the radiation pattern of the reflector varying elevation angles.
IV. CONCLUSION

The Ka-band shaped reflector antenna was designed based on a curve-deformation equation. The deformation of the surface was performed in the vertical and horizontal directions. The cosecant-squared patterns in the vertical and horizontal planes were obtained by simulation using the CATIA and CST software packages. These patterns satisfied the specifications of the antenna for a detection radar system for the road. The method herein presented can be used to design antennas for the detection of foreign-object debris on airport surfaces, for surveillance radar, and for the ship-mounted surface radar.

V. ACKNOWLEDGMENT

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Compact Broad Band-Stop Filter with Circular Fractal-Shaped Stubs for X-Band Radar Applications

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Abstract — In this letter, we use the fractal structures to design a novel compact band-stop filter with prominent cut-off sharpness and wide stop-band for X-band applications. By cutting five U-shaped slots on the ground plane and by inserting five Fractal- Shaped stubs in the microstrip transmission line, the proposed structure is created hence a constant and flat impedance bandwidth at the X-band can be produced. The operating frequencies of the filter can be easily controlled by changing the protruded fractal-shaped stubs dimensions, without changing the area taken by the structure. The experimental results show good agreement with simulation results and demonstrate that excellent stop-band performance could be obtained through the proposed band stop filter.

Index Terms — Band-stop filter, circular fractal-shaped stubs, defected ground plane, X-band applications.

I. INTRODUCTION

Conventionally the microwave Band-Stop Filter (BSF) is implemented either by all shunt stubs or by series connected high-low stepped-impedance microstrip line sections. However, generally these are not easily available in microwave band due to the high impedance microstrip line and the spurious pass-bands. To remove these disadvantages, defected ground structures for microstrip lines have been presented in recent years. They have been presented in a number of different shapes for filter applications [1-2]. This technique is suitable for periodic structures, and for both band-stop and band-pass filters, e.g., [3]-[4]. The Defected Ground Structure (DGS) applied to a microstrip line causes a resonant character of the structure transmission with a resonant frequency controllable by changing the shape and size of the slot.

This paper introduces a DGS with U-shaped slots. The resonant behavior of the DGS used here introduces transmission zeroes to the filter response and consequently improves its stop-band performance. The proposed structure is designed based on the fractal structures. By using this periodical structure, we have a constant and flat impedance bandwidth at the X-band frequency range. The designed filter has a small dimension of $10 \times 15 \times 0.635 \text{ mm}^3$.

II. BAND-STOP FILTER DESIGN AND CONFIGURATION

The proposed quasi-elliptic band-stop filter configuration with apertures under the high-impedance transmission lines is shown in Fig. 1. In general, the cut-off frequency of the microwave band-stop filter can be adjusted by setting proper values of the lumped elements of the filter [5]. In addition, to realize the desired capacitive and inductive values of the filter elements by the stubs of the high/low impedance transmission lines, the characteristic impedance and effective dielectric constant of these transmission lines have to be determined. The band-stop filter in Fig. 1 was designed and fabricated on a Rogers RT/Duroid 5880 substrate with 0.635 mm in thickness and with a relative dielectric constant of 2.2. Defected Ground Structure (DGS) evolved from Photonic Band Gap (PBG) is realized by etching defected pattern and slot in the ground plane. The etched defect in ground plane disturbs the shield current distribution in the ground plane. This disturbance can increase the effective capacitance and inductance of a transmission line respectively. Thus, an LC equivalent circuit can represent the proposed unit DGS circuit [1-2]. The proposed DGS slot is shown in Fig. 1 (b). The slot is etched in the ground metallization under the microstrip line. This slot has a major advantage in providing tighter capacitive coupling to the line in comparison to known microstrip DGS. Moreover, the resonant frequency of the structure can be controlled by changing the distance between the U-shaped slots. The resonant frequency of the slot can be modified by changing the overall slot size, which shifts the cut-off frequency of the filter down. To shift the frequency up instead of frequency back, it is necessary to reduce the inductance of the narrow strip-line that is located over the slot. This can easily be done by increasing the width of the strip [6]. The final values of presented band-stop filter design parameters are specified in Table 1.
observed that when five U-shaped slots on the ground plane and five fractal-shaped stubs in the microstrip transmission line are used, the return loss of the proposed filter is increased amount of transmission zeros in the insertion loss. As shown in Fig. 2 (b), the five U-shaped slots on the ground plane and five fractal-shaped stubs in the microstrip transmission line also influence the bandwidth of the insertion loss. The proposed transmission line structure can be used to extend the lower edge frequency and the upper edge frequency of the insertion loss bandwidth.

![Diagram](image)

**Fig. 1. Geometry of proposed microstrip filter: (a) top view and (b) bottom view.**

**Table 1: Optimal dimensions of proposed filter**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value (mm)</th>
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<th>Value (mm)</th>
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<td>L₂</td>
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</tr>
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<td>Lₛ₂</td>
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</tbody>
</table>

**III. RESULTS AND DISCUSSIONS**

The microstrip band-stop filter, as shown in Fig. 1, was designed on both substrate sides by opening apertures in the ground metallization under the high-impedance transmission line. Replacing some of the apertures by the proposed U-shaped structure introduces transmission zeroes. The number of transmission zeroes is equal to the number of apertures pairs according to centre in this case this number is three [6]. For the input/output connections 50-Ohm microstrip lines are used. The simulated results are obtained using the Ansoft simulation software high-frequency structure simulator (HFSS) [7], [8]. To minimize physical size of the proposed low-pass filter and increase its bandwidth, five U-shaped slots on the ground plane and five fractal-shaped stubs in the microstrip transmission line inserted to alter the input impedance characteristics. Figure 2 shows the return/insertion loss characteristics of the various filter used for simulation studies. From the result in Fig. 2 (a), it is observed that when four steps of semi-circular fractal-shaped open stubs are introduced into the microstrip transmission line to alter the input impedance characteristics.

To minimize physical size of the proposed band-stop filter and increase its bandwidth, four steps of semi-circular fractal-shaped open stubs are introduced into the microstrip transmission line to alter the input impedance characteristics.

Return/insertion loss characteristics for the structure of the various filter used for simulation studies are compared in Figs. 3 (a) and (b). From the result in Fig. 3 (a), it is observed that when four steps of semi-circular fractal-shaped open stubs are used, the return loss of the proposed filter is changed at lower frequencies. As shown in Fig. 3 (b), the semi-circular fractal-shaped open stubs also influence the bandwidth of the insertion loss.

The proposed transmission line structure can be used to extend the lower edge frequency and the upper edge frequency of the insertion loss bandwidth. The proposed filter with optimal design, as shown in Fig. 4, was fabricated and tested in the Antenna Measurement Laboratory at Urmia University. Figure 5 shows the

![Graph](image)

**Fig. 2. Simulated return/insertion loss characteristics for the various filter structures: (a) return loss and (b) insertion loss.**
simulated and measured insertion and return loss of the filter.

![Simulated return/insertion loss characteristics for the various steps of Koch-Snowflake fractal structures: (a) return loss and (b) insertion loss.](image)

![Photograph of the realized printed band stop filter: (a) top view and (b) bottom view.](image)

![Measured and simulated return/insertion loss for the proposed band stop filter.](image)

As shown in Fig. 5, a flat insertion and return losses are introduced to the filter response at about 8.02 to 12.07 GHz. Consequently a wide stop-band was achieved. Additionally, the proposed DGS band-stop filter also has characteristics of wider and deeper stop-band than those of conventional band-stop filters [9], [10]. As shown in Fig. 5, there exists a discrepancy between measured data and the simulated results. This discrepancy is mostly due to a number of parameters such as the fabricated filter dimensions as well as the thickness and dielectric constant of the substrate on which the filter is fabricated, the wide range of simulation frequencies and also the effect of SMA [10], [11]. In order to confirm the accurate return loss characteristics for the designed antenna, it is recommended that the manufacturing and measurement process need to be performed carefully, besides, SMA soldering accuracy and RT/Duroid substrate quality needs to be taken into consideration.

IV. CONCLUSION

In this paper, a novel band-stop microstrip filter by using a modified defected ground structure is presented for satisfying X-band applications. By cutting five U-shaped slots on the ground plane and by inserting five fractal-shaped stubs in the microstrip transmission line, the proposed structure is created; hence, a constant and flat impedance bandwidth at the X-band can be produced. The desired resonant frequencies are obtained by adjusting the number of U-shaped slots on the ground plane. Also, in order to enhance the impedance bandwidth characteristic five fractal-shaped stubs are inserted in the microstrip transmission line. Prototypes of the proposed filter have been constructed and studied experimentally. The measured results showed good agreement with the numerical prediction and good flat insertion and return losses characteristics.

REFERENCES


RCS Validation of Asymptotic Techniques Using Measured Data of an Electrically Large Complex Model Airframe

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Abstract — This paper validates the accuracy with which various asymptotic techniques including RL-GO and SBR can calculate the RCS of an electrically large complex airframe. This target has a maximum electrical length of 106λ. Two CEM packages are utilized namely, CST MWS and FEKO. The simulated RCS results are compared to measured RCS data, obtained in a compact range. The effect of the 3D CAD model accuracy on the simulation accuracy is also investigated. Comparisons between simulated and measured RCS data are provided using RCS plots and ISAR images.

Index Terms — Asymptotic methods, CAD model accuracy, RCS measurements, validation.

I. INTRODUCTION

Radar cross section (RCS) modelling and simulation has a wide range of applications in the field of radar and electronic warfare (EW). These include platform detectability analysis, the generation of test data for development and testing of radar and EW systems, as well as signature database generation for applications such as non-cooperative target recognition (NCTR). For these applications it is important that calculated radar signatures of targets are accurate and obtained within reasonable timeframes. The accuracy of calculated RCS results depends on a few factors. Two of the factors, investigated in this study, include the accuracy of the 3-dimensional (3D) computer aided design (CAD) model of the target, as well as the computational electromagnetic (CEM) method utilized.

It was shown in [1] that the overall shape of targets CAD models, as well as small geometric features on the models can have an impact on the RCS scattering characteristics. The differences between four aircraft CAD models were investigated using simulated data and quantified using different contour-based shape descriptors. The four targets included a Pilatus PC-21, an F-16 fighter jet, and two models of the same aircraft, namely a Cessna 172.

The second factor contributing to the simulation accuracy is the CEM method. Asymptotic CEM techniques are generally used for RCS predictions of electrically large complex targets. Numerous asymptotic techniques are available, which are capable of solving electrically large scattering problems within timeframes that are a fraction of the time required by full-wave methods. Some of these methods include physical optics (PO), geometrical optics (GO), the physical theory of diffraction (PTD), ray-launching GO (RL-GO), as well as shooting and bouncing rays (SBR).

In [2], a new efficient ray-tracing algorithm for the calculation of RCS, based on PO and PTD, was presented. This method was evaluated by comparing the monostatic RCS simulations of a few different targets, with either full-wave method of moments (MoM) results or RCS measurements used as reference. The targets investigated included a thin and thick flat plate, trihedral corner reflector, generic cruise missile and two aircraft models. The RCS results obtained for the first four targets were compared to MoM simulation results. Good agreements between the results were observed. The first aircraft target was a 1:32 scaled model with an electrical length of 60λ. The simulated results for this aircraft were compared to measured RCS data, with rather good agreement observed. The physical model used in the RCS measurements was manufactured using the simulated CAD model. High range resolution (HRR) profiles of both aircraft targets, scaled to original size, were generated using the data calculated with the PO and PTD algorithm, and compared to one another. It was observed that the objects could be distinguished based on these profiles.

Recently a study evaluated the suitability of three
CEM techniques, including the multilevel fast multipole method (MLFMM), PO and PO with SBR, for RCS calculations of electrically large targets [3]. Three targets were used for the analyses, and included a trihedral corner reflector, generic cruise missile similar to that used in [2], and the high fidelity Cessna 172 model used in [1]. Only simulated RCS results were considered, with MLFMM data used as reference for the comparisons. It was shown that the RCS of the corner reflector and generic cruise missile calculated with the PO and PO with SBR methods compared well with the MLFMM results.

In [4], the measured and simulated RCS data of a Boeing 777 scale model, with electrical length of 20λ, was compared. A commercially available 3D CAD model of the aircraft was simulated using the CADRCS software package. This package implements PO combined with ray-tracing and shadowing to calculate the RCS of objects. Although good correspondence between the main features in the RCS diagrams were obtained, differences were still observed which highlighted the need for different techniques to fully represent the RCS of an object.

In [5], the accuracy and efficiency with which full-wave and asymptotic CEM methods could predict the RCS of a large complex airframe was investigated. This study utilized the same physical 1:25 scale model of a Boeing 707 that was used in an installed antenna performance investigation [6]. RCS measurements of this target were obtained in a compact range at the University of Pretoria, South Africa. The methods that were validated included PO, PO with SBR and MLFMM. Three EM simulation packages were utilized in this study, viz. CST Microwave Studio (MWS), FEKO and SigmaHat. All of the methods showed good agreement with the measured data over the important azimuth ranges where the main features were found.

This paper serves to illustrate the effects of different options and asymptotic technique implementations on the simulated RCS results for a realistic representation of a large and complex model airframe. Measured RCS data of a conducting Boeing 707 scale model, with an electrical length of 106λ, is used to illustrate the effect of the geometrical accuracy of CAD models on calculated RCS results. Simulated data of a generic CAD model, constructed from canonical structures [6], and a laser scanned CAD model, generated from the physical airframe, are compared to the measured RCS results obtained in a compact range. Secondly, the accuracies of a few different implementations of asymptotic techniques to calculate the RCS of the large complex airframe are validated against the measured results. The methods include RL-GO as implemented in FEKO [7] and SBR using CST [8]. For the RL-GO method the effect of using different mesh types, consisting of linear and curvilinear triangles, is illustrated. The differences between the measured and simulated RCS results using the SBR method with rays and ray-tubes are also presented. Comparisons of the measured and simulated datasets are conducted using RCS graphs and inverse synthetic aperture radar (ISAR) images to gain more insight into the scattering mechanisms.

II. CAD MODEL ACCURACY

RCS measurements of the scale model Boeing 707 were conducted in the compact range at the University of Pretoria, South Africa. This setup is shown in Fig. 1. An investigation of the effect of the geometrical accuracy of two different 3D CAD models of the target, on the simulation accuracy, was conducted. These models included the scanned and generic CAD models.

Fig. 1. Scale model setup in the compact range at the University of Pretoria, South Africa.

The scanned model was developed by converting the 3D point cloud, generated with a handheld laser scanner, to a mesh model using 3D processing software [5]. The mesh model was imported into FEKO where a simulation mesh was created. The scanned model has an average accuracy of better than 0.2 mm relative to the actual scale model. An overlay of these two models, with a zoomed in view of the engines, is provided in Fig. 2. The scanned CAD model is shown in yellow and the generic CAD model in orange.

Fig. 2. Overlay of scanned (yellow) and generic (orange) CAD models and zoomed-in view of engines.

The geometrical differences between the two CAD models are clearly observed in Fig. 2. The largest discrepancies are the wing alignments, the engine positions and the details within the engines. It can further be observed that the scanned CAD model is a more realistic and accurate representation of the actual scale model of the target that was used for the measurements, shown in Fig. 1.
Experiments were conducted to determine which CAD model of the target would be the preeminent model for validating the asymptotic methods. It was shown in [5] that the RCS of the Boeing 707, calculated with PO compared very well with the RCS calculated with the full-wave MLFMM method at 10 GHz and 17 GHz. Consequently it was decided to analyze the effect of the geometrical accuracy of the two CAD models, relative to the scale model, on the simulation accuracy with the PO method implemented in FEKO, at both these frequencies as well as at a lower frequency of 3 GHz. Figures 3, 4 and 5 provides a comparison between the measured data and PO simulated data generated with the scanned and generic CAD models at 3 GHz, 10 GHz and 17 GHz, respectively.

The PO simulations of both the scanned and generic CAD models produced comparable results to the measured data as seen in Figs. 3, 4 and 5. Larger discrepancies between both PO simulated data sets and the measured data are observed over 40° and 60°. It is however clear that, the scanned CAD model yields overall more accurate RCS results compared to the measured data than the results obtained with the generic CAD model. This is particularly evident in the nose (0°) and tail (180°) regions of the airplane where the RCS values are lower. As the frequency increases, the smaller details on the models play larger roles in the RCS signatures.

Further analyses of the structural behavior of the scale model and the scattering centers of the two CAD models were conducted. This was done by generating ISAR images of the measured and PO simulated targets that were illuminated from the front (-30° to 30°) and from the port broadside (60° to 120°). The ISAR measurements and simulations were conducted for VV-polarized monostatic RCS centered at 10 GHz using 801 frequencies in steps of 8 MHz, and 101 frequencies in steps of 60 MHz, respectively. Figures 6 and 7 provides the ISAR images of the physical scale model measured in the compact range and the PO simulation of the 3D scanned CAD model as well as the generic 3D CAD model illuminated from the front and side, respectively.

It is evident from the ISAR image of the measured data in Fig. 6 (a) that there are certain areas on the target that produce dominant scattering when illuminated in this range, such as the engines. The wings and nose of the aircraft also produce some scattering. Even though the wooden mounting rod used to position the model in the compact range was covered with radar absorbing material (RAM), it still produces some scattering, not present in the simulations. Almost no scattering is observed on the stabilizers of the aircraft. Very similar scattering patterns located at the nose and cockpit area of the measured scale model and scanned CAD model are observed in Figs. 6 (a) and (b). A different scattering pattern is observed in this area of the generic CAD model seen in Fig. 6 (c). A lot less scattering is observed from the wings of the generic CAD model than with the measured data. Although the scattering produced by the engines of the scanned CAD model is slightly less than that of the physical scale model, these scattering patterns are very similar. The cavities in the engines of the generic CAD model produce slightly different scattering patterns than the enclosed engines of the scale model and scanned CAD model.

It is clear in Fig. 7 that the main parts contributing to the RCS of the aircraft, in this range, include the two visible port side engines, the fuselage, and the vertical stabilizer. The scattering produced by the fuselage of the CAD models are very similar to the measured data, however slightly less scattering is produced by the fuselage of the generic CAD model, Fig. 7 (c). The scattering center located on the vertical stabilizer of the generic CAD model is larger than that of the measured data. The obscured starboard side engines of the scale model and the scanned CAD model also contribute somewhat to the RCS patterns observed in Figs. 3, 4 and 5, whereas no scattering is observed from this part of the generic CAD model. The wingtip and the tip of the horizontal stabilizer of the scale model and the scanned CAD model produce scattering not observed with the generic CAD model.

The differences between the measured and simulated scattering centers observed in the ISAR images in Fig. 6 and Fig. 7, clarifies some of the discrepancies observed in the angular RCS data provided in Figs. 3, 4 and 5. It is evident that the scanned CAD model delivers more accurate scattering results compared to the measured data when comparing the various scattering centers. This can be attributed to the fact that the scanned CAD model is a more accurate geometrical representation of the actual scale model used for measurements than the generic CAD model. Additional scattering analysis of the scanned CAD model was therefore conducted to investigate the reason for the discrepancies observed between 40° and 60°. The ISAR images of measured and simulated data illuminated from 30° to 60° are provided in Figs. 8 (a) and (b).

A few main scattering points are observed in the image of the measured data, Fig. 8 (a). These are found at the leading edge of the wing, the juncture between the wing and the fuselage, the engines and the leading edge of the horizontal stabilizer of the aircraft. The corner reflector created between the wing and the fuselage is the dominant scattering center over this azimuth range. Some of the same scattering centers, although with lower intensity, are observed in the simulated data in Fig. 8 (b). The dominant measured scattering center located at the corner reflector, formed between the wing and the fuselage of the airplane, is
not present in the PO simulated data. This explains why the simulated RCS is lower than the measured data over this range.

Fig. 3. RCS at 3 GHz measured and simulated in FEKO with PO using the scanned and generic CAD models.

Fig. 4. RCS at 10 GHz measured and simulated in FEKO with PO using the scanned and generic CAD models.

Fig. 5. RCS at 17 GHz measured and simulated in FEKO with PO using the scanned and generic CAD models.

Fig. 6. ISAR images of: (a) measured data, (b) PO simulation of scanned CAD model, and (c) generic CAD model illuminated from the front.

Fig. 7. ISAR images of: (a) measured data, (b) PO simulation of scanned CAD model, and (c) generic CAD model illuminated from the side.
Further analysis of the RCS capabilities of the other asymptotic methods were conducted exclusively with the scanned CAD model to minimize the errors introduced in the radar signature due to geometrical differences between the measured and simulated targets.

Fig. 8. ISAR images of: (a) measured data, and (b) PO simulation illuminated from 30° to 60°.

III. VALIDATION OF ASYMPTOTIC METHODS

A. RL-GO as implemented in FEKO

RL-GO (FEKO) simulations were performed at 3 GHz and 17 GHz and were validated against measured data. No edge-diffractions were taken into account. The effects of two different mesh types, compatible with this method, on the simulation accuracy were investigated. These meshes included a linear and curvilinear triangular mesh that is available with the FEKO Suite 7.0.2 Feature Update [9, 10]. The RCS of the CAD model, meshed with both types of meshes, was computed with the RL-GO method at both frequencies. One and three interactions were considered. It was found that the RL-GO data using a curvilinear mesh was very inaccurate with multiple interactions and is therefore not shown. The RCS results obtained with the linearly meshed model considering three interactions are provided in Figs. 9 and 10, respectively. The RCS results using both mesh types with one interaction are provided in Figs. 11 and 12, respectively.

It is clear from Figs. 9 and 10 that the RL-GO data using a linear mesh with three interactions follows a similar trend as the measured RCS data. However, large discrepancies are observed between the nose region of the airplane and the broadside reflection (20° to 70°) as well as the broadside reflection and the tail region of the aircraft (110° to 170°). The simulation accuracy clearly increased significantly with respect to the measured data when only one interaction is considered, especially over the range of 110° to 170°, as seen in Figs. 11 and 12. There is overall excellent agreement between this simulated RCS data and the measured data, especially in the ranges where the RCS values are higher (above -5 dBsm). Some ranges are still slightly inaccurate, 40° to 60° and 110° to 170°. The RL-GO data of the linearly and curvilinearly meshed models are almost identical. These RL-GO results are also very similar to the PO results shown in Figs. 3 and 5.

Further scattering analysis of the RL-GO method with three interactions is conducted with the linearly meshed target. Scattering analyses are also conducted of the RL-GO method when only one interaction is considered with both mesh types. The same ISAR measurement and simulation setups as described in Section II were implemented, with the illumination from 110° to 170°. Because the RCS calculated with the linearly and curvilinearly meshed model, considering a single interaction, are so similar only the curvilinear data is shown. The three ISAR images are provided in Fig. 13.

It is clear from the ISAR image of the measured data seen in Fig. 13 (a) that the main scattering is produced by the corner reflector created between the trailing edge of the wing and the fuselage, the vertical stabilizer, and the trailing edges of the engines. Most of these main scattering centers are also observed in the RL-GO simulation image in Fig. 13 (b). However, the calculated scattering produced by the engines and the trailing edge of the wing are much higher than the measured data. This explains the larger simulated RCS value over this range in the angular RCS data provided in Figs. 9 and 10. When only one interaction is considered the scattering centers are very similar to the measured data as seen in Fig. 13 (c). The reason for the reduced error in the angular RCS data over this range as seen in Fig. 11 and 12 is due to the less noisy scattering observed between the fuselage and wing of the airplane. The calculated RCS is still slightly higher than the measured data due to the higher scattering produced by the engines and the trailing edge of the wing.

A summary of computational resources required by this method is provided in Table 1.

Fig. 9. RCS at 3 GHz measured and simulated in FEKO with RL-GO using a linear mesh considering 3 interactions.
Fig. 10. RCS at 17 GHz measured and simulated in FEKO with RL-GO using a linear mesh considering 3 interactions.

Fig. 11. RCS at 3 GHz measured and simulated in FEKO with RL-GO using linear and curvilinear meshes considering 1 interaction.

Fig. 12. RCS at 17 GHz measured and simulated in FEKO with RL-GO using linear and curvilinear meshes considering 1 interaction.

Fig. 13. ISAR images of: (a) measured data, (b) RL-GO simulation using a linear mesh with 3 interactions, and (c) using a curvilinear mesh with 1 interaction, illuminated from 110° to 170°.

B. SBR as implemented in CST MWS

The SBR method implemented in CST MWS 2015 was validated. The ability of this method to calculate the RCS of the airframe was investigated using rays and ray-tubes at 3 GHz and 17 GHz. The optimum number of reflections required, in terms of solution accuracy and execution time, was found to be three. The RCS results are provided in Figs. 14 and 15, respectively.

It is clear from Fig. 14 and Fig. 15 that there is overall excellent agreement between the measurements and the RCS calculated with the SBR method using rays. The RCS calculated with the SBR method using ray-tubes does not compare as well with the measured RCS over the entire azimuth range. Large discrepancies are observed between 40° to 60° where this simulated data is larger than the measured data. In this range, the RCS calculated with the SBR method using rays was slightly lower than the measured data. ISAR images of the measured and SBR simulated data using rays and ray-tubes were generated to examine the disagreements in this range. Figure 16 provides the ISAR images of the measured data, and the SBR simulation using rays, and ray-tubes illuminated from 30° to 60°. A few main scattering points are observed in the image of the measured seen in Fig. 16 (a). These are found at the leading edge of the wing, the juncture between the wing and the fuselage, the engines, the horizontal stabilizer, and the nose of the aircraft. The corner reflector created
between the wing and fuselage is the dominant scatterer over this azimuth range. There is overall excellent agreement between the scattering centers observed in the measured data and the simulated data generated with the SBR method using rays, shown in Fig. 16 (b). The scattering produced by the corner reflector, formed between the wing and the fuselage of the airplane, is slightly lower in this simulated data than in the measured data. This explains the slightly lower simulated RCS values observed in this range seen in Fig. 14 and Fig. 15. The main scattering centers found in the measured data are also observed in the ISAR image produced by the SBR method using ray-tubes, seen in Fig. 16 (c). However, the scattering center produced by the corner reflector, found between the wing and fuselage of the airplane, has a much higher value than the measured data. The simulation data is also noisier, possibly due to cross range smear [11]. This explains why the RCS calculated with this method is higher than the measured data from 40° to 60°.

A summary of computational resources required by this method is provided in Table 1.

![Fig. 14. RCS at 3 GHz measured in the compact range and simulated in CST with SBR using rays and ray-tubes.](image1)

![Fig. 15. RCS at 17 GHz measured in the compact range and simulated in CST with SBR using rays and ray-tubes.](image2)

![Fig. 16. ISAR images of: (a) measured data, (b) SBR simulation with rays, and (c) with ray-tubes illuminated from 30° to 60°.](image3)

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### IV. CONCLUSION

The effect of the geometrical accuracy of the 3D CAD, with respect to the scale model, on the accuracy of the calculated RCS data was investigated. This was done by calculating the RCS of two CAD models and comparing the results with measured RCS data generated in a compact range. A conducting scale model of a Boeing 707, with a maximum electrical length of 106λ, was measured. The two CAD models utilized in this investigation included a laser scanned and a generically constructed CAD model of the target. It was found that the laser scanned CAD model produced more accurately calculated RCS results compared to the measured data than the generic CAD model. Therefore, if measured data is used for validation purposes, the numerical model of the target has to be a very accurate approximation of the measured target. This can be achieved by either laser scanning the physical target or by accurately manufacturing the target from the CAD model specifications. Consequently, the validation of the
asymptotic methods was conducted with the scanned CAD model of the target. The accuracy with which the RL-GO and SBR asymptotic CEM techniques calculated the RCS of the electrically large complex target was validated. This was done by comparing the simulated RCS results with measured data using RCS plots and ISAR images. Almost all of the simulated RCS data, generated with the various asymptotic methods, followed the same trend as the measurements and had excellent agreement over the ranges where the projected area of the aircraft was large. The accuracy also increased with frequency. Very poor RCS results were obtained when a curvilinear mesh model was simulated with multiple reflections using the RL-GO method in FEKO. However, the accuracy of the RCS results increased when this method was applied to a linearly meshed model. The accuracy of this method increased significantly, with both mesh types, when only one interaction was considered. These results were very similar to the PO results generated with the scanned CAD model. The SBR method as implemented in CST MWS produced accurate RCS results when rays were used and less accurate results when ray-tubes were used.

It was also shown that ISAR imaging provided a handy tool to examine the differences between the measured and simulated radar signatures. The simulations were performed on a computer with six 3.2 GHz processors and 64 GB RAM. It is clear from Table 1 that the SBR method with rays (CST 2016) was the most time efficient method, and RL-GO (FEKO 14.0.420-552) was the most time demanding. However the RL-GO method (FEKO) was the most memory efficient method whereas the SBR method with ray-tubes (CST) was the least.

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REFERENCES

A Novel UWB Monopole Antenna with Controllable Band-Notch Characteristics

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Abstract — A novel microstrip monopole antenna for Ultra Wide Band applications with switchable band-notch function is presented. For this purpose, elliptical radiator and a half circular shape ground plane are modified. Using these modifications, including a rectangular and an arc-shaped slots on ground plane and a complex form of slot, etched on the patch, new resonances are excited and hence bandwidth is enhanced. In addition, by adding one rectangular step to patch, wide fractional bandwidth of more than 124% (2.7-11.61 GHz), defined by 10 dB return loss is achieved, in following part effects of the rectangular step is investigated. The rejection of 3.01-3.9 GHz, WiMAX and 5.07-6 GHz, WLAN bands is achieved using small connections as switches across the circular slot and rectangular arm on the radiation patch in specific positions. The total size of antenna is only 21×26 mm². Parametric simulation of the proposed modifications and measurement results of the manufactured antenna are presented and discussed.

Index Terms — Frequency band-notched, microstrip-fed monopole antenna, switches, Ultra Wide Band (UWB).

I. INTRODUCTION

Due to rapid growth of Ultra Wide Band communication systems and their inherent properties such as low-spectral-density radiated power and positional for accommodating higher data rate [1], there is essential call for efficient communication devices to work in such environments. Special frequency band, 3.1 to 10.6 GHz, has allocated by FCC for unlicensed use of ultra-wide band devices [2]. Printed monopole antennas are potential candidates in emerging UWB applications because of their low cost and compact size and stable radiation properties. To avoid the electromagnetic interference between UWB systems and narrowband communication systems, such as Worldwide Interoperability for Microwave Access (WiMAX) operating at 3.4-3.69 GHz and the wireless local area network (WLAN) operating at 5.15-5.825 GHz, band-notched characteristic should be considered in UWB antenna design. For this purpose, recently, modified UWB monopole antennas with frequency band-notched function have been attempted. To get Reconfigurable capability, various electronic switches such as p-i-n diodes [3], radio frequency micro-electromechanical systems (RFMEMS) [4], and varactor [5] can be used. Extensive discussions of reconfigurable antenna, switches and their advantages were investigated in [6]. Also different shapes of the slots are used to obtain desired rejected bands [7-9]. In [10], using SRRs elements leads to triple band-notched characteristics. Parasitic strips with dual band notches in [11], band stop filter in [12], fractal structure [13] and DGS structure [14] are other methods used for band-notch characteristics.

In this letter, a new microstrip-fed monopole antenna with modified radiation patch and ground plane is suggested to provide UWB characteristics and band-notch function. Etching a rectangular and an arc shaped slot on the ground plane, leads to improvement of bandwidth. Additionally, a circular slot with three arms is employed on radiating patch to get much wider impedance bandwidth. Small connections as switches across the circular slot and one of arms on the patch, lead to desired reconfigurable frequency band-notches covering 3.01-3.9 GHz WiMAX and 5.07-6 GHz WLAN. Dimensions of designed antennas are small, also its structure has less complexity and better functionality. Additionally novelty in comparison to previously presented antennas is another specification of this design.

II. ANTENNA CONFIGURATION AND DESIGN

The configuration of proposed monopole antenna is illustrated in Fig. 1, which is fabricated on a FR4 substrate with the size of 21 (x-axis) × 26 (y-axis) × 1 mm³, relative dielectric constant of 4.4, and loss tangent of 0.018. The basic antenna structure is made up of a half circular shape ground plane, feed line and elliptical radiating patch. On the front surface of substrate, the radiiuses of elliptical patch are 10 mm and 8 mm.
respectively. On the other side of the substrate, ground plane has radius of R. The width of the microstrip feed line is fixed at $W_f = 2$ mm to obtain $50 \Omega$ characteristic impedance. The ground plane with a rectangular and an arc-shaped slot has substantial efficacy on controlling frequency response. In this case, the main parameter of these slots is $H_g$, which will be investigated in the following part. A circular slot with three arms is employed on the elliptical radiation patch to enhance the impedance bandwidth and provide notch function. One of these arms is placed on the feed line and by optimizing its length ($Y_f$), surface currents are dispersed in new paths, so notch function focuses on desired frequency bands. Furthermore, the rectangular step is added on the patch to achieve smooth transition between frequency bands and avoid unwanted notched bands as considered by parametric study in Fig. 2. The location of rectangular step, $K_n$, is critical parameter to control UWB bandwidth. Also $\alpha$ connects feed line to radiation patch with angle of 45 degrees. Optimal dimensions of desired antenna are as shown in Table 1.

![Geometry of the proposed microstrip monopole antenna](image1)

Fig. 1. Geometry of the proposed microstrip monopole antenna: (a) front view (including a microstrip-fed slotted patch) and (b) bottom view (including ground plane with slots).

![Simulated return loss characteristics](image2)

Fig. 2. Simulated return loss characteristics of the proposed monopole antenna with and without rectangular step.

### Table 1: Parameters of antenna (Unit: mm)

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<tr>
<td>$K_1$</td>
<td>3.2</td>
<td>$K_2$</td>
<td>4.2</td>
</tr>
<tr>
<td>$K_n$</td>
<td>19.4</td>
<td>$K_1$</td>
<td>3.2</td>
</tr>
</tbody>
</table>

### III. RESULTS AND DISCUSSION

#### A. Full band UWB monopole antenna

Ansoft simulation software high frequency structure simulator (HFSS) [15] is used for design and parametric analysis of antenna.

The optimized parameters are defined by changing selected parameter while fixing others. Figure 3 illustrates the structure of the various antennas used for simulation studies. Return loss characteristics for ordinary modified monopole antenna [Fig. 3 (a)], defected ground plane [Fig. 3 (b)], and the proposed antenna with slotted elliptical patch [Fig. 3 (c)], respectively are compared in Fig. 4. As shown in Fig. 4, slotted ground plane has an important effect on exciting new resonances and achieving different frequency responses. In this case, the new coupling paths between the modified patch and slotted ground plane can be obtained. Therefore the number of resonances, matching and bandwidth of antenna can be controlled. In this case, the covered bandwidth is from 2 to 8.35 GHz. To work in UWB frequency band, the simple elliptical patch is changed to slotted patch and in following, a tapered step is added to the patch. By this modification, it is found that good impedance bandwidth and matching is achieved at upper frequencies. Essential parameters for ultra wide band characteristics of proposed antenna are $H_g$, $R$, $r_1$, $r_2$, $K_n$, and $\alpha$. By carefully adjusting these parameters, ultra wide band operation is achieved. $K_n$ is a key parameter in controlling the resonances of antenna. As shown in Fig. 5 (a), while $K_n$ swaps form 16.4 mm to 19.4 mm, additional resonance will be added at 9.5 GHz but first and second resonances have almost fixed position. By selecting $K_n = 19.4$ mm, good matching in all frequency bands is realized. The other main parameter is $H_g$. Its effect on antenna performance is indicated in Fig. 5 (b).

By increasing $H_g$, the matching of high frequencies is considerably improved. In optimal value of $H_g$, frequency bands from 2.7 to 11.61 GHz are covered.
B. UWB monopole antenna with switchable frequency band-notch characteristics

UWB monopole antenna with two band-notch modes is introduced here by using proposed structure depicted in Fig. 1 and adding two slots across the circular slot and rectangular arm on radiation patch with connections used as switches. Positions of connections, $D1$ and $D2$, are adjusted appropriately to create desirable frequency notched bands. For the proposed structure, two operating states are investigated. At first, $D1$ is connected as a switch. By selecting $D1 = 8.3$ mm, first rejected band of 3.01-3.9 GHz, WiMAX is obtained. In second configuration, when other connection as a switch at $D2 = 2$ mm is attached, band-notch of 5.07-6 GHz WLAN is clearly seen. In this case, as shown in Fig. 6 (a) and Fig. 6 (b) simulated return loss curves with various values of $D1$ and $D2$ are optimized to reach desired notched bands. The phenomenon of switching between UWB and band-notch performances is clarified here by simulated current distributions on the radiation patch of proposed antenna according to the switching conditions. As shown in Fig. 7 (a), at 4.5 GHz, main part of surface current flows on the transmission line and dispersed by the means of rectangular slit, while around the circular slot current is small. The simulated current distributions at frequencies 3.5 and 5.5 GHz are illustrated in Figs. 7 (b) and (c). It can be observed that the current distributions mainly concentrate around the specific parts of circular slot. Impedance nearby feed-point changed markedly making considerable reflection at the desired rejected frequencies in three optimal designs. UWB antenna and two single band-notch antennas were built and tested. The photographs of fabricated prototypes are presented in Fig. 8. Simulated and measured reflection coefficients of selected designs are considered in Fig. 9. From this figure, it is clear that in all of designs, the simulated and measured results are in acceptable agreement. In first design, as indicated in Fig. 9 (a), fabricated antenna shows UWB performance from 2.8 to 12 GHz. In Fig. 9 (b), the results of second proposed antenna design with a connection on rectangular arm is shown. It reveals that measured rejected band from 3 to 4.1 GHz is obtained. Finally, Fig. 9 (c) illustrates the third design with a connection across circular slot. In this case, the antenna has measured notched frequency band from 5 to 6.2 GHz. The discrepancy between the measured and simulated values may be due to the errors of the manufactured antenna and the effects of the SMA port which is not considered in simulated results. Figure 10 indicates that gain of dual and single band-notched antenna is between 0 dB to 5 dB and has comprehensive level during frequency bands except for two notched bands. Figure 11 shows the measured and simulated patterns including the co and cross polarization in the H-plane (x-z plane) and E-plane (y-z plane). It is clear that radiation patterns in H-plane are nearly omni-directional in the four frequencies and by such results antenna behavior is alike to the usual printed monopole antennas.
Fig. 6. Simulated return loss characteristics of the proposed antenna with different values of: (a) D1 and (b) D2.

Fig. 7. Simulated surface current distributions on radiation patch: (a) UWB monopole antenna at 4.5 GHz, (b) single band-notch antenna with connected D1 at 3.5 GHz, and (c) single band-notch antenna with connected D2 at 5.5 GHz.

Fig. 8. Prototype antennas: (a) UWB monopole antenna, (b) single band-notch monopole antenna (WiMAX), and (c) single band-notch monopole antenna (WLAN).

Fig. 9. Measured and simulated return loss results of: (a) UWB monopole antenna, (b) single band-notch (WiMAX), and (c) single band-notch (WLAN).

Fig. 10. Measured antenna gain of the proposed antennas.
IV. CONCLUSION

This letter has presented a novel printed UWB monopole antenna with switchable band-notch characteristics supporting various wireless applications. It has been shown that using circular slots with three arms etched on patch can enhance bandwidth from 2.7 to 11.61 GHz. In addition, using defected ground plane by inserting two rectangular and arc-shaped slots can also improve input reflection coefficient. By embedding a pair of connections as switches in proper situations, across the slotted patch, two single stop-bands will be created, which exempt from interfaces with existing WiMAX and WLAN bands.

REFERENCES


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A Novel Compact Polarization Diversity Ultra-Wideband MIMO Antenna

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Abstract — A very compact modified simple structure Ultra-Wideband (UWB) antenna with a size of 18 mm by 30 mm is presented for polarization diversity applications. The antenna employs two orthogonal monopole antenna to achieve polarization diversity over the UWB. The antenna was fabricated to study the performance such as S-parameters, radiation pattern, radiation efficiency, peak gain, envelope correlation coefficient and group delay. The measured results demonstrated that the proposed antenna has not only UWB (147.96% impedance bandwidth) but also good isolation less than about -25 dB. Moreover, the system fidelity factor is sufficient for pulse transmission with average 89.6% and 85.3% for ports 1 and 2, respectively. Furthermore, a low envelope correlation coefficient of less than 0.001 occurred, too. All these features show that the proposed UWB MIMO antenna can meet the requirement of MIMO/diversity of communication applications well.

Index Terms — Microstrip feed, monopole antenna, polarization diversity, UWB.

I. INTRODUCTION

The rapid developments in modern wireless communication systems demand a high data rate, strong dependability and heftiness. Ultra-wideband (UWB) technique is one of the most important technologies in indoor communications in order to have benefits such as low susceptibility to multipath fading, reduced probability of detection and intercept, and potentially high data rates [1-7]. But similar to most of the wireless communication systems, UWB systems usually suffer from channel fading caused by multipath environment [1-7]. To solve this problem, Multiple-Input-Multiple-Output (MIMO) technology is developed to supply best coverage and to become better performance over multipath wireless channels by utilizing multiple antennas at the transmitter and receiver [5-9]. The main problem facing the implementation of MIMO technology is the limited space available at each end of the communication link. Saving this extra space may cause performance degradation; therefore, polarization diversity needs to be considered in true wireless channels. These advantages enable UWB antenna to change polarization diversity by its capability attractive for wireless body area networks (WBANs). An appropriate UWB-WBAN diversity antenna must have low mutual coupling, i.e., high isolation between its branches [10]. The higher isolation leads to better diversity performance and higher efficiency of each branch. Hitherto, various techniques to attain UWB diversity antennas have been investigated and reported, aimed at reducing the antenna size and increasing the isolation [1-7]. In [1], a uniplanar, UWB dual-polarized antenna embedded with narrowband reject filter is presented. A style of designing ground plane has resulted in an enhance antenna foot print to 58×58×1.524 mm3. Isolation between two ports is less than -15 dB. In [3, 4], by using a similar radiation patch, two type of UWB polarization diversity antenna in different large size and number in elements are provided (details is given in Table 1). In [5], a large size (50×50×1.524 mm3) CPW fed uniplanar antenna with frequency range from 2.76 to 10.75 GHz and a rejection performance in the frequency band 4.75-6.12 GHz, along with isolation better than 15 dB, is reported. In [11] and [12], two UWB tapered slot antennas (TSAs) and mutual coupling below 15 dB are developed. That design utilizes a spatial diversity technique and, to the authors’ knowledge, has the smallest size (27×47 mm3) among the recently designed UWB diversity antennas. It should be noted that although a printed cantor set fractal antenna using spatial diversity, proposed in [13], has a smaller size (25×48 mm2), its bandwidth is 80% of the UWB frequency defined range. In [7], a smaller UWB polarization antenna than reported works until the time of its release was worked. That is 52×27 mm2 in size, and isolation between two input ports is less than -22 dB. In this work, we present a low profile 18x30x1.6 mm3, small size polarization diversity antenna with covering impedance bandwidth from 2.97 to 19.86 GHz. This antenna with isolation less than about -25 dB between two ports and correlation coefficient less than -30 dB is a good choice for wireless systems which needs polarization diversity application. The proposed antenna has an area of 540 mm2, which is significantly less than the recently published UWB polarization diversity antenna, as summarized in Table 1. Compared to other
similar types of antennas, the proposed antenna displays an impedance bandwidth which is significantly larger and shows no reduction in the gain performance as well as having better other results.

Table 1: Comparison of the proposed antenna with same works (IBW is Impedance Bandwidth, Sij is Isolation, ECC is Envelope Correlation Coefficient, FF is Fidelity Factor, GD is Group Delay, PW is Proposed Work, and RE is Radiation Efficiency)

<table>
<thead>
<tr>
<th>Ref.</th>
<th>Size (mm)</th>
<th>IBW (GHz)</th>
<th>Sij (dB)</th>
<th>ECC</th>
<th>FF (%)</th>
<th>Gain (dB)</th>
<th>GD (ns)</th>
<th>RE (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>[1]</td>
<td>58×58</td>
<td>8.2 GHz</td>
<td>-14</td>
<td>0.025</td>
<td>80</td>
<td>2.2</td>
<td>1</td>
<td>85</td>
</tr>
<tr>
<td>[3]</td>
<td>48×48</td>
<td>8.7 GHz</td>
<td>-15</td>
<td>0.04</td>
<td>--</td>
<td>--4.3</td>
<td>--</td>
<td>80</td>
</tr>
<tr>
<td>[4]</td>
<td>65×65</td>
<td>8.25 GHz</td>
<td>-40</td>
<td>--</td>
<td>--</td>
<td>--6.5</td>
<td>--</td>
<td>--</td>
</tr>
<tr>
<td>[5]</td>
<td>50×50</td>
<td>7.99 GHz</td>
<td>-15</td>
<td>0.025</td>
<td>95</td>
<td>-5.5</td>
<td>1</td>
<td>75</td>
</tr>
<tr>
<td>[6]</td>
<td>64×64</td>
<td>8 GHz</td>
<td>-40</td>
<td>0.006</td>
<td>--</td>
<td>-6.5</td>
<td>1</td>
<td>75</td>
</tr>
<tr>
<td>[7]</td>
<td>27×52</td>
<td>8.75 GHz</td>
<td>-22</td>
<td>0.01</td>
<td>85</td>
<td>--</td>
<td>--</td>
<td>--</td>
</tr>
<tr>
<td>[8]</td>
<td>40×40</td>
<td>8 GHz</td>
<td>-20</td>
<td>--</td>
<td>--</td>
<td>--5</td>
<td>--</td>
<td>85</td>
</tr>
<tr>
<td>[9]</td>
<td>38.5×38.5</td>
<td>8.72 GHz</td>
<td>-15</td>
<td>0.02</td>
<td>--</td>
<td>7.5</td>
<td>--</td>
<td>50</td>
</tr>
<tr>
<td>[16]</td>
<td>45×50</td>
<td>8.2 GHz</td>
<td>-25</td>
<td>0.02</td>
<td>76</td>
<td>4</td>
<td>1</td>
<td>85</td>
</tr>
<tr>
<td>[17]</td>
<td>30×60</td>
<td>7.5 GHz</td>
<td>-20</td>
<td>0.01</td>
<td>--</td>
<td>4.2</td>
<td>--</td>
<td>80</td>
</tr>
<tr>
<td>[22]</td>
<td>~90×90</td>
<td>9.4 GHz</td>
<td>-20</td>
<td>--</td>
<td>--</td>
<td>--5</td>
<td>--</td>
<td>--</td>
</tr>
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</table>

II. ANTENNA DESIGN AND CONFIGURATION

Figure 1 displays the geometry of the proposed antenna. It includes two similar monopoles that are perpendicular to each other and printed on FR4 substrate with thickness of 1.6 mm, relative permittivity of (εr = 4.4 and loss tangent of (tanδ) = 0.02. Spacing between two monopole antennas (center to center) is 12 mm. Each antenna is fed by a width of 2 mm microstrip line in order to attain 50Ω input impedance.

The patch of the antenna consists of a Trapezium- and a rectangular-shape which is united together. The ground of antenna comprises a rectangular and two symmetrical L-shape slot inside it. Details of other dimension are given in Table 2. Figure 2 demonstrates the structure of the various antennas employed for simulation studies. S11 characteristics for ordinary square monopole antenna [Fig. 2 (step 1)], the antenna with an improved patch [Fig 2. (step 2)] and the proposed antenna by cutting ground [Fig 2 (step 3)] structures are compared in Fig. 3. As shown in Fig. 3, by using the modified radiating patch and two L-shape slots in defected ground inserted on the other side of substrate, additional third and fourth resonances are excited respectively, and hence, the bandwidth is increased. As exposed in Fig. 3, in the offered antenna configuration, the ordinary square monopole can provide the fundamental and next higher resonant radiation band at 4 and 7.9 GHz, respectively, in the absence of two L-shaped slots and without modifying the edges of the patch. The upper frequency bandwidth is significantly affected by using the radiating patch because by improving the edge of the patch, surface current which is focused in the edge of the ordinary square patch (as seen in Fig. 4 (a)) is eliminated and, therefore, surface current spreads in the total surface of patch conductor (see Fig. 4 (b)). By inserting two L-shaped slots in ground plane, the antenna bandwidth increases. The two L-shaped slots prevent the spreading of power in microstrip feed line on the ground conductive surface and, also, causes an increase in the surface current rotation in ground conductive (see Fig. 4 (c)).

![Fig. 1. Structure and dimension of proposed antenna.](image-url)

Table 2: Parameters dimension

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wf</td>
<td>2 mm</td>
<td>W1</td>
<td>5 mm</td>
</tr>
<tr>
<td>Lf</td>
<td>7 mm</td>
<td>W2</td>
<td>10 mm</td>
</tr>
<tr>
<td>Ls1</td>
<td>3 mm</td>
<td>g</td>
<td>0.8 mm</td>
</tr>
<tr>
<td>Ls2</td>
<td>2.5 mm</td>
<td>h</td>
<td>1.6 mm</td>
</tr>
<tr>
<td>Lp</td>
<td>8 mm</td>
<td>Wsub</td>
<td>12 mm</td>
</tr>
<tr>
<td>Wp</td>
<td>2.5 mm</td>
<td>Lsub</td>
<td>17 mm</td>
</tr>
<tr>
<td>Ws</td>
<td>1 mm</td>
<td>Lg</td>
<td>3.8 mm</td>
</tr>
</tbody>
</table>
III. STUDY OF DGS EFFECT AT TDR

In order to comprehend defected ground structure effect in antenna performance Figs. 5 (a) and (b) are displayed. In order to calculate the TDR results for the proposed equivalent circuits, the impedance of these circuits in Laplace domain can be represented as in Equation (1):

$$Z_{DGS} = \frac{Ls + R}{LCs^2 + R + 1}$$  \hspace{2cm} (1)

Assuming that the characteristic impedance of the microstrip line is $Z_0$, we can write the reflection coefficient through a defected structure as in Equation (2), which is observed at the source end, i.e., port 1,

$$\Gamma_z(s) = \frac{Z(s)}{Z(s) + 2Z_0}$$  \hspace{2cm} (2)

Therefore, the reflected waveform for the proposed DGS can be written as:

$$\Gamma_{DGS}(s) = \frac{Ls + R}{2Z_0LCs^2 + (Z_0RC + L)s + R + 2Z_0}$$  \hspace{2cm} (3)

A step voltage source with rise time $\tau_r$ and amplitude $V_0$, can be expressed as in [18-21],

$$V_{in}(s) = \frac{V_0}{2\tau_r s^2} \left(1 - e^{-\tau_r s}\right).$$  \hspace{2cm} (4)

Therefore, the reflected waveform in Laplace domain can be written as:

$$V_{TDR}(s) = V_{in}(s)\Gamma_{DGS}(s).$$  \hspace{2cm} (5)

In TDR measurements, the impedance follows as:

$$Z_{TDR} = \frac{Z_0(V_{in}(t) + V_{TDR}(t))}{V_{in}(t) - V_{TDR}(t)}.$$  \hspace{2cm} (6)

In which $Z_o$ is the characteristic impedance of the transmission line at the terminal.

![Fig. 5. (a) Geometry of the proposed DGS, and (b) equivalent circuit model.](image)

The computed $R$, $L$ and $C$ of equivalent are $1.41\Omega$, $0.72nH$ and $16.01pF$, respectively. In additionally, as mentioned with attention to LC circuit in equivalent circuit causes to creation of resonance in antenna performance.

IV. RESULT AND DISCUSSION

The proposed antenna was simulated by High Frequency Structure Simulator (HFSS) ver. 14, and then was optimized since the validation of results was fabricated and measured in frequency- and time-domain. In Fig. 6 (a) simulation results of insertion and isolation of two ports is indicated. As shown in this figure, simulated $S_{11}<-10$ dB covered a frequency range from 2.98 to 20 GHz, and in this region of bandwidth, simulated $S_{21}$ is less than about -25 dB. Scattering parameters of antenna was measured using Agilent EM 8722ES vector network analyzer. Measured results of $S_{11}$ and $S_{12}$ are...
displayed in Fig. 6 (b). By comparing simulation and measured scattering results, it can be concluded that there is good matching between them in the expanding region. Measured results indicate that the antenna supplies an impedance bandwidth (S11&$S_{22}\leq-10$ dB) from 2.97 to 19.86 GHz, and it can also be realized that the measured port isolations ($S_{21} & S_{12}$) are less than about -25 dB throughout the band. Thus, the bandwidth prerequisite for UWB applications is realized. Due to the effects of manufacturing tolerance, imperfect solder joints of the SMA connector to the feed-line and measurement environment, measured port is slightly worse than the simulation at frequencies from 3 to 11 GHz. Figure 7 depicts measured radiation patterns at 3, 6, 10, 14, and 19 GHz when port 2 is excited, while port 1 is terminated with a 50Ω load, and vice versa.

![Fig. 6. Comparison between simulated and measured S11, S22 and S21: (a) Simulated and (b) measured.](image)

![Fig. 7. Depicts measured radiation patterns at 3, 6, 10, 14 and 19 GHz when port 2 is excited: (a) 3 GHz, (b) 6 GHz, (c) 10 GHz, (d) 14 GHz, and (e) 19 GHz.](image)

Figure 8 illustrates the simulated electric field distribution at 4, 8, and 12 GHz of the diversity antenna when two ports are excited respectively at different frequencies. It can be observed that the electric field is X-direction when port 1 is excited while the electric field shifts to Y-direction when port 2 is excited, which is consistent with the aforementioned current analysis. However, the polarization worsens at high frequency, which is attributed to the complicated current distribution on the radiator [8]. Gains and radiation efficiencies of the antennas for port 1 and 2 are measured. Figure 9 shows the measured gains of two antenna elements within the UWB band that are larger than 3.8 dB and have a peak gain of 4.7 dBi.

![Fig. 8. The simulated far field electric field distribution at 4, 8, and 12 GHz of the diversity antenna when two ports are excited: (a) port 1 directed in X-direction, and (b) port 2 directed in Y-direction.](image)
It is essential to evaluate the Envelope Correlation Coefficient (ECC) since an ECC greater than 0.05 (less than -13 dB) can typically degrade the diversity performance. The ECC of the proposed antenna is also calculated [10, 23] using:

$$\rho_e = \frac{|S_{11}^2 + S_{21}^2|}{(1-|S_{11}|^2)(1-|S_{21}|^2)},$$  \hspace{1cm} (7)

and is plotted in Fig. 10. The measurement and simulated values of ECC remain low throughout the UWB spectrum, which indicates that the proposed antenna is a good candidate for wireless communication systems with polarization diversity.

In a UWB system, the antenna needs to possess a high level of pulse-handling capability to handle high-frequency impulses. Hence, the time-domain properties are equally as important as frequency domain [1]. The group delay of the antenna is measured by exciting two identical antennas kept in the far field with face-to-face orientation (when one of the ports is excited, another port is terminated with 50 load, and vice versa). It is clear from Fig. 11 that the antenna displays a group delay that remains almost constant with variations less than 1 ns.

The HFSS default Gaussian pulse with spectrum covering from 2 GHz to 20 GHz band was employed as the input signal, as it completely complies with the FCC indoor and outdoor power masks [15]. Figure 12 displays the antenna impulse reply for the two measured directions.
To compute the level of distortion, the system fidelity factor has been considered as in [14], and results are specified in Table 3. The measured average system fidelity factors, for the considered directions, of ports 1 and 2 are 88.2% and 84.3%, respectively, which shows that the level of signal distortion is quite suitable for UWB signals transmission [7]. The footprint of fabricated proposed compact polarization diversity MIMO antenna is illustrated in Fig. 13.

Table 3: Measured of system fidelity factor

<table>
<thead>
<tr>
<th>Port 1</th>
<th>φ=0</th>
<th>89.6%</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>φ=90</td>
<td>86.8%</td>
</tr>
<tr>
<td>Port 2</td>
<td>φ=0</td>
<td>85.3%</td>
</tr>
<tr>
<td></td>
<td>φ=90</td>
<td>83.2%</td>
</tr>
</tbody>
</table>

Fig. 13. Photograph of fabricated antenna.

V. CONCLUSION

An UWB MIMO antenna for polarization diversity applications has been proposed. The antenna prototype (with a size of 18x30 mm²) in compared with same articles [1-9] have very compacted size and better results. Results show that the proposed antenna achieves an impedance bandwidth of larger than 147.96% (2.97 to 19.86 GHz). A high isolation between two ports has been achieved. Besides, low envelope correlation coefficient less than 0.001 was obtained. In the future, the proposed diversity UWB antenna mentioned above can be a promising candidate for wireless communication systems where a challenge such as multipath fading is a major concerns.

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Saeid Karamzadeh received his M.S. and Ph.D. degrees in Department of Communication Systems, Satellite Communication & Remote Sensing program at Istanbul Technical University in 2013 and 2015 respectively. He won the most successful Ph.D. thesis award of Istanbul Technical University. Currently, he is an Assistant Professor in the Istanbul Aydin University, Department of Electrical and Electronics Engineering. He is also with Application & Research Center for Advanced Studies in the Istanbul Aydin University, Turkey. His research interests include remote sensing, radar, microwave, and Antenna design.
Dual-Band Wide-Angle Circularly-Polarized Microstrip Antenna by Ferrite Ring Inserted in Its Cavity Domain

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University of Alberta, Alberta, Canada

Abstract — In this paper coaxially-fed circular microstrip patch antenna with ferrite ring in its cavity domain is presented in order to obtain dual-band circularly-polarized antenna in X-band having wide angle axial ratio in both bands. A mode matching approach is used to see the effects of each mode on input impedance of the antenna and is validated numerically by finite element method. The theoretical calculations for input impedance are in good agreement with full-wave simulation. The scattering and radiation parameters of the antenna are investigated. The antenna patch radius and height are 8 and 1 mm, respectively. The ferrite ring was made of yttrium iron garnet (YIG) and the substrate of antenna is Rogers RT5880. In the first band the antenna has 7 dB gain and the ratio of Copol/Xpol is about 24 dB and in the second band has 5 dB gain and the XPD, i.e., the ratio of Copol to Xpol is about 20 dB.

Index Terms — Dual-band circularly-polarized antenna, microstrip antennas, mode-matching, wide-angle antenna.

I. INTRODUCTION

Circular polarization (CP) is extensively used in wireless and satellite communications. In many papers, ferrite substrate was used to generate CP [1]-[2]. In [3], circularly polarized microstrip antenna based on the unidirectional resonant modes of a ferrite disk has been introduced which produce wide angle circular polarization for GPS application. In [4], circularly polarized microstrip antenna has been obtained by small ferrite disks inserted in its cavity domain. In order to have single-feed dual-band CP antenna various configurations have been investigated for GPS application [5]-[6]. A compact CP dual-band antenna was successfully designed for Meteosat satellite in L and X communication bands [7]. In [8], a compact dual-band CP multilayer microstrip antenna using LTCC technology has been proposed and implemented, due to the stacked-patch structure and inserted slits, the designed antenna has a small volume compared to the conventional dual-band CP antennas. A crossed asymmetric dipole antenna over a dual-band AMC surface has been introduced in [9] in which, the proposed antenna yields a low profile, good impedance matching, good CP radiation, and an improved 3-dB AR bandwidth at both operating bands. Sun et al. have introduced a dual-feed stacked annular-ring patch antenna which is dual-band, dual-layer; and is excited by two orthogonal H-shaped slots, fed by a 3-dB hybrid [10]. In [4], it is shown that dual-band CP antennas can be obtained by insertion of two or more ferrite disks in the cavity region of the antenna along with appropriate optimization of the bias magnetic field.

In this letter, a new configuration to achieve single-feed dual-band CP microstrip antenna is presented. Antenna has been excited via coaxial port; in addition, a ferrite ring is inserted in antenna cavity domain in order to produce circular polarization.

This paper is organized as follows. Section II introduces the structure of complete antenna. The theoretical analysis of input impedance of antenna is described in Section III and the results are validated by full-wave simulations and discussed. In Section IV radiation characteristics of antenna are simulated with CST Studio and discussed.

II. ANTENNA STRUCTURE

Figure 1 (a) shows the proposed antenna, which consists of a ferrite ring inserted in the cavity domain of the substrate. The ferrite disk is magnetized normal to the ground plane by a dc bias magnetic field $H_0$, which can be provided by a permanent magnet placed underneath the ground plane. The substrate of antenna is made of RT5880, permeability ($\mu$) of the substrate is equal to that of the air, i.e., $\mu = \mu_0$, and has relative permittivity 2.2 and its loss tangent $\tan(\delta)$ is about 0.0009. The cavity domain of antenna has four regions as it can be seen from Fig. 1 (b). Region I is defined by
For - $r < a$, which is from the center of the patch to the current probe that is fed at $r = a$. Region II is defined by $a < r < b$. This region is between feed probe and ferrite ring. Region III is defined by $b < r < c$, which contains ferrite ring, and finally, region IV is defined by $c < r < d$, which is between ferrite ring and edge of the patch. The ferrite ring with thickness 1 mm and height 1 mm is inserted in the cavity domain of patch antenna with radius 8 mm, and its substrate height is 1 mm.

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**III. INPUT IMPEDANCE**

To determine the input impedance of the antenna, it is necessary to find the field solution beneath the circular patch. In general, these solutions take the form of a cylindrical mode expansion, with each mode being determined by arbitrary constants. To find all of these constants, additional boundary conditions are required, which are obtained by considering the wall admittances. The electric and magnetic field solution in each region can be written as following, in which for simplification purposes, the variations of the fields in $z$ direction are ignored:

\[ (r, \phi) = \sum_n^{\infty} -j \omega A_n e^{im \phi} J_n(kr), \]

\[ H_\phi^{\prime} (r, \phi) = \sum_n^{\infty} -j \omega A_n \frac{1}{\mu_0} e^{im \phi} \frac{\partial}{\partial r} J_n(kr), \]

\[ E_z^{\prime} (r, \phi) = \sum_n^{\infty} -j \omega e^{im \phi} \left( B_n J_n(kr) + C_n Y_n(kr) \right), \]

\[ H_\phi^{\prime} (r, \phi) = \sum_n^{\infty} -j \omega e^{im \phi} \left( B_n \frac{\partial}{\partial r} J_n(kr) + C_n \frac{\partial}{\partial r} Y_n(kr) \right), \] where $J_n$ and $Y_n$ are Bessel function of the first kind and second kind, respectively. In region I, II and IV, we have ordinary substrate and $k = k_0 \sqrt{\varepsilon_r}$ in which, $k_0$ is

### Table 1: Ferrite material properties

<table>
<thead>
<tr>
<th>$H_0$</th>
<th>$\Delta H$</th>
<th>$4\pi M_s$</th>
<th>$\alpha$</th>
</tr>
</thead>
<tbody>
<tr>
<td>600 (Oe)</td>
<td>20 (Oe)</td>
<td>1780 (Gauss)</td>
<td>15</td>
</tr>
</tbody>
</table>
In region III, due to the presence of the ferrite material electric and magnetic fields are written as following:

$$E_n^{III}(r,\phi) = \sum_j -j\omega e^{j\phi}(D_jJ_n(k_jr) + E_nY_j(k_jr)), \quad (8)$$

$$H_n^{III}(r,\phi) = \sum_j -\frac{j}{\mu_0} e^{j\phi} \left( \mu_r \frac{\partial}{\partial r} E_n^{III}(r,\phi) + n\mu_r E_n^{III}(r,\phi) \right), \quad (9)$$

in which $k_j = k_0\sqrt{\varepsilon_r \mu_r}$. In region IV, we have the next boundary condition can then result to:

$$E_n^{IV}(r,\phi) = \sum_j -j\omega e^{j\phi}(F_jJ_n(k_jr) + G_nY_n(k_jr)), \quad (10)$$

$$H_n^{IV}(r,\phi) = \sum_j -\frac{1}{\mu_0} e^{j\phi} \left( F_j \frac{\partial}{\partial r} J_n(k_jr) + G_n \frac{\partial}{\partial r} Y_n(k_jr) \right), \quad (11)$$

In order to take the feed probe into account, neglecting the variation of the probe current in the $z$ -direction, an infinitely thin electric current line source carrying a constant current $I_0$ is assumed. The current density of the line source is:

$$J = \frac{\partial}{\partial z} J_z = \frac{\partial}{\partial z} \delta(r-a)\delta(\phi).$$

Boundary conditions on the tangential components of the electric and magnetic fields are applied as following:

$$E_n^I(a,\phi) = E_n^{III}(a,\phi), \quad (12)$$

$$H_n^I(a,\phi) = H_n^{IV}(a,\phi) = J_z, \quad (13)$$

$$E_n^I(b,\phi) = E_n^{IV}(b,\phi), \quad (14)$$

$$H_n^I(b,\phi) = H_n^{IV}(b,\phi), \quad (15)$$

$$E_n^I(c,\phi) = E_n^{IV}(c,\phi), \quad (16)$$

$$H_n^I(c,\phi) = H_n^{IV}(c,\phi). \quad (17)$$

By considering wall admittance on the side wall of the microstrip antenna, the next boundary condition can be written as following:

$$H_n^{IV}(d,\phi) = -y_x E_n^{IV}(d,\phi). \quad (18)$$

By using Equations (11) through (17), the constants $A_n$, $B_n$, $C_n$, $D_n$, $E_n$, $F_n$, and $G_n$ will be evaluated. The input impedance can be written as following:

$$Z_n = -\frac{1}{I_0} \int_0^h E_n(r = a,\phi = 0)\,dz. \quad (19)$$

In this paper the wall admittance, described in [11] is used, this wall admittance $y_x$ fix the ratio between the $z$-directed electric field and the $\phi$-directed magnetic field for each mode. The antenna parameters are considered as Table 2.

**Table 2: Antenna parameters**

<table>
<thead>
<tr>
<th>$a$</th>
<th>$b$</th>
<th>$c$</th>
<th>$d$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.5 mm</td>
<td>4 mm</td>
<td>5 mm</td>
<td>8 mm</td>
</tr>
</tbody>
</table>

In the absence of ferrite ring, the superposition of two azimuthally travelling waves in opposite direction, have the same amplitude and resonance frequency, results in a standing wave behavior of the electric field. In order to show the effect of ferrite ring on the separation of resonance frequency of the right-handed and left-handed azimuthal modes, input impedance of each mode is individually plotted in Fig. 3. As it can be seen, modes of $n = \pm 1$ do not have the same resonance frequency. These two modes have the most influence on the input impedance, and the other modes have a negligible effect on the real part of input impedance but increase the imaginary part of the input impedance.

Figures 4 and 5 show the comparison between our theoretical results for the input impedance and return loss, and those obtained by CST studio full wave simulator. For each calculation, we have considered 5 modes, the modes having order of greater than 5 were found to have insignificant effect on the calculated input impedance. It is seen that the mode matching results are close to that obtained by the CST studio simulation. The antenna has impedance bandwidth between (5.26 GHz-5.34 GHz) or 1.5% and (6 GHz-6.2 GHz) or 1.7% in first and second band, respectively.
The proposed dual-band CP antenna can be designed by adjusting the thickness of ferrite ring and by varying the dc bias field $H_0$ of ferrite.

Figure 6 shows the effect of ring thickness on the first and second band resonance frequency. By increasing the ring thickness, both resonance frequencies decrease which is due to the increasing of the effective permittivity and permeability of the substrate. Also, the separation between two resonance frequencies increases because the ferrite region which has anisotropic behavior is increased.

Fig. 4. Comparison between mode matching method and CST studio results: (a) real part and (b) imaginary part.

Fig. 5. Comparison of return loss between mode matching method and CST studio results.

Figure 7 shows the effect of dc bias field $H_0$ on the resonance frequency. As it can be seen, by increasing the bias field, the resonance frequencies, and especially the second can be controlled.

Fig. 6. Full-wave simulation result of the return loss against the ring thickness. The other design parameters are the same as in Fig. 4.

IV. RADIATION PROPERTIES

In order to examine radiation properties of the antenna, we consider a structure whose patch and ground plane are made of copper and having thickness of 50 microns. The ground dimensions in full wave simulation are considered $60 \times 60 \text{ mm}^2$.

Figure 8 shows the simulation results of axial ratio of the antenna on broadside direction versus frequency. As it can be seen, 3 dB axial ratio at first and second band is between (5.06 GHz-5.42 GHz) or 6.87% and (6.04 GHz-6.27 GHz) or 3.74%, respectively. The axial ratio bandwidth is wider than the impedance bandwidth which is given in Fig. 5. In Fig. 9, simulated axial ratio of the proposed antenna versus $\theta$ at the first and second resonance frequencies are shown, the wide angle behavior of the antenna can be seen in this figure.

In Fig. 10, the gain of the antenna as a function of frequency is shown, the antenna has 7 dB gain in first band and 5 dB gain in second band.

In Fig. 11, simulated radiation patterns for RHCP and LHCP at first and second resonance frequency in the XOZ plane ($\phi = 0$) and YOZ ($\phi = 90$) plane are shown.

Fig. 7. Full-wave simulation result of the return loss against the magnetic bias field. The other design parameters are the same as in Fig. 4.

Fig. 8. The simulated broadside axial ratio versus frequency.
Fig. 9. Simulated axial ratio of the proposed antenna versus $\theta$: (a) 5.3 GHz and (b) 6.16 GHz.

Fig. 10. The simulated broadside gain versus frequency.

It can be observed that the antenna has LHCP polarization in the first band and RHCP polarization in the second band. The Co-pol/Xpol is about 24 dB and 20 dB in the first and second bands, respectively. It is noticeable that the state of polarization can be switched by reversing the direction of the DC magnetic bias field. The efficiency of the antenna in first and second bands are 90% and 60%, respectively. The decrease in efficiency of the second band is due to the increase in ferrite loss. In Fig. 12, the loss of each part the antenna is plotted as a function of frequency. Here, the total input power in full-wave simulation is 500 mW. As it can be seen, the loss of ferrite ring is more than other losses and it plays the major role in antenna efficiency.

Fig. 11. Simulated radiation patterns for RHCP and LHCP at 5.3 GHz and 6.16 GHz in the XOZ plane ($\phi = 0$) and YOZ ($\phi = 90^\circ$) plane: (a) 5.3 GHz and (b) 6.16 GHz.

Fig. 12. Loss in each part of the antenna (total input power is 500 [mW]).
**V. CONCLUSION**

A new single-layer single-feed dual-band CP antenna with wide-angle axial ratio in both frequency bands by inserting a ferrite ring in cavity domain has been proposed. This antenna has 6.87% axial ratio bandwidth, and 1.5% impedance bandwidth in the first band. It also has 3.74% axial ratio bandwidth and 1.7% impedance bandwidth in the second band and can be used as a frequency tunable antenna. Proposed structure is compact, easy to design and fabricate, and does not require a complicated feeding network. Therefore, it could be a good candidate for realizing wide-angle dual-band CP antennas.

**REFERENCES**


Computationally Efficient Technique for Wide-Band Analysis of Grid-Like Spatial Shields for Protection Against LEMP Effects

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Abstract — This paper introduces a heterogeneous CPU+GPU co-processing implementation of the method of moments (MoM) for broadband full-wave electromagnetic analysis of grid-like spatial shields for protecting structures against LEMP effects. Broadband capacity of the approach is achieved through supporting MoM by adaptive frequency sampling and implicit rational interpolation of the observed quantity via Stoer-Bulirsch algorithm. The overall application performance is increased by hardware acceleration, i.e., by employing CPU+GPU co-processing. Sample numerical results for a lightning protection system directly hit by lightning show that reliable rational interpolation can be done at substantially reduced computational effort compared to that of conventional uniform sampling, and the CPU+GPU co-processing offers additional noticeable speedup over the CPU single-thread implementation of the method.

Index Terms — CPU+GPU co-processing, grid-like shield, lightning protection system, method of moments, rational interpolation, Stoer-Bulirsch algorithm.

I. INTRODUCTION
Wire meshes in the form of spatial grid-like structures are widely used as lightning protection systems (LPS) designed to reduce aggressive high-intensity electromagnetic (EM) effects caused by lightning strikes. For effective design of LPS, prediction of its response to lightning-induced electromagnetic excitation is of vital importance. Therefore, a considerable research effort has been devoted over the last years to the development of accurate and efficient techniques for EM analysis of complex LPSs. For spatial grid-like structures composed of arbitrarily arranged conductors, perhaps the best choice is the full-wave method of moments (MoM) formulated in the frequency domain (FD) [1]. When a wideband response of a structure is required, the investigation is usually carried out by point-by-point frequency swept computations, i.e., evaluation of samples of the required physical observable over a predefined set of uniformly spaced frequency nodes. The approach is computationally inefficient, since EM simulation must be performed repeatedly at many frequencies resulting in that the computation time can be unacceptably long for complex resonant structures. Among available approaches aimed at reducing the number of EM simulations needed for reconstruction of the system response, and thus, minimizing the overall processing time is the rational-function interpolation approach based upon the assumption that the system response can be represented by a rational polynomial [2]. The approach usually involves adaptive procedures for selecting the interpolation nodes and the rational interpolant order. In this study, we employ an adaptive frequency sampling (AFS) technique based upon interval halving (bisection) in combination with the rational interpolation implemented through Stoer-Bulirsch (SB) algorithm [3]. The details of the formulation are given in [4, 5].

Till the end of Pentium IV era, the possibility of MoM-based wide-band simulation of LPS structures on PC-based workstations was seriously limited. For example, the runtime needed for a wide-band simulation from 1 kHz to 20 MHz of a single-layer grid-like LPS type 1 (10 m × 10 m × 10 m) [6] discretized into 2224 wire segments was about one week [7]. The situation has changed dramatically with the introduction, about 2006, of powerful multi-core CPU technologies and the unified graphics and computing Graphics Processing Unit (GPU) architecture known as Nvidia CUDA (Compute Unified Device Architecture). Multi-core processors and CUDA-enabled GPUs offer an inexpensive massively parallel programmable hardware platform very attractive for use in scientific computing. It is now well known that by extending a traditional CPU-based computation model through adoption of the General-Purpose computing on GPU (GPGPU) paradigm, the performance of EM simulations can be remarkably increased.

In this paper, a CUDA-enabled heterogeneous CPU+GPU co-processing implementation of the method of moments supported by AFS and implicit rational interpolation for electromagnetic simulation of grid-like lightning shields over a wide frequency band is outlined.
The approach employs the technique described in [8] for
mapping CPU sequential MoM procedures to parallel
GPU platform. For consistence of presentation, we
briefly summarize partial concepts of the overall
approach including AFS-SB algorithm and CUDA-
based CPU+GPU implementation of the relevant
computer program. The potential of the approach is
demonstrated by a numerical example involving grid-
like LPS under direct strike.

The key components of a hardware platform engaged
in this study were the Intel Core i7-3820 Quad-Core
Processor and GeForce GTX 680 graphics card. Software
tools included Intel Fortran, PGI Fortran, CULA and
Intel MKL libraries. The overall approach constitutes
an example of the integration of the advanced computa-
tional electromagnetics technique with modern architec-
ture of a rather typical low-cost PC-style workstation
for the purpose of increasing efficiency of the
application-oriented EM simulator.

II. METHOD

A. Matrix approximant to the integral equation

The approach outlined in this paper adopts (for
wires) the frequency-domain mixed-potential electric
field integral equation (EFIE) formulation developed in
[9] for analyzing an arbitrary configuration of conducting
bodies and wires. For the sake of completeness, the
formulation is briefly outlined here.

For a wire residing in a simple medium \((\varepsilon, \mu)\) and
illuminated by an incident time-harmonic \((\exp (j\omega t))\)
EM field \((E^i, H^i)\), the EFIE for the total axial current
\(I(l)\) excited on the wire can be written as [9]:

\[
(j\omega A + V\phi)I = I_i E^i,
\]

with conventional notation \(A\) and \(\phi\) employed for the
magnetic vector potential and electric scalar potential,
respectively, and \(I_i\) denoting the unit vector locally
parallel to the wire axis. For the wire approximated by a
series of broken line segments, the unknown current is
expanded as a linear combination of one-dimensional
(triangle) RWG-type functions:

\[
I(l) \equiv \sum_{n=1}^{N} I_n T_n(l),
\]

where

\[
T_n(l) = \begin{cases} 
1_n^+ (l - l_{n-1}) / \Delta_n^+ & \text{if } l_{n-1} \leq l \leq l_n, \\
1_n^-(l_{n+1} - l) / \Delta_n^- & \text{if } l_n \leq l \leq l_{n+1}, \\
0 & \text{otherwise,}
\end{cases}
\]

and

\[
\Delta_n^+ = |r_n - r_{n-1}| \quad \text{and} \quad \Delta_n^- = |r_{n+1} - r_n|.
\]

with \(l\) and \(r_i\) denoting the arc length along the wire axis
and a position vector of the \(i\)-th point subdividing the
wire into segments, respectively. The EFIE-MoM
procedure leads to the matrix equation:

\[
Z(f)I(f) = V(f),
\]

in which \(Z_{NM}\) denotes the MoM-generated system
matrix with elements \((m, n = 1, 2, \ldots, N)\):

\[
Z_{mn} = j\omega \left[ A_n(r_{m-1/2}) \cdot (r_m - r_{m-1/2}) + A_n(r_{m+1/2}) \cdot (r_{m+1} - r_m) \right] + \phi_n(r_{m+1/2}) - \phi_n(r_{m-1/2}),
\]

where \(A_n(r)\) and \(\phi_n(r)\) denote \(A\) and \(\phi\) values from \(n\-
th basis function at the observation point specified by \(r\),
respectively, with

\[
r_{m+1/2} = \frac{r_{m-1} + r_m}{2}, \quad r_{m+1} = \frac{r_m + r_{m+1}}{2}.
\]

The unknown current expansion coefficients constitute a
column vector \(I_{N \times 1}\), and the elements of a column vector
\(V_{N \times 1}\) representing the excitation are given by \((m = 1, 2, \ldots, N)\):

\[
V_m = E^i(r_{m-1/2}) \cdot (r_m - r_{m-1/2}) + E^i(r_{m+1/2}) \cdot (r_{m+1} - r_{m}).
\]

The complex valued dense impedance matrix \(Z\) is
frequency, \(f (= \omega / 2\pi)\), dependent and, therefore, the
matrix equation must be set up and then solved repeatedly
for each individual frequency within a set of discrete
frequencies of interest. The Equation (5) can be solved by
standard methods of linear algebra. In this paper, only the
LU decomposition is considered in GPU context, since the
technique is widely used in MoM simulations.

B. Adaptive frequency sampling

An adaptive frequency sampling scheme employed in
this study consists in performing repetitive bisection
of each of initially chosen frequency intervals until a
specified convergence criterion is met for the observable
\(H(f)\). The efficiency of sampling process is noticeably
improved by way of interpolation of the quantity of
interest by a rational function \(R(f)\), fitting the support
points \(\{f_i, H_i; i = 0, 1, 2, \ldots, N\}\). Such the function is
defined as a quotient of polynomials \(P_L(f)\) and \(Q_M(f)\)
of orders \(L\) and \(M\), respectively, that is

\[
R_{LM}(f) = \frac{P_L(f)}{Q_M(f)} = \frac{\sum_{i=0}^{N} p_i f^i}{1 + \sum_{i=1}^{N} q_i f^i},
\]

where \(L + M = N\). Instead of constructing \(R_{LM}\)
explicitly, we employ in this study a recursive tabular
algorithm developed by Stoer and Bulirsch, which
generates implicitly the so-called diagonal rational
interpolant [3]. A combination of SB algorithm with
bisectional AFS results in the AFS-SB adaptive frequency
sampling scheme. This latter is controlled by error
surrogates. To be precise, for the interval \([f_{l-1}, f_l]\), three approximate values for \(H: H^+_{m}, H^-_{m}\) and \(H_{m}\) are computed at the midpoint \(f_m\) from three rational fitting models \(R_{L,M}\), \(R_{L+1,M-1}\) and \(R_{L-1,M+1}\) respectively. Then, the absolute values of relative errors between \(H^+_{m}\) and \(H_{m}\), and \(H^-_{m}\) and \(H_{m}\) respectively, are computed for the purpose of controlling the AFS-SB process. When one of the errors (or both of them) exceed(s) the assumed convergence tolerance, a new sample \(H_m\) is computed at \(f_m\) via MoM, the number of support points for the rational fitting model is thus increased by one, and the bisection process continues until the convergence criterion is met.

C. GPU+CPU co-processing

As already mentioned in the introductory section, the GeForce GTX 680 CUDA-capable device has been used to accelerate the MoM solution process. The device has 4 GB of GDDR5 memory and 8 Kepler-based Streaming Multiprocessors (SMXs) comprised of 8\times192 CUDA cores. Each SMX has access to 64 KB of on-chip memory configured as 48 KB of shared memory and 16 KB of L1 cache. The device has the capability to overlap kernel execution and data transfer between the device and host memory, offers fully IEEE-754 compliant single and double precision floating point operations, supports concurrent kernel execution, and employs a dynamic voltage and frequency scaling (DVFS) technique [10].

Solution of the integral equation via MoM involves two computationally intensive phases, i.e., assembling the system matrix \(Z\) and the solution of the linear system given by (5). Correspondingly, the CPU+GPU implementation of the MoM scheme has been divided into two relevant parts. The matrix assembly part is ported on the GPU device and handled by a highly optimized CUDA Fortran kernels [8]. To maximally exploit the compute capability of the device, blocks of 16\times16 threads using 40 registers each are employed in computing the system matrix \(Z\). The SMX with 64 K register file accommodates six such blocks, resulting in thread capacity of 1536 threads in each SMX utilizing 61440 registers, that is, 94% of the register file.

For the solution of the linear system given by (5), the routine \texttt{cuda_device_zgesv()} from a commercial library CULA Tools [11] is employed when the matrix \(Z\) fits into GPU memory. When the matrix is too big to reside in GPU memory, an out-of-core-like approach described in [12] is followed. In brief, the LU decomposition process of the \(Z\) matrix is divided into numerous tasks on top of blocks of its columns called panels. The panels are factorized on the CPU using a multi-core routine such as \texttt{zgetf2()} from the MKL library, while the trailing submatrices are updated on both the CPU and GPU with the use of highly optimized MKL/CUDA kernels. The pseudo-code for the proposed LU decomposition scheme is presented in Fig. 1. Note that four different CUDA streams are created to manage the computations (line 8). The initial data is assumed to be on the CPU, and when the GPU is executing the task, the data need to be copied from the host and sent back to be used for updating the impedance matrix. All data transfers are asynchronous, allowing the overlapping with kernel executions (line 16 and 19). To reduce CPU idle time, a concept known as a look-ahead is employed [13]. After performing LU factorization of the matrix, the backward substitution executed on the CPU yields a solution to the matrix equation (line 27).

Various aspects of GPU+CPU co-processing in solving dense linear algebra problems are discussed from general and CEM perspectives in [13, 14] and [15-17], respectively.

![Fig. 1. Pseudo-code for out-of-core-like LU decomposition of MoM matrix.](image_url)

III. RESULTS

To demonstrate the efficiency of the proposed approach, a lightning protection system directly hit by lightning is considered. The LPS, serving as a building shielding structure from the lightning electromagnetic pulse (LEMP), is modeled by a grounded wire-mesh cage. A perfectly electrically conducting (PEC) ground plane is assumed and taken into account by the method of images. The dimensions of the building are (length \(\times\) width \(\times\) height) 10 m \(\times\) 10 m \(\times\) 50 m. The model is based on the type 3 grid-like large volume shield considered in
The shield is assumed to be made of perfectly conducting wires of radius 4 mm forming a square mesh of 0.5 m × 0.5 m (see Fig. 2 (a)). The lightning is assumed to strike a corner of the building. The lightning channel is represented by a vertical lossy monopole antenna of the height 2 km and radius 5 cm, loaded with the distributed inductance of 4.5 μH/m in series with the resistance of 1 Ω/m [18]. The monopole is fed at its base by a delta-gap unit-voltage generator. The entire structure including LPS and lightning channel is discretized into linear segments of 1 m in length. The total number of segments is 18710, and the number of unknowns (basis functions) associated with the structure is 27109.

As a numerical example, the electric field/current transmittance:

\[ T_{E/I}(f) = |E(f)|/|I_g(f)|, \]  

where \( E(f) \) denotes the electric field intensity at the centre of the shielded volume \((x = 5m, y = 5m, z = 25m)\) and \( I_g \) is the current at the channel base (i.e., at the feed-point of the equivalent monopole antenna) has been computed. The resulting frequency run of the transmittance in the range from 1 kHz to 20 MHz is shown in Fig. 3 in the linear and logarithmic scales. The empty circles represent data points (EM samples) generated by the AFS-SB/GPU algorithm outlined in Section II. As can be seen, the AFS-SB/GPU results compare very well with those derived from FEKO [19].

The computations of \( T_{E/I} \) were performed for the frequency range from 1 kHz to 20001 kHz with the initial frequency step \( \Delta f = 2 \text{ MHz} \) and the convergence tolerance \( \delta = 0.01 \). The AFS-SB algorithm generated totally 149 non-uniformly spaced frequency samples of \( T_{E/I} \) with the frequency step locally decreased to 3.90625 kHz. To achieve the same convergence level with uniform sampling, 5121 samples taken with \( \Delta f = 3.90625 \text{ kHz} \) would be required so that the AFS-SB algorithm offers about 34.4x reduction of the number of EM samples. Moreover, engaging GPU device in both phases of MoM solution, that is, assembling the system matrix \( Z \) and solving the system of linear Equations (5), accelerates computations by a factor of 6.7 for each frequency sample. The total wall-clock simulation time was 16 h 16 min, and the improvement in performance with a speedup ratio of about 34.4 x6.7 = 230x was achieved compared to a reference single-thread sequential CPU implementation of the uniform sampling scheme. When a parallel four-core CPU OpenMP version of the code is taken as a reference, the above figure drops to about 64x.

The knowledge of voltages induced in electrical circuits inside a protected volume/building is crucial for the design of LPS. To mimic the situation of interest, a long vertical cylindrical wire of radius 0.89 mm was placed in the protected volume parallel to the down conductors of the LPS system and connected directly between midpoints of the roof and the floor coinciding with PEC ground (see Fig. 2 (b)). The wire was discretized into 100 0.5-m segments resulting in that the total number of basis functions associated with the considered structure increased to 27210. The task was to calculate the voltage/current transmittance defined as:

\[ T_{U/I}(f) = |U(f)/I_g(f)|, \]

where \( U \) is the open-circuit voltage at point \( P \) located in the middle of the wire (see Fig. 2 (b)) and \( I_g \) denotes the current at the lightning channel base. Figure 4 shows the frequency run of the transmittance of interest in the range from 1 kHz to 20 MHz using a convention similar to that applied for \( T_{E/I} \). Again, the AFS-SB/GPU results are in excellent agreement with the results derived from a commercial full-wave EM simulator FEKO [19]. This time the AFS-SB algorithm launched for the frequency range from 1 kHz to 20001 kHz with the initial \( \Delta f = 2 \text{ MHz} \) and \( \delta = 0.01 \) generated 70 non-uniformly spaced frequency samples of \( T_{U/I}(f) \) with the frequency step locally refined to 31.25 kHz. This implies that 641 samples uniformly spaced at every 31.25 kHz would be required to achieve the same convergence level. Hence, the number of samples needed for reconstruction of \( T_{U/I}(f) \) is reduced by a factor of about 9.2. The overall improvement in performance with a speedup ratio of about 17x was achieved compared to the four-core parallel OpenMP version of the code. The total wall-clock simulation time was 7 h 41 minutes.
IV. CONCLUSION

The fast technique based on method of moments for wideband analysis of lightning protection systems is presented in the paper. Broadband capability of the technique is attained through supporting MoM by the dynamic adaptive frequency sampling employing the interval halving scheme backed by the recursive tabular Stoer-Bulirsch rational interpolation algorithm. The approach offers significant reduction in the number of EM samples needed for reconstruction of the response of the system. Further speedup of numerical MoM-based simulations is achieved by GPU hardware acceleration. In case of GeForce GTX 680 CUDA-capable device used in this study, the improvement in performance with a speedup ratio of about 6.7x for each frequency sample is reached compared to the single-thread sequential CPU implementation of the algorithm. Numerical examples for the grid-like LPS directly hit by lightning are presented to illustrate the usefulness and efficiency of the approach. From a broader perspective, the approach described in this paper represents an example of utilizing the potential for technical computing provided by CPU+GPU architectures of low-cost PC-based workstations.

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https://www.feko.info/

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Shape Reconstruction of Three Dimensional Conducting Objects Using Opposition-Based Differential Evolution

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Abstract — In this paper, shape reconstruction of three dimensional conducting objects using radar cross section (RCS) of the scatterer and opposition-based differential evolution is investigated. The shape of the scatterer is modeled with nonuniform rational B-spline (NURBS) surfaces composed of more than one Bezier patches. NURBS are piecewise polynomial with unknown coefficients that are determined in the procedure of shape reconstruction. Opposition-based differential evolution (ODE) is then employed as an optimization tool to find the unknown coefficients. Physical optics approximation is used to predict RCS of the large conducting scatterer in various directions and at multiple frequencies. The effect of noise is also considered in the inverse process.

Index Terms — Inverse scattering, NURBS modeling, opposition-based differential evolution, physical optics approximation.

I. INTRODUCTION

The objective of inverse scattering methods is to discover features of an object by means of the electromagnetic (EM) scattered field. These methods have several applications such as nondestructive testing, biomedical imaging, and ground-penetrating radars. The complexity encountered in inverse scattering is mostly due to ill-posed and nonlinear problems. Mathematical algorithms of inverse scattering problems are mostly categorized into the time-domain or the frequency-domain solutions. The time-reversal method is an example of time-domain solutions [1]. Optimization methods are mostly utilized in widely used frequency-domain approaches. Optimization methods are commonly used for reconstruction of two dimensional conducting and dielectric objects [2-5]. In [2], the shape of the scatterer is modeled with the cubic B-spline curves. These curves are piecewise polynomial where their coefficients are determined by control points. The control points are found such that a specific measure of difference between reconstructed and original scattered fields is minimized. This approach could be generalized to three dimensional problems. In this case, the structure is modeled with non-uniform rational B-spline (NURBS) surfaces. NURBS are also piecewise polynomials where their coefficients are defined by a set of control points and associated weights. For computational purposes, NURBS surfaces are decomposed into Bezier surfaces. These surfaces are also piecewise polynomials. In [6], a NURBS surface composed of only one Bezier patch is considered and genetic algorithm (GA) is used to reconstruct the shape of a three dimensional conducting object.

Generally, NURBS surfaces have a complex geometry and are composed of more than one Bezier surface. This paper tries to reconstruct a more complex structure composed of more than one Bezier surface. The geometrical continuity of the surfaces complicates the reconstruction approach. The proposed algorithm is based on opposition-based differential evolution (ODE) as an optimization tool, because unlike GA, the ODE is simple to implement; it does not require coding and decoding of population members. In each iteration of the optimization algorithm, RCS of the reconstructed conducting body is calculated using physical optics (PO) approximation. The paper is organized as follow. Section II presents a brief review of NURBS modeling. Computation of PO integral is discussed in Section III. The inverse problem is discussed in Section IV. Some simulation results are presented in Section V. Concluding remarks are given in Section VI.

II. GEOMETRIC DESCRIPTION OF THE BODIES

In this paper, non-uniform rational B-spline surfaces are used for geometric modeling of the bodies.
The main reason for this choice is that a small amount of information is needed for accurate representation of complex objects. NURBS surfaces are specified with a set of control points, associated weights, and knot vectors. A NURBS surface is expanded as a set of Bezier patches. Geometrical parameter calculation of Bezier patches is easier than the NURBS surfaces. In the following, we discuss the concept of rational Bezier curves and then extend it to the three-dimensional surfaces. Rational Bezier curves could be formulated as follows [7]:

$$\vec{r}(u) = \sum_{i=0}^{m} w_i \vec{b}_i B^n_i(u) \bigg( \sum_{j=0}^{m} w_j B^n_j(u) \bigg), \quad (1)$$

where \( \vec{b}_i \in \mathbb{R}^3 \), \( i = 0, \ldots, m \), are the control points, \( w_i \in \mathbb{R}, \quad i = 0, \ldots, m \), are the associated weights, the integer \( m \) is the curve degree, and \( B^n_i(u) \), \( i = 0, \ldots, m \), are the Bernstein polynomials given by:

$$B^n_i(u) = \frac{m!}{i!(m-i)!} u^i (1-u)^{m-i}, \quad 0 \leq u \leq 1, \quad (2)$$

\( u \) is a parameter between zero and one that shapes the curve. When these control points move through space on another Bezier curve, a Bezier surface is formed. The resulting surface could be formulated as follows:

$$\vec{r}(u,v) = \sum_{i=0}^{m} \sum_{j=0}^{n} w_{ij} \vec{b}_{ij} B^n_i(u) B^n_j(v) \bigg( \sum_{j=0}^{m} \sum_{j=0}^{n} w_{ij} B^n_i(u) B^n_j(v)w_{ij} \bigg), \quad (3)$$

where \( \vec{b}_{ij} \in \mathbb{R}^3 \), \( i = 0, \ldots, m \), \( j = 0, \ldots, n \), are the control points, \( w_{ij} \in \mathbb{R} \), \( i = 0, \ldots, m \), \( j = 0, \ldots, n \), are the associated weights, and the integers \( m \) and \( n \) are degrees of the surface. Similar to \( u \), \( v \) is a parameter between zero and one that shapes the other dimension of the surface. When a set of Bezier surfaces are connected by a specific continuity rule, a B-spline surface is formed. The resulting B-spline surface has an appealing property of local control ability [7]. A B-spline surface can be expanded as a linear combination of B-spline basis functions [9].

**III. PHYSICAL OPTICS**

When the dimensions of the conducting object are large compared to the wavelength, the backscattering electric field is specified by [9]:

$$\vec{E}_s(r) = -\frac{j}{\lambda} \frac{\exp^{-jk\vec{r} \cdot \vec{r}'}}{r} \vec{k} \vec{E}_0 \vec{I} = \int n(r') \exp^{jk \vec{r} \cdot \vec{r}'} ds', \quad (4)$$

where \( \lambda \) is the operating wavelength, \( \vec{E}_0 \) is the polarization of the incident field, \( \vec{k} \) is the wave vector, \( \vec{r}' \) is the position vector, \( ds' \) is the differential element of the surface, \( \hat{n} \) is the normal vector at the surface point, \( k_0 \) is the wave number, and \( \vec{I} \) is the physical optics integral. For a Bezier surface, \( \vec{I} \) is written as follows:

$$\vec{I} = \int_{u=0}^{1}\int_{v=0}^{1} g(u,v) \exp[jk(f(u,v))] du dv, \quad (5)$$

where

$$\vec{g}(u,v) = \hat{r}_u \times \hat{r}_v, \quad f(u,v) = 2k\vec{r}(u,v). \quad (6)$$

Any surface can be formed with composition of three kinds of Bezier surfaces, (a) singly curved, (b) doubly curved, and (c) plane patch. PO integral can be evaluated for these kinds of surfaces as explained in continue.

**A. Singly curved surfaces**

When the degree of a Bezier surface is equal to one, then a singly curved surface is formed as shown in Fig. 1 (a). In other words, this surface is formed when a curve moves on a straight line in space. Suppose that the surface is linear along parameter \( v \), then the phase term in PO integral can be written as follows:

$$f(u,v) = f_s(u) + v f_p(u) = 2k \vec{j}_s(u) + v 2k \vec{j}_p(u), \quad (7)$$

thus, the PO integral is

$$\vec{I} = \int_{u=0}^{1}\int_{v=0}^{1} \exp[jk f_s(u)] \int_{v=0}^{1} \vec{g}(u,v) \exp[jk f_p(u)] du dv. \quad (8)$$

Integration with respect to the parameter \( v \) can be computed by expanding \( g(u,v) \) in Taylor series around \( v_0 = 0.5 \) and then calculating the integral of each term in the series analytically, then we have,

$$\vec{I} = \int_{u=0}^{1} \exp[jk f_s(u)] G(u), \quad (9)$$

where \( G(u) \) is

$$G(u) = \sum_{n=0}^{\infty} \sum_{k=0}^{n} \frac{g_i(u,v_0) v_0^{n-k}}{(k-n)!} A_n(u), \quad (10)$$

and

$$A_n(u) = \int_{v=0}^{1} \exp[jk f_s(u)] dv = \frac{n!}{-jk f_s(u)^{n+1}} \sum_{i=0}^{n} \frac{n! \exp[jk f_s(u)]}{(n-i)![-jk f_s(u)]^{n+1}} \quad (11)$$

Integration with respect to the parameter \( u \) can be evaluated via a trapezoidal numerical method. In some references, this integral is computed with stationary phase method [8-10]; however our simulations show that numerical method is more accurate.

**B. Doubly curved surfaces**

When both degrees of a Bezier surface is greater than one, a doubly curved surface is formed as shown in Fig. 1 (b). In this case, currents near the certain critical points produce the main contribution of the scattered field. There are three kinds of critical points: stationary phase points, boundary points, and vertex
points as shown in Fig. 2. The phase term of the integrand is expanded in Taylor series around the critical points and then physical optics integral is easily calculated. This method is explained in [8-10].

C. Plane patches

When both degrees are equal to one, a plane patch is formed as shown in Fig. 1 (c). For plane patch, PO integral can be evaluated using Gordon method [11].

Fig. 1. Three kinds of Bezier surfaces and their control points: (a) singly curved surface, (b) doubly curved surface, and (c) plane patch [8].

Fig. 2. critical points over the Bezier surface [5].

IV. INVERSE SCATTERING

In the inverse scattering procedure, the control points of the rational spline surface are optimally located such that the RCS of the reconstructed scatterer in multiple directions and at several frequencies approaches the RCS of the original scatterer. Here, the shape of the scatterer is approximated by a degree- \( n \) surface that is constructed by rational spline curves (Fig. 3). The shape of these curves and the distance between them are determined by an optimization algorithm. Therefore, arbitrary objects can be reconstructed. Compared to the reference [6], an exact algorithm for reconstruction is presented here, and some complex objects are rebuilt as well. In addition, in this case, other issues such as the effect of the shadowing of a surface by another surface, is taken into consideration by the authors while nothing is concerned in reference [6] regarding this effect.

A. Optimization algorithm

The opposition-based differential evolution is our optimization approach as follows. If the problem has \( D \) unknown parameters, then \( NP \) parameter vectors of \( D \)-dimension are produced in the first step [12]:

\[
x_{i,j}, \quad i = 1, \ldots, NP.
\]

Then, the opposite population is calculated by:

\[
\alpha x_{i,j} = a_j + b_j - x_{i,j},
\]

where \( a_j \) and \( b_j \) are the lower and upper bounds of the \( j^{th} \) dimension of the parameter vector respectively. If the cost function of \( \alpha x_{i,j} \) is lower than \( x_{i,j} \), then \( x_{i,j} \) is replaced by \( \alpha x_{i,j} \). According to probability principles, this happens 50\% of the time. In the second step, a mutant vector is produced for each target vector as:

\[
u_i^{G+1} = x_{i1}^{G} + F_i (x_{i2}^{G} - x_{i3}^{G}),
\]

where \( G \) is the generation index and \( r_1, r_2, r_3 \) are three mutually different integers that also differ from target index \( i \). \( F \) is also the mutant constant that is usually taken to be 0.8. Next, from the combination of the mutant vector and the target vector, the trial vector is produced:

\[
u_i^{G+1} = u_i^{G+1} = (u_{i1}^{G+1}, u_{i2}^{G+1}, \ldots, u_{iD}^{G+1}),
\]

where

\[
u_{i,j}^{G+1} = \begin{cases} 
\nu_{i,j}^{G+1} & \text{if } h_j < H \text{ or } j = l \\
\nu_{i,j}^{G+1} & \text{if } h_j > H \text{ and } j \neq l
\end{cases}
\]

In this equation, \( h_j \) is a random number in the interval \([0,1]\), \( H \in (0,1) \) is a crossover constant selected by the user, and \( l \) is a random integer \( \in [1, 2, \ldots, D] \). If the cost function of \( u_{i,j}^{G+1} \) is smaller than \( x_{i,j}^{G+1} \), then \( x_{i,j}^{G+1} \) is replaced by the trial vector. Similarly, opposite of the current population is generated by:

\[
\alpha x_{i,j}^{G} = \text{MIN}_j^{G} + \text{MAX}_j^{G} - x_{i,j}^{G},
\]

where \( \text{MIN}_j^{G} \) and \( \text{MAX}_j^{G} \) are the minimum and maximum of \( j^{th} \) dimension in the current population. Now, a random number between \([0,1]\) is generated and
if it is lower than the preselected jumping rate \( J_r \), then \( x_{i,j}^G \) is compared with \( a x_{i,j}^G \) and the one with a lower cost function is selected as the member of the current population. Here, the selected parameters of the opposition-based differential evolution are listed in Table 1.

B. RCS based cost function

The cost function for this optimization is defined as:

\[
 f(p) = \frac{\sum \sum \sum |\sigma_{\theta,\phi,\omega}^{\text{true}} - \sigma_{\theta,\phi,\omega}^{\text{rec}}|}{\sum \sum \sum |\sigma_{\theta,\phi,\omega}^{\text{true}}|},
\]

where \( \sigma_{\theta,\phi,\omega}^{\text{true}} \) and \( \sigma_{\theta,\phi,\omega}^{\text{rec}} \) are radar-cross sections of the original and the reconstructed scatterer respectively. The cost function is minimized to find the location of control points, \( p \) and the distance between curves. For considering the noise effect, the original RCS is modified as follows [6]:

\[
 \sigma_{\theta,\phi,\omega} = \sqrt{\sigma_{\theta,\phi,\omega}^2 + (NL) \times (\text{rand})}.
\]

In this equation, \( \sqrt{\sigma_{\theta,\phi,\omega}^2} \) is the rms of the original RCS, \( NL \) is the noise level, and \( \text{rand} \) is a random number picked from the interval \([0,1] \). In this paper, the radar cross section of the scatterer is used in the cost function, so that the phase of the scattered field is not taken into account, and the transmission of the object is obtained.

V. NUMERICAL RESULTS

For the first example, the reconstruction of perfectly conducting cone modeled with one NURBS surface composed of three Bezier surfaces is presented. The cone has the height of 1m and the bottom radius of 1m and the top radius of 0.5m as shown in Fig. 4 (a). In the reconstruction procedure, the degree of the surface and weight coefficients are selected a-priori. In addition, we assume that the curvature of the surface is negative. It should be noted that the weight of control points and the degree of surface can also be considered as the optimization parameters; however, in this state, the volume of computations is enormous and it is not considered here as just a generalized method for complex structures was aimed. This cone is modeled with 6x2 control points. The scattered filed is evaluated at 45 points that are uniformly located around the object at \( \theta = 60^\circ, 75^\circ, 90^\circ \) and at frequencies \( 0.4, 0.8, 1.2 \text{GHz} \).

Figure 4 (b) displays the reconstructed cone. The average cost function for five simulations as a function of number of iterations are depicted in Fig. 4 (c). The RCS of the original and the reconstructed cones are presented in Fig. 4 (d). A very good agreement between the original cone and the reconstructed cone is observed.

![Figure 4](image-url)
Fig. 5. (a) Original cone cylinder, (b) reconstructed cone cylinder, (c) average cost function, and (d) radar cross section of the original and the reconstructed cone-cylinder at $f = 1.2 \text{GHz}$ and $\phi = \pi / 4$.

Table 1: Opposition-based differential evolution parameters

<table>
<thead>
<tr>
<th>Jumping Rate</th>
<th>Mutant Constant</th>
<th>Crossover Rate</th>
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<tbody>
<tr>
<td>0.5</td>
<td>0.8</td>
<td>0.5</td>
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To evaluate the accuracy of the reconstruction procedure, a shape error is defined as follows [6]:

$$RECP = \frac{1}{N_{\text{net}}} \sum_{i=0}^{N_{\text{net}}} \left[ \| \Delta^{a_i} p_{i,j}^\text{true} - \Delta^{a_i} p_{i,j}^\text{true} \|_2 \right]^2 + \frac{\| \Delta^{b_j} p_{i,j}^\text{true} - \Delta^{b_j} p_{i,j}^\text{true} \|_2^{1/2}}{\| \Delta^{b_j} p_{i,j}^\text{true} \|_2},$$

where $N_{\text{net}} = 2mn + m + n$ is the number of elements in the vector net and $\| p_{i,j} \|$ is the Euclidean norm given by:

$$\| p_{i,j} \| = \sqrt{x_{i,j}^2 + y_{i,j}^2 + z_{i,j}^2}.\quad (21)$$

$\Delta^{a_i} p_{i,j}$ and $\Delta^{b_j} p_{i,j}$ are related to the control points as:

$$\Delta^{a_i} p_{i,j} = p_{i,j+1} - p_{i,j} \quad \Delta^{b_j} p_{i,j} = p_{i+1,j} - p_{i,j}. \quad (22)$$

In the simulation, the shape error for a half cone is calculated to be 0.04423. In the presence of a noise level of 10%, the shape error is 0.04725. For the second example, the reconstruction of perfectly conducting cone-cylinder modeled with one NURBS surface composed of six Bezier surfaces is presented. The cone-cylinder has the height of 1m for both the cone and the cylinder and radius of 1m at the bottom and 0.5m at the top. Similar to the previous example, Fig. 5 shows the target and the simulation results. Here, the shape error for cone-cylinder is calculated to be 0.071. In the presence of a noise level of 10%, the shape error is 0.1527. In the following, we can consider this issue for the reconstruction of buried objects by taking into account the effect of a background layer.

VI. CONCLUSION

In this paper, the PO approximation, the ODE algorithm, and NURBS modeling are used to reconstruct three-dimensional conducting objects. NURBS surface are used to model unknown scatterers by a minimum number of parameters. The reconstruction is done by applying the ODE algorithm as an optimization tool. Here, NURBS surfaces composed of more than one Bezier surface is reconstructed. A very good agreement between the original object and the reconstructed object is achieved.

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