Theoretical Approach for the Design of a New Wideband Ku-band Printed Antenna

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Abstract — A design of a broadband Ku-band low-cost printed circuit board technology (PCB) antenna is presented in this paper. An approach was developed to enhance the bandwidth of a simple printed patch antenna. The proposed method is, step by step, detailed to discuss the evolution of the antenna geometry and depicts the contribution of the imported changes on the properties achieved each time. A 22% relative bandwidth in Ku-band was obtained for a footprint of 0.4λ0×0.6λ0 (λ0 is the wavelength in the free space). A good agreement between the simulation and the measurement results of the wideband patch was observed, which proves the interest of this approach.

Index Terms — Antenna input impedance, antenna theory, Ku-band, linear polarization, polygonal antennas, wideband antenna.

I. INTRODUCTION
There is a growing interest in small, flat, discreet, efficient, and low-cost antenna design. In satellite application context, these antennas should have a broadband behavior covering all the Ku-band, a high directivity and a linear polarization. The reflector based antennas are commonly used because they satisfy all these requirements, but they are not practical due to their relatively big size and their 3D geometry. An interesting alternative of such antennas could be the grounded planar printed based antennas because of their low profile, cheap price and simple manufacturing [1,2]. Nevertheless, with such a technology for simple shape antenna, broadband behavior is limited to a few percent. To enhance the bandwidth, different techniques can be used. Some are based on the superposition of several layers of dielectrics and resonators known as the stacked antennas [3-7]. This technique implies a precise alignment of the resonators hard to achieve, especially at high frequency like in Ku-band. Others use a co-planar arrangement of parasitic elements surrounding the driven resonator. These parasitic elements have almost the same size as the driven one which leads to a relatively large size of the patch. When high directivity has to be reached, antenna array is needed and therefore the patch size becomes a crucial criterion. In this case, if the basic element has more than a wavelength size, grating lobe problem arises. Coplanar multi-resonator solution is then irrelevant and incompatible with antenna array [8-11]. In [12] and [13], the authors explain that with some modifications of the geometry of the rectangular patch antenna, a relative bandwidth of 20% can be achieved just by coupling two different modes. The two chosen modes are orthogonal. It means that the polarization is unstable within the bandwidth. Therefore, the steady linear polarization criterion for satellite reception cannot be satisfied. In this paper, we propose to develop a new broadband single element printed antenna operating in Ku-band with compact size and stable linear polarization in order to be suitable with an antenna array configuration and achieve higher directivity. This article is organized as follows: In Section II, a rigorous theoretical approach is developed and validated according to simulations using CST Microwave Studio® software. A prototype of the proposed antenna is realized and measured. Measurement results, presented in Section III, are in good agreement compared to the simulations.

II. ANTENNA DESIGN
A. Rectangular patch antenna
Different kinds of planar antenna topologies exist: ungrounded and grounded ones. The first is interesting for its omnidirectional radiation pattern and an ultra-wideband behavior could be easily achieved. It is extensively used for applications like mobile communication systems. The second is more suitable for
point-to-point communication to avoid energy losses, except that the limited bandwidth is its handicap. As satellite services require point-to-point communication with direct link antennas, the grounded planar antenna technology is then more suitable, if solutions are found to maintain the linear polarization over a wide bandwidth. In this technology, the bandwidth usually depends on the thickness, the nature of the dielectric substrate, and the antenna’s geometry. To broaden the bandwidth of a rectangular patch antenna, the most used techniques are based on decreasing the substrate relative permittivity $\varepsilon_r$, raising the dielectric thickness $h$ and enlarging the patch width $W$ [14]. However, the bandwidth of this simple shape printed antenna remains limited to about 10%. To highlight this issue, a probe-fed rectangular microstrip antenna printed on a 1.58 mm height Teflon-glass substrate of a relative permittivity 2.55 and $\tan \delta = 0.007$ operating at 11.7 GHz is firstly simulated with CST Microwave Studio®. Its dimensions are tuned in order to enlarge the bandwidth for this simple pattern. The optimized rectangular antenna’s reflection coefficient $S_{11}$ is represented in Fig. 1.

![Fig. 1. Simulated reflection coefficient $S_{11}$ of the rectangular patch antenna ($L = 7$ mm and $W = 10$ mm and $x = 2.7$ mm).](image)

As previously mentioned, a relative bandwidth of 10% is observed in this figure, which is quite close to the maximum bandwidth for this kind of structure [14]. An idea to overcome this insufficiency consists in designing a simple patch antenna by exploring the rectangular patch characteristics and making some changes in its geometry to get an enlarged bandwidth of more than 10%, while maintaining the same linear polarization over the whole bandwidth. Therefore, a rectangular patch is introduced and analyzed. Its dimensions are calculated from the analytical expressions given in [15,16]. According to these expressions, the variation of the length $L$ of a rectangular patch printed on a Teflon-glass substrate for fixed values of $W$ (width of the patch), $h$ (the substrate thickness), and $\varepsilon_r$ (substrate relative permittivity) versus the frequency is represented in Fig. 2.

![Fig. 2. Length of a rectangular patch versus frequency when $W = 13$ mm, $h = 1.58$ mm, $\varepsilon_r = 2.55$ and $x = 2.7$ mm.](image)

According to Fig. 1, the value of the input resistance is related to the position $x$ of the feed point from the center of the antenna. To get maximum power transfer, this position should be determined in a way that the input resistance $R_i$ is equal to the source resistance (typically 50 $\Omega$). On the other hand, for a fixed distance $x$, the input resistance will only depend on the frequency when $W$, $h$ and $\varepsilon_r$ have also fixed values as illustrated by Fig. 3 below.

![Fig. 3. Input resistance $R_i$ ($\Omega$) versus frequency when $W = 13$ mm, $h = 1.58$ mm, $\varepsilon_r = 2.55$ and $x = 2.7$ mm.](image)

According to Fig. 3, some same input resistance is met for two different frequencies. For example, $R_i = 50$ $\Omega$ is obtained at both 4.7 GHz and 18.2 GHz, which means that two collinear resonators can be optimally coupled to...
the same feed point position.

**B. Polygonal patch antenna**

In accordance with Fig. 3, two resonators can be optimally coupled having the same feeding point; in this case, this is possible for coaxial feeding probe situated at \( x = 2.7 \text{ mm} \) from the center of the resonators. Based on Fig. 2, the first resonator has 3.9 mm length for a frequency of 18.2 GHz and the second has 19.2 mm length for a frequency of 4.7 GHz. We should then present a geometry that has these two different lengths. One way consists in using the dimensions \( L \) and \( W \) of the patch antenna as \( L_1 \) and \( L_2 \). But, in this case, two orthogonal modes are excited, which means that the radiated power has different polarizations. To ensure same polarizations over the two frequencies, \( L_1 \) and \( L_2 \) has to be carried on along only one axis. As illustrated in Fig. 4 (a), a polygonal design can be a possible candidate to meet the mentioned condition of the linear polarization using the two different lengths. From Fig. 3, the expected reflection coefficient \( S_{11} \) of this antenna should have the form given in Fig. 4 (b).

![Fig. 4. Proposed antenna and its expected reflection coefficient: (a) polygonal patch antenna, and (b) \( S_{11} \) parameter of the polygonal antenna matched to 50 \( \Omega \).](image-url)

In order to reduce the size of the polygonal antenna, to widen the bandwidth of each resonant frequency and to have protection against the environment, a 3.175 mm thickness Nelco NY9220 substrate with a relative permittivity of 2.2 and \( \tan \delta = 0.0009 \) is used as a rodome. To take into account the rodome layer effect in the simulation, we need an optimization of the polygonal antenna dimensions. Figure 5 shows the dimensions of the antenna with superstrate and the simulation result of its \( S_{11} \) parameter.

![Fig. 5. (a) Dimensions of the polygonal antenna with rodome, (b) side view, and (c) simulated \( S_{11} \) parameter.](image-url)

This figure confirms that the optimized antenna with rodome has a dual band behavior. Table 1 summarizes the electric field distribution for the two resonant frequencies to check their polarizations quality.

<table>
<thead>
<tr>
<th>Frequency (GHz)</th>
<th>Electric Field (E_x)</th>
<th>Electric Field (E_y)</th>
</tr>
</thead>
<tbody>
<tr>
<td>9.75 GHz</td>
<td>Maximal</td>
<td>Null</td>
</tr>
<tr>
<td>13.29 GHz</td>
<td>Maximal</td>
<td>Null</td>
</tr>
<tr>
<td>18.2 GHz</td>
<td>Null</td>
<td>Maximal</td>
</tr>
<tr>
<td>20 GHz</td>
<td>Null</td>
<td>Maximal</td>
</tr>
</tbody>
</table>

We notice that for all these two dips, the transverse fringing fields along Y-axis (\( E_y \)) on both sides of the antenna are in opposite phase with quite the same magnitude. In other words, the resulted vertical polarization radiation (cross-polarization) in the broadside direction is null for all frequencies, meaning that the polygonal shape of the patch does not introduce theoretically any cross-polarization. For the frequencies 9.75 and 13.29 GHz, the electric fields along X-axis are not in opposite phase, so the resulted radiation horizontal polarization (co-polarization) is maximal in the broadside direction.
Table 1: E-field of the polygonal antenna with rodome

<table>
<thead>
<tr>
<th>Frequency (GHz)</th>
<th>9.75</th>
<th>13.29</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>I</td>
<td>II</td>
</tr>
</tbody>
</table>

C. Polygonal antenna with circular slot

The polygonal antenna depicted in Fig. 5 presents two separated bands corresponding to two distinct modal resonances. Nevertheless, wideband behavior is expected. From Fig. 3, the impedance plot presents a maximum for a frequency located between the two frequencies matched to 50 \( \Omega \), which explains the high reflection coefficient for this distinct frequency. The idea consists of reducing the reflection coefficient at this maximum without deteriorating the impedance matching of the existing two frequencies. It can be resolved by modifying the propagation conditions inside the resonator. Thus, follows a manner to enlarge the bandwidth by using a slot inside the polygonal patch is step by step detailed.

1) Influence of a slot inside the patch

First, it is important to review theoretically the effect of a simple slot inside a patch. Usually, a slot can be modeled as a capacitance whose value depends not only on the dimension of the slot, but also on its orientation and its position inside the patch. To evaluate the influence of the slot, the electric field distribution inside the substrate, under the patch, is studied. For the fundamental resonance of a rectangular patch antenna, the magnitude of the electric field is expressed in [16] as follows:

<table>
<thead>
<tr>
<th>E_x</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
</tr>
<tr>
<td>b</td>
</tr>
<tr>
<td>c</td>
</tr>
</tbody>
</table>

| E_y |

Fig. 6. Electric fields \( E_x \) and \( E_y \).

The value of the magnitude of this electric field can be determined by calculating the potential difference between both sides of the slot:

\[
E_s \delta = V_2 - V_1, \quad (5)
\]

where \( \delta \) is the slot width, \( V_1 \) is the potential at \( y = d \) and \( V_2 \) is the potential at \( y = d + \delta \).

Assuming that \( d >> \delta \) and \( \delta << L \), then:

\[
E_s = E_0 \frac{h}{L} \cos \frac{nd}{L}. \quad (6)
\]

From the expression of the electric field magnitude \( E_s \), we deduce that \( E_s \) is much smaller than \( E_r \) because \( L \) is much bigger than \( \Delta \). Therefore, the slot does not have great influence on the radiation pattern of the antenna. Now, if the slot is oriented with an angle \( \theta \), Fig. 7, \( E_s \) can be written as follows:

\[
E_s (y) = E_0 \frac{h}{L} \cos \frac{\theta y}{L} \cos \frac{nd}{L}, \quad (7)
\]

where \( d \) is the distance between the \( Y \)-axis of the patch and the slot location for a given value of \( y \).

Fig. 7. Representation of the slot with an angle \( \theta \).
To maintain the symmetry of the structure, we propose to use a circular slot. In this case, the distance \( d \) will depend on the angle \( \theta \) and the inner radius \( R \) of the circular slot and can be written as follows:

\[
d = R \cos \theta,
\]

where \( \theta \) varies from 0° to 360°, Fig. 8.

\[\theta (\frac{\pi}{L}, \frac{\pi R \cos \theta}{L})\]

\[
\text{Fig. 8. Variation of the distance } d \text{ in a circular slot.}
\]

Finally, the magnitude of the electric field inside the slot has the following expression:

\[
E_s = E_0 \frac{n h}{L} \cos \left( \frac{n R \cos \theta}{L} \right) \cos \theta,
\]

\[\text{Fig. 9 represents the variation of } E_s \text{ versus } \theta \text{ for different values of the slot radius } R \text{ when } E_0 = 100.\]

\[\text{Fig. 9. Variation of the magnitude of the electric field inside the circular slot } E_s \text{ versus } \theta \text{ according to the equation (9).}\]

To explain the circular slot influence, we consider the patch antenna as a transmission line [16]. From this model, the input impedance is related to the characteristic impedance of the line which is given by the following expression:

\[
Z_C = \frac{L_0}{C_s}
\]

where \( L_0 \) is the serial inductance per unit length and \( C_s \) is the parallel capacitance per unit length.

When a slot is introduced inside the patch antenna, its equivalent capacitance \( C_s \) reduces the serial inductance \( L_0 \) and so the characteristic impedance of the line, assuming that the phase velocity of the travelling wave remains unchanged. From Fig. 9, we notice that the value of the electric field \( E_s \) inside the circular slot is non-null, when theta (\( \theta \)) is within the range [0°, 90°] and it is null when \( \theta = 0° \) or \( \theta = 90° \) for \( R \approx \frac{L}{2} \). In this case, the capacitance \( C_s \) is equal to zero when theta’s value is equal to 0° or 90°, due to the absence of the electric field for these two values of theta. Therefore, the slotted patch characteristic impedance \( Z'_c \) at \( \theta = 0° \) and \( \theta = 90° \) is almost equal to the patch characteristic impedance \( Z_c \) without slot. But, its value decreases when \( \theta \) is within the range of degrees from 0° to 90°.

In section I, we demonstrated that for a polygonal antenna, the lower resonant frequency is related to the largest length (L₂) and the higher one is related to the smallest length (L₁). Now, after the insertion of the circular slot, when \( \theta = 0° \), a portion of the slot is located on the largest length. But when \( \theta = 90° \), another portion is located on the smallest length. It is then expected, theoretically and based on the discussion following Fig. 9 that the circular slot will not impact the impedance matching for the two resonant frequencies of the antenna presented in Fig. 5. However, the frequencies between them undergo an input resistance reduction, which should improve the bandwidth of the antenna.

2) Simulation results

A polygonal antenna with a circular slot inside the patch [17] has been simulated and it is shown in Fig. 10. According to the previous theory, the value of the outer radius \( R_{out} \) is chosen close to \( \frac{L_2}{2} \) (\( R_{out} = 3.7 \) mm). The slot width is equal to 0.3 mm. The feeding probe is located at a distance \( x = 2.9 \) mm from the center of the antenna. A small air gap of 0.1 mm needs to be taken into account in the simulation between the patch and the rodome. The simulation result of \( S_{11} \) parameter of the proposed antenna is given in Fig. 11.

According to the simulation result for the given value of the slot width (0.3 mm), this antenna has a bandwidth around 3 GHz (from 11.6 GHz to 14.8 GHz) at -10 dB. The simulation shows that due to the insertion of the circular slot, the dual band antenna was indeed transformed to a broadband antenna.

\[\text{Fig. 10. Proposed polygonal antenna with a circular slot.}\]
Fig. 11. Simulation result of the $S_{11}$ parameter of the antenna patch with circular slot.

To show the influence of the slot width on the antenna reflection coefficient, a parametric study for different widths of the circular slot (quite small compared to the wavelength) is given in Fig. 12.

Fig. 12. Parametric study for different widths of the circular slot.

Table 2 shows that the relative bandwidth of the proposed antenna is not highly affected by the slot width which remains around 20%. Only the central frequency shifts towards higher frequencies as the slot width increases.

Table 2: Antenna relative bandwidth for different slot width

<table>
<thead>
<tr>
<th>Slot Width (mm)</th>
<th>Relative Bandwidth (%)</th>
<th>Central Frequency (GHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.2</td>
<td>21</td>
<td>12.75</td>
</tr>
<tr>
<td>0.3</td>
<td>21</td>
<td>13.2</td>
</tr>
<tr>
<td>0.4</td>
<td>22</td>
<td>13.7</td>
</tr>
</tbody>
</table>

This is mainly due to the changes in the phase velocity supposed to be constant in the theory. The E-fields of the circular slotted polygon at 11.63 GHz, 13 GHz, and at 14.8 GHz are provided in Table 3 below.

The electric field distribution symmetry observed for all frequencies within the bandwidth, shows that the resulted field is oriented along X-axis and that the cross-polarization theoretically is null due to its perfect symmetry.

Table 3: E-field of the polygonal antenna with circular slot

According to Table 3 comments, the simulated co/cross-polarization radiation pattern, given in Table 4, shows that the cross-polarization level is about 20 dB less than the main polarization, as expected. The same polarization is observed over the whole bandwidth.

Table 4: Co/Cross-polarization in the E-plane at different frequencies

III. PROTOTYPE AND MEASUREMENTS

A prototype of this antenna was manufactured and measured. The dimensions of this design are given in Table 5. The patch was printed on a Teflon-glass substrate of 1.58 mm thickness with a relative permittivity of 2.55 and $\tan \delta = 0.007$. Its dimensions are set to $50 \times 50 \text{mm}^2$ ($2\lambda_0 \times 2\lambda_0$ where $\lambda_0$ is the wavelength at the lower frequency
10.7 GHz).

Table 5: Prototype antenna dimensions

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(L_1)</td>
<td>5.1</td>
</tr>
<tr>
<td>(W_1)</td>
<td>13</td>
</tr>
<tr>
<td>(L_2)</td>
<td>8.9</td>
</tr>
<tr>
<td>(W_2)</td>
<td>4.5</td>
</tr>
<tr>
<td>(R_{in}) (the slot inner radius)</td>
<td>3.41</td>
</tr>
<tr>
<td>(R_{out}) (the slot outer radius)</td>
<td>3.72</td>
</tr>
<tr>
<td>Feeding probe at (x)</td>
<td>2.9</td>
</tr>
</tbody>
</table>

The used rodome is a Nelco NY9220 substrate of a 3.175 mm thickness with a relative permittivity of 2.2 and \(\tan\delta = 0.0009\). The total size of the antenna is near \(0.4\lambda_0 \times 0.6\lambda_0\), compatible for the design of an antenna array. A photo of the proposed antenna is given in Fig. 13.

As shown in Fig. 14, a good agreement between simulations and measurements in terms of bandwidth is observed. It is around 3 GHz at -10 dB, which represents a relative bandwidth of 22%. The difference between the simulated and measured \(S_{11}\) is mainly due to the manual fabrication of the prototype, especially the feeding probe drilling (about few hundred \(\mu\)m).

Figure 15 below presents the measured radiation pattern of the antenna. The main and the cross-polarizations in E- and H-planes are given for three frequencies inside the band.

In the main radiation direction, the cross-polarization is about 10 dB lower than the main polarization. However, a slight degradation of the co/cross-polarization level is observed as we move away from broadside direction, particularly observed at lower frequencies of the bandwidth.

The reason behind this result could arise from the prototyping technology and maybe the zero-scale balance of the feeding probe problem due to the manual drilling. The observed ripples in the radiation pattern for all frequencies can be explained by the diffraction of the radiated field on the ground plane because of its limited dimensions. The maximum directivity observed is about 6.4 dBi.

Fig. 13. Photo of the prototype antenna.

Fig. 14. Comparison of \(S_{11}\) parameter of the simulated and measured antenna.

Fig. 15. Radiation pattern measurements within the bandwidth.
IV. CONCLUSION

In this paper, a theoretical approach of an original broadband antenna design is presented. It consists of a polygonal antenna with a circular slot inside. A polygonal antenna presents initially a dual band behavior due to two different collinear resonant lengths. But, the insertion of a circular slot transforms it to a broadband behavior because this slot acts as an impedance regulator. The measurements agree well with the simulations and confirm the interesting properties of this design such as the wideband behavior (a relative bandwidth of 22% in the Ku-band is observed) and the guaranteed linear polarization over the entire bandwidth. With only a footprint of $0.4\lambda_c \times 0.6\lambda_c$ and a 6.4 dBi gain, this design is a good candidate for antenna array configuration to achieve high gain like in satellite application services.

REFERENCES


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