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Equivalent Circuit Models for Propagation Analysis of In-Building Power line Communications Systems

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Abstract — In-building power line transmission measurements show potential for low attenuation propagation above 30 MHz. These measurements show that frequency bands can exist having low or minimum attenuation above 100 MHz. A simple high-frequency propagation model for analysis of in-building communications up to 900 MHz, which can be implemented using a commercial circuit simulator, is described. This physics-based model is extracted using broadband data from both time- and frequency-domain network transmission ($S_{21}$) measurements. The novelty of this modeling approach is that different propagation modes such as electromagnetic coupling, waveguide propagation through the wiring conduit, and fading are included. An RF circuit model in a simulator environment is useful for analyzing a wide range of communication problems at the circuit, subsystem, and system levels.

Index Terms - Frequency response, modeling, power line communications, propagation, transmission line, and waveguide.

I. INTRODUCTION

The power line network is a low-cost alternative to existing wired and wireless systems for wideband or broadband data communications. Broadband power line communications (PLC) is a system that uses existing power distribution lines and is characterized by a carrier system connected to power lines to transmit radio frequency signals for broadband communications. PLC is an alternative mode of communication and differs from other wired and wireless systems and is preferred due to the wide availability and easy implementation using the existing power line networks in a designated area [1, 2]. PLC was initially used as a remote monitoring system in the high voltage portion of the power line system for unmanned sites for the purpose of controlling and monitoring the power network [3]. One of the main uses of PLC is carrier transmissions over power line (CTP), which covers three basic functions including operations management, electric line monitoring and limitation, and removal of failures [4]. It is gradually being applied to the medium and low voltage lines especially in home networks due to the wide availability of power lines [5, 6]. This is due to the existing power line system, which can greatly reduce the cost of deploying a new communication system since it does not require additional infrastructure. Another advantage is that it can penetrate areas that are remote or rural and do not have a readily available connection [4, 7]. A number of research trials have been carried out at different locations and show that broadband power line is a possible technique for data communications [8–11].

Most of the PLC research to date only covers the frequency band up to 30 MHz [12]. Although this is sufficient at present, it is necessary to increase the transmission rates due to the requirements for higher data rates and higher speed. Since the introduction of PLC there has been promising research for evaluation at frequencies above 30 MHz [5]. Commissions and regulatory bodies around the world such as the federal communications commission (FCC) have set up guidelines and regulations for operators regarding broadband PLC [12]. It is stated in the FCC guidelines that frequencies above 40 MHz...
requires further research and development. In [13], a technique to provide Wi-Fi coverage to users within a physical or “fenced” boundary is proposed. Power line communications can be utilized to perform the same purpose since it supports relatively short distances such as in a room or on an office floor. A model of the PLC channel transfer function is derived for the frequency range of 1 MHz to 30 MHz by using a two-wire transmission approximation and derivation of characteristic impedance and propagation constant are done analytically [14, 15]. A broadband power line model based on transmission line theory is validated by comparing transfer function response with actual measurements for frequencies up to 100 MHz. Above 30 MHz, the experimental and modeled results begin to deviate [16]. The power line network is modeled using a multiconductor transmission line and the network is simulated with ABCD matrices. The results are however, validated using a laboratory setup and do not use an actual power line system [17, 18].

The focus of this paper is to develop a model, which can be used to evaluate the feasibility of higher frequency broadband PLC circuits and systems. This model is useful for simulating circuit configurations in a PLC environment. Since the model is physics-based, effects such as time delay, multipath, and dispersion are included. This model is broadband so that effects at harmonic frequencies can also be simulated. Time-varying effects such as fading can also be included using random simulation of varying attenuation in the model.

To develop a model for PLC for use above 30 MHz, in-building measurements were taken to determine the transmission parameters ($S_{21}$) of the network. The neutral line was chosen instead of the phase line for transmission because it is believed to have less loading and to minimize the presence of high voltage on the measurement equipment [19]. Different locations and times of the day were chosen for measurements. From the measured data, it is shown that potential PLC systems have significant attenuation and that the transmission characteristics can vary significantly during the day. Electric field emission measurements were also taken and to comply with FCC specifications, the input power to the PLC must be limited to keep the emissions to acceptable levels [20]. The broadband propagation model is fitted to measured data, which can be implemented using Agilent ADS [21]. The availability of an RF model in a circuit simulator environment is especially useful for analyzing a wide range of communications problems at the circuit, subsystem, and system levels.

This paper is organized as follows: section II describes the methodology used for measurements, section III describes the measurement results, section IV describes the methodology for extraction of an equivalent RF circuit model for the PLC, and finally the paper is concluded.

II. MEASUREMENT METHODOLOGY AND CONFIGURATION

The in-building power line system is utilized by exciting the neutral and ground lines in a transmission line mode where the signal is fed into the neutral line and the ground is used as the signal return. The neutral and ground run separately as parallel wires and are connected only at the incoming service main circuit breaker or transformer. In order to develop the broadband models for in-building power line system, $S_{21}$ (transmission) parameter measurements were carried out to determine the attenuation and return loss. These measurements were taken using a network analyzer and include high pass filters connected to the neutral and ground using shielded cables at the power sockets in the measurement setup shown in Fig. 1.

Fig. 1. $S_{21}$ transmission measurement setup.

The high pass filters have a cutoff frequency of 5 MHz and are located at each end of the path. The filters are necessary to protect the measurement equipment since the power line network is constantly active and supports many loads including lighting, air conditioning, computers, printers, and elevators all of which can
contribute noise, transients, and even faults in the power system. The high-pass filter schematic diagram is shown in Fig. 2. The high pass filter circuit with the power socket is shown in Fig. 3.

Several locations in building Block 22 at Universiti Teknologi Petronas located in Tronoh Malaysia were chosen for these measurements. Block 22 has four floors including the ground and was constructed in 2003. Path A in room 22-02-02 has a length of 11 m (in the same room), path B is in room 22-02-02 with approximate length of 9 m (from inside to outside of the room), path C is in room 22-02-05 with approximate length of 6 m (from inside to outside of the room), path D is in room 22-02-02 with approximate length of 3 m (in the same room), and path E is from Wing 1 to Wing 2 with approximate length of 45 m. There are several panels distributed nearly evenly throughout each wing. All of the ground, neutral, and phase lines in each room pass through a PVC duct and are collected at the panel located adjacent to that room. These panel locations are shown in the diagram in Fig. 4. All of the ground, neutral, and phase lines from the panels then pass through an overhead metallic conduit to the end of each wing to the riser.

The simulated and measured transmission ($S_{21}$) and reflection ($S_{11}$) coefficients for the high pass filter for $Z_0 = 50$ $\Omega$ are shown in Fig. 5. The measured insertion loss for the filter is less than 4 dB below 0.8 GHz. Also shown in the figure is the return loss ($\Gamma$) of the high pass filter connected to the power line network. The measured return loss is better than 10 dB for several frequencies below 500 MHz.
The neutral-ground transmission line configuration has an average input impedance of about 70 \(\Omega\). The filters were connected to the wall socket and the transmission parameters (S\(_{21}\)) were measured using a calibrated Agilent 8712ET network analyzer. As will be evident in the S\(_{21}\) measurements, as the path length increases, the received signal attenuates and a power amplifier is required to increase the transmission of the system. The field measurements were carried out by injecting RF signals into the power line through a power amplifier and high-pass filter and the field emissions were measured using an AFJ EBA-01 log periodic dipole and an Advantest R3132 spectrum analyzer located a distance of 3 meters from the power line feed points (Fig. 6).

**Fig. 5.** S\(_{21}\) and S\(_{11}\) for the high-pass filter (\(Z_0 = 50 \Omega\)).

**Fig. 6.** Electric field measurement setup.

### III. MEASUREMENT RESULTS

In this section, the measurement setup described in the previous section is used to measure the transmission coefficient S\(_{21}\) for the paths shown in Fig. 4. The measurements were taken at 10 am, 12 pm, 3 pm, 5 pm, and 8 pm over a span of nearly one month to determine the attenuation and amount of fading in the PLC. Broadband measurements were taken to estimate the impulse response of the power line system. Field probe measurements were taken and the results are compared with the transmission data to identify any possible coupling. In the next section, this measurement data is used to extract an equivalent RF circuit model of the power line system.

#### A. Different times of day

The measured S\(_{21}\) for paths A, B, and E are shown in Figs. 7 - 9. The response for each path shows that the transmission can vary with the time of the day and that a frequency band having minimum attenuation or resonance exists between 400 MHz and 700 MHz. This is strongly evident in path A and path E at different times of the day while for path B the location of the resonance is nearly constant. The measurement data shown in Figs. 7 and 8 were measured at 5 pm on separate days for both paths and show almost no difference in resonance frequency. The electrical line loads vary at different times, which also affect the RF S\(_{21}\) transmission.

**Fig. 7.** S\(_{21}\) measured at 5pm on separate days for path A.

At 5 pm, the S\(_{21}\) measured for path A shows resonance between 400 MHz and 500 MHz and between 500 MHz and 715 MHz. The measurement for path B shows nearly constant S\(_{21}\) from 400 MHz to 715 MHz with the exception of a slight variation in the peak in the range of 600 MHz to 715 MHz. The wing-to-wing (path E) measurements in Fig. 9 show a peak in S\(_{21}\) between 244 MHz and 650 MHz. The maximum variation in the measured S\(_{21}\) or fading is about 20 dB. In each case the resonant frequency range is nearly constant.
The average measured transmission, $S_{21}$ for path E (wing to wing) and electric field intensity near the center of the walkway are shown in Fig. 10. The field probe is located at a distance of 3 meters from the input to the power line (see Fig. 4). The input power to the high pass filter is 16 mW. These measurements reveal that there is a correlation between peaks in both $S_{21}$ and the resulting electric field intensity. For some frequencies e.g. 450 MHz there is both low attenuation in $S_{21}$ and a minimum field emission level.

B. Field emission measurements

The measured total electric field levels are higher than permitted by FCC (40 dBμV/m for frequencies above 40 MHz) and are due to the configuration of the power line network in the building. Here, asymmetries in distribution of the neutral and ground lines generate common mode currents resulting in radiation [20]. Simply lowering the input power to the PLC however, can lower these emission levels. The measured input power to the high pass filter required to maintain a field emission of 40 dBμV/m is only -15 dBm at 700 MHz. From the FCC and other commission guidelines, frequencies above 40 MHz are subjected to further development and deployment scenarios.

C. Frequency response and estimation of impulse response of power line system

The measurement setup described in the previous section and shown in Fig. 1 was also used to estimate the impulse response of the PLC. The data was obtained for the transmission paths in Block 22 (Fig. 4). The $S_{21}$ was first measured for each path and then converted into real and imaginary parts. The frequency range used was 0.3 MHz to 1.3 GHz. Next, the data was loaded into MATLAB™ [22] and expanded by using complex conjugation into a set of positive and negative frequencies. Finally, the data was inverse fast Fourier transformed using the IFFT command to estimate the (real) impulse response.

Figure 11 is the original transmission ($S_{21}$) magnitude data in frequency domain and Fig. 12 is the estimated impulse response for path A. A number of reflections are present on the line and from 400 MHz – 600 MHz there is a small increase in $S_{21}$. This is believed to be primarily due to the conduit. Figure 13 is the original transmission ($S_{21}$) magnitude data in frequency and Fig. 14 is the impulse response for path B. For this path, there are also several reflections present and another small peak in $S_{21}$ occurs near 600 MHz. Figure 15 – 18 are the original transmission ($S_{21}$) magnitude data in frequency and impulse response for paths C and D.

Transmission paths C and D have the shortest path lengths or propagation distances and have the fewest reflections. Figure 16 (path C) response shows that the signal is damped for $t > 200$ nsec. Figure 18 (path D) response shows that the signal is damped for $t > 75$ nsec. The time required for
the reflections to decay is inversely proportional to the path length. Path C and path D have a shorter distance compared to path A, B, and E, which show the least damping.

Fig. 11. Frequency magnitude response for transmission path A.

Fig. 12. Impulse response for transmission path A.

Fig. 13. Frequency magnitude response for transmission path B.

Fig. 14. Impulse response for transmission path B.

Fig. 15. Frequency magnitude response for transmission path C.

Fig. 16. Impulse response for transmission path C.

Fig. 17. Frequency magnitude response for transmission path D.

Fig. 18. Impulse response for transmission path D.
Figures 19 and 20 show the $S_{21}$ responses for path E (wing to wing). Figure 19 is the measured transmission ($S_{21}$) magnitude data in frequency domain and Fig. 20 is the estimated impulse response. Figure 20 shows damping in the signal and some reflections and a peak at $t = 280$ nsec. In the frequency response, above 400 MHz there are several peaks. The corresponding impulse response shows peaks at 30 and 280 nsec. These peaks can be identified as direct electromagnetic coupling between the two wings and a high frequency waveguide mode due to propagation through the conduit.

**Fig. 19.** Frequency response for transmission path E (wing to wing).

**Fig. 20.** Impulse response for path E (wing to wing).

Field probe measurements were taken to provide further insight into electromagnetic coupling into the power line. Figure 21 shows the measured $S_{21}$ for the wing-to-wing (path E) wall socket to wall socket (N-G to N-G) and wing-to-wing wall socket (N-G) to a field probe located adjacent to the second wall socket. The distance between the field probe and first wall socket is 9 m. The wall socket to wall socket transmission data (N-G to N-G) shows both low and high frequencies present (> 400 MHz). From the field probe measurement data, low frequencies couple the most and the high frequency data is not present. Figure 22 shows the corresponding time domain wing-to-wing measurements. Comparison of the impulse response for wall socket to wall socket and wall socket to field probe show that propagation through the ground-neutral lines for $t > 250$ nsec is due to the waveguide mode in the conduit only. Also, the field probe measurements show a response for $t > 28$ nsec, which suggests coupling from the wall socket. From the foregoing analysis of the frequency- and time-domain responses, the primary propagation components through the power lines are direct electromagnetic coupling and a waveguide mode through the conduit.

**Fig. 21.** Frequency response for transmission path E (wing to wing): direct and field probe.

**Fig. 22.** Impulse response for transmission path E (wing to wing): direct and field probe.

**IV. EQUIVALENT RF CIRCUIT MODEL FOR POWER LINES**

During measurement of the power line network in the previous section, it was observed that there could be several transmission paths. There is a direct path and additional paths that result in reflections. When the source and receiver are located in different wings, electromagnetic (EM) coupling can also occur. Also, the signal can propagate in modes other than the neutral-ground
(TEM) type mode. In Block 22 for distances greater than 5 meters, the wires must travel through an overhead conduit where the transmission coefficient \( S_{21} \) can increase instead of decrease with frequency. At certain frequencies, this increase in \( S_{21} \) was found to be caused by exciting a waveguide mode inside the conduit. From the dimensions of the conduit, it was calculated that the waveguide cutoff frequency for the lowest order \( TE_{10} \) mode is about 750 MHz. For other locations where the path length is less than 5 meters and the wires do not pass through a conduit (waveguide) the \( S_{21} \) shows a response that decreases monotonically with frequency.

For power line connections with path lengths greater than 5 meters and where the neutral and ground lines pass through a conduit, a simple model was developed using ADS\textsuperscript{TM} and CST\textsuperscript{TM} [23] to estimate the power distribution between the conduit represented by \( TE_{10} \) mode and the neutral-ground wires represented by the TEM mode. This model decomposes the propagation into TEM and \( TE_{10} \) propagating modes and is shown in Fig. 23.

\[
\text{Fig. 23. Equivalent circuit model for propagation through conduit.}
\]

To create the conduit model for implementation in a circuit simulator such as ADS\textsuperscript{TM}, a numerical procedure was first used to estimate the coupling \( C \) for 2-wire transmission through a rectangular waveguide. The power coupled into each mode is \( \text{conduit} = C \), and for the neutral-ground wires \( \sqrt{1-C^2} \). For the model, parameters varied are the spacing \( d \) between the 2 wires and the height \( h \) of the wires inside the waveguide as shown in Fig. 24. Simulations were carried out with varying parameters \( d \) and \( h \) using CST\textsuperscript{TM} and the resulting coupling parameter value \( C \) was extracted. In the simulations, the conduit length is 5 meters and wire diameters are 1 mm. The values for \( Z_0 \) and \( k \) (relative dielectric constant) used in the transmission line model are assumed to be 200 \( \Omega \) and 1.8. The spacing \( d \) and the height \( h \) are varied and simulated accordingly. The neutral and ground wires inside the conduit with spacing, \( d \) are varied between 1 and 5 cm. The estimated coupling, \( C \) is extracted using the following procedure:

1. Set the \( d \) and \( h \) values.
2. EM-simulate the structure shown in Fig. 24 from 0.3 MHz to 900 MHz using CST\textsuperscript{TM}.
3. Import the resulting S-parameters into the circuit simulator.
4. Fit the S-parameters to the circuit shown in Fig. 23 to extract \( C \) value.

For height \( h \) value of 0.1 mm, the value for \( C \) is lowest since the neutral and ground wires are placed near the bottom of the conduit and become nearly short-circuited. The coupling value \( C \) for this work occurs for the neutral and ground located at least 10 mm from the bottom of the conduit and the neutral and ground are spaced at least 20 mm apart. When the height \( h \) is 10 mm to 20 mm and spacing \( d \) is 20 mm to 50 mm, the range for the coupling, \( C \) is \( 0.18 < C < 0.23 \).

A frequency dependent coupling can also be used. Here, the coupling increases with frequency and has the form \( C = \alpha f \) where \( f \) is frequency. Using the procedure described above \( \alpha = 0.6 – 0.8 \) \( \text{GHz}^{-1} \) for the height \( h \) between 10 mm and 20 mm and spacing \( d \) between 20 mm and 50 mm.

\[
\text{Fig. 24. Conduit cross-sectional view including neutral and ground.}
\]

From the layout given in Fig. 4, the equivalent RF circuit model for the wing-to-wing path consists of high pass filters at the transmitter and receiver, an equivalent circuit model for the conduit in each wing, a transmission line for the riser that connects both wings, and a short section of high attenuation transmission line used to model the coupling between the wings. Frequency dependant coupling between the TEM and \( TE_{10} \) modes in the conduit is included using \( \alpha = 0.7 \) \( \text{GHz}^{-1} \). Figure 25 shows the equivalent circuit
propagation model for path E for implementation using ADS™. The final component values are determined by optimizing the model parameters with the frequency- and time-domain $S_{21}$ data using ADS™. Time-varying attenuation or fading can be included in the model for random or Monte Carlo type analysis by varying the transmission line “$atw$” parameter. For 20 dB variation in attenuation, the range $0.4 < atw < 0.8$ is used.

Figure 26 shows the measured and simulated $S_{21}$ for the wing-to-wing transmission in the frequency- and time-domains. The measured data and simulated model compare well in both domains. For wing-to-wing transmission, the signal propagates through two conduits and the riser as well as direct coupling between the wings and is evident in the time domain response at 28 nsec and 290 nsec in Fig. 26 (b). Figure 26 (a) shows that the frequency response for measurement and simulation are similar up to 900 MHz. As mentioned earlier, the response for frequencies above 400 MHz is primarily due to the TE mode excited in the conduits.

V. CONCLUSION

The transmission measurements in an office building at different locations and times show that the power line system can have low attenuation for frequencies above 30 MHz. These measurements show that frequency bands exist that are nearly fixed with only 40 – 50 dB attenuation and maximum variation of 20 dB. Field strength measurements of the broadband power line were taken and demonstrate that in order to not exceed field levels required by FCC regulations, a low input power level must be used. A simple broadband propagation model for analysis of the PLC up to 900 MHz is extracted by using both frequency- and time-domain representations of the measured $S_{21}$ parameters. Analysis of $S_{21}$ in both domains is not only helpful in fitting the measured response to a useful model but is also helpful in identifying the various propagation modes. The RF propagation model can be implemented using a standard circuit simulator and provide a unified analysis capability for in-building PLC at the component, sub-system, and system levels. The model is easily modified to account for fading.

REFERENCES


[22] MATLAB version R2009a, Mathworks Inc, Massachusetts, USA.

[23] CST Microwave Studio version 2011, Computer Simulation Technology, Darmstadt, Germany.

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Discontinuous Galerkin Time Domain Method for Scattering Analysis of Air-Inlets

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Abstract — In this paper, a high-order three dimensional (3-D) discontinuous Galerkin time domain (DGTD) method has been introduced for the first time for the efficient scattering analysis of air-inlets. This method combines the geometrical versatility of finite element method (FEM) with the explicit time-stepping of finite volume time domain (FVTD) method, thus having the advantages of handling electrically large, arbitrarily shaped, and complex media objects. To validate the capability of this method, the radar cross section (RCS) of three typical air-inlet models have been simulated. The results of the DGTD method agree well with that of the method of moments (MoM), which proves the DGTD method a useful alternative to the traditional methods to solve the scattering problems.

Index Terms — Air-inlets, DGTD, and RCS.

I. INTRODUCTION

Scattering properties of air-inlets is of great importance in radar signature analysis [1], as the air-inlets could significantly affect the overall RCS from jetfighters. Therefore, the development of accurate and efficient methods to evaluate the RCS from such structures is an important task and has attracted much attention in the computational electromagnetics community.

Classic frequency methods of scattering analysis include high frequency methods and low frequency methods. However, the high frequency methods employing ray tracing techniques [2] are less accurate when dealing with cavity structures, while the low frequency methods like the MoM [3] is hard to deal with electrically large and complex objects with dielectric coating. Moreover, as the increasing needs for the wideband scattering information, time domain method is more efficient, nonetheless, classic time domain methods such as the finite difference time domain (FDTD) method [4] and the finite element method time domain (FEMTD) [5] suffer from low accuracy or great resource consumption. As a result, new time domain method for efficiently solving the electrically large and complex scattering problem is highly desirable.

Recently a set of high-order DGTD methods has been developed [6-9], which commonly combines the geometrical versatility of the FEM [5] and the explicit time-stepping of the FVTD method [10]. It exceeds FDTD and FEMTD in accuracy and efficiency respectively [11], thus becoming a very suitable method for the electrically large, arbitrarily shaped, and complex media targets. Therefore, in this paper, for the first time, the high-order 3-D DGTD method is applied for the RCS evaluation of air-inlets. To validate the capability of this method to solving scattering problem, three typical air-inlet models have been simulated. The results of them have shown good agreement with that of the MoM, which proves the DGTD method a useful alternative to the other numerical methods.
The remaining parts of the paper are organized as follows. In section II, the DGTD method is briefly presented. In section III, several numerical results of air-inlet models are given to verify the accuracy of the method. Finally, conclusions are drawn in section IV.

II. DGTD FUNDAMENTALS

To introduce the high-order 3D DGTD method simply, the Maxwell’s curl equations in linear, isotropic, and homogeneous media are presented in conservation form first,

\[ \mathbf{Q} \cdot \partial_t \mathbf{q} + \nabla \cdot \mathbf{F}(\mathbf{q}) = 0, \]  

(1)

where the material matrix \( \mathbf{Q} \), the state vector \( \mathbf{q} \), and the flux \( \mathbf{F} \) are denoted as follows,

\[ \mathbf{Q} = \begin{bmatrix} \varepsilon & 0 \\ 0 & \mu \end{bmatrix}, \quad \mathbf{q} = \begin{bmatrix} \mathbf{E} \\ \mathbf{H} \end{bmatrix}, \quad \mathbf{F}(\mathbf{q}) = \begin{bmatrix} -\varepsilon \mathbf{E} \times \mathbf{H} \\ \varepsilon \mathbf{H} \times \mathbf{E} \end{bmatrix}, \]

\[ i = x, y, z. \]

Then, considering a 3D physical domain \( \Omega \), which is discretized by a carefully chosen set of the interpolation nodes \( N_p \) normal to the contour of element \( \Omega \) shown, equation (1) is sampled with test function \( \mathbf{q}^k \) using Lagrange interpolation polynomials \( L_i(\mathbf{r}) \)

\[ \mathbf{q}^k(\mathbf{r}, t) \approx \sum_{i=1}^{N_p} \mathbf{q}^k_i(t) L_i(\mathbf{r}), \]  

(2)

where \( N_p \) represents the number of the local expansion. \( \mathbf{q}^k \) contains a \( N_p \)-vector of expansion coefficients to be solved. The relationship between \( N_p \) and the polynomial expansion order \( N \) for tetrahedron is \( N_p = (N+1)(N+2)(N+3)/6 \). A carefully chosen set of the interpolation nodes \( \mathbf{r}_i \) could lead to good numerical behaviour [12].

Next, using the classic Galerkin method, equation (1) is sampled with test function \( L_i(\mathbf{r}) \) as shown,

\[ \int_{\Omega} (\mathbf{Q}^k \cdot \partial_t \mathbf{q}^k + \nabla \cdot \mathbf{F}(\mathbf{q}^k)) \cdot L_i(\mathbf{r}) d\mathbf{r} = 0. \]  

(3)

In order to couple with the neighboring elements, the divergence part of the integral in equation (3) is first manipulated by an integration by parts as

\[ \int_{\Omega^k} (\mathbf{Q}^k \cdot \partial_t \mathbf{q}^k \cdot L_i(\mathbf{r}) - \mathbf{F}(\mathbf{q}^k) \cdot \nabla L_i(\mathbf{r}) d\mathbf{r} = \]

\[ -\int_{\partial\Omega^k} (\mathbf{n}^k \cdot \mathbf{F}(\mathbf{q}^k)) \cdot L_i(\mathbf{r}) d\mathbf{r}, \]

where \( \mathbf{n}^k \) denotes the unit outward-pointing vector normal to the contour of element \( \partial\Omega^k \) denoted by \( \partial\Omega \). Then, replace the flux \( \mathbf{F} \) on the RHS by the numerical flux \( \mathbf{F}^* \) and perform another integration by parts, the strong variational formulation of equation (3) can be obtained as,

\[ \int_{\Omega^k} (\mathbf{Q}^k \cdot \partial_t \mathbf{q}^k + \nabla \cdot \mathbf{F}(\mathbf{q}^k)) \cdot L_i(\mathbf{r}) d\mathbf{r} = \]

\[ \int_{\partial\Omega^k} (\mathbf{n}^k \cdot (\mathbf{F}(\mathbf{q}^k) - \mathbf{F}^*(\mathbf{q}^k))) \cdot L_i(\mathbf{r}) d\mathbf{r}. \]  

(4)

The numerical flux \( \mathbf{F}^* \) on the surface \( \partial\Omega^k \) is to exchange the coupling between neighboring elements. It can be obtained properly by solving a local Riemann problem [6]. Here, the pure upwind flux [13] is used, which could strongly damp the unphysical modes [6],

\[ \mathbf{n} \cdot (\mathbf{F}(\mathbf{q}^k) - \mathbf{F}^*(\mathbf{q}^k)) =
\]

\[ \begin{bmatrix} [\mathbf{Z}^{-1} \mathbf{n} \times (\mathbf{Z}^* [\mathbf{H}^k] - \mathbf{n} \times [\mathbf{E}^k])] \\
[\mathbf{Y}^{-1} \mathbf{n} \times (\mathbf{Y}^* [\mathbf{E}^k] + \mathbf{n} \times [\mathbf{H}^k])] \end{bmatrix}, \]

(5)

where \([\mathbf{E}]=\mathbf{E}^* - \mathbf{E}^k \) and \([\mathbf{H}]=\mathbf{H}^* - \mathbf{H}^k \) measure the jump in the field values across element interfaces; i.e., superscript “*” refers to field values from the neighbor element while the “-” refers to field values local to the element. For the possible difference of material properties between two elements, local impedance and conductance, \( \mathbf{Z}^* = (\mathbf{Y}^*)^{-1} = \sqrt{\mu / \varepsilon} \) and local sums \( \mathbf{Z} = \mathbf{Z}^* + \mathbf{Z}^{-*} \), \( \mathbf{Y} = \mathbf{Y}^* + \mathbf{Y}^{-*} \) has to be defined.

Finally, by substituting the expansions in equation (2) into equation (4) and assuming parameters \( \varepsilon \) and \( \mu \) constant in each element, the explicit expressions of the DGTD can be easily obtain as follows,

\[ \frac{\partial \mathbf{E}^k}{\partial t} = \frac{\mathcal{M}^k}{\varepsilon^k} \begin{bmatrix} -\mathbf{S}^k \times \mathbf{H}^k + \mathbf{F}^k \cdot \mathbf{n} \times (\mathbf{Z}^* \mathbf{H}^k - \mathbf{n} \times [\mathbf{E}^k]) \\
\mathbf{F}^k \cdot \mathbf{n} \times (\mathbf{Y}^* [\mathbf{E}^k] + \mathbf{n} \times [\mathbf{H}^k]) \end{bmatrix}, \]

(6)

where \( \mathbf{E}^k \) and \( \mathbf{H}^k \) are \( N_p \)-vectors. The mass matrix \( \mathcal{M}^k \), the stiffness matrices \( \mathcal{S}^k \), and the face mass matrix \( \mathcal{F}^k \) with respect to the element contour \( \partial\Omega^k \) are defined as shown below

\[ \begin{align*}
(\mathcal{M}^k)_{ij} &= \int_{\partial\Omega^k} \mathbf{L}_i(\mathbf{r}) \mathbf{L}_j(\mathbf{r}) d\mathbf{r}, \\
(\mathcal{S}^k)_{ij} &= \int_{\partial\Omega^k} \mathbf{L}_i(\mathbf{r}) \mathbf{p} \mathbf{L}_j(\mathbf{r}) d\mathbf{r}, m \in \{x, y, z\}, \\
(\mathcal{F}^k)_{ij} &= \int_{\partial\Omega^k} \mathbf{L}_j(\mathbf{r}) \mathbf{L}_i(\mathbf{r}) d\mathbf{r}, \quad j \in \{j | r_j \in \partial\Omega^k\}. 
\end{align*} \]

Since equation (6) are ordinary differential
equations with respect to time, a 4th-order, five-stage, low-storage Runge-Kutta scheme [14] is employed for the time integration.

III. NUMERICAL RESULTS

In this section, we present several numerical results to validate the accuracy of the DGTD method while solving the scattering problem of air-inlets. The 3rd-order Lagrange polynomial is employed as the basis function. And a commercial MoM is employed for comparison. Figure 1 shows the computational setup of the air-inlet model. For simplicity here, the electrically large air-inlet is considered as a long perfect electric conducting cylindrical waveguide with a closed-end (deep cavity). It is placed in the center of the total field (TF). A two-cell perfectly matched layer (not depicted here) is wrapped around the scattering field (SF) in order to truncate the computational area. A modulation Gaussian pulse ($\phi = 180^\circ$, $\theta = 0^\circ$, polarization angle $= 0^\circ$) is injected using the TF/SF technique [4].

![Fig. 1. Computational setup of the air-inlet model.](image)

Figures 2 to 4 show three numerical results and their corresponding model insets. The models are the straight, the frustum, and the bending air-inlet models as shown in Figs. 2b to 4b, respectively. Each model is $10\lambda$ length and $0.5\lambda$ radius, except that the radius of frustum one varies from $0.5\lambda$ to $0.25\lambda$, and the bending one bends $90^\circ$ from the $z$-direction at the rear. They are all meshed with tetrahedrons of $0.1\lambda$ edge-length.

Two comparable bistatic RCS results at 300 MHz are shown in Figs. 2a to 4a, which are the blue circle curves by the DGTD method and the red line curves by the MoM using FEKO v6.1. All the RCS values are evaluated at the direction of $\phi = 0^\circ$, $\theta$ from $0^\circ$ to $360^\circ$ with $1^\circ$ increment. From these values, although the air-inlets models are various and electrically long, we could observe great agreement between the results of these two methods. Among these values, the majors mainly appear at the front ($\theta = 0^\circ$) and back ($\theta = 180^\circ$) of the air-inlet models. It could be caused by the direction of the incident plane wave and its multiple reflections by the deep cavity.

![Fig. 2. (a) the bistatic RCS results and (b) the inset of the straight air-inlet model.](image)

![Fig. 3. (a) the bistatic RCS results and (b) the inset of the frustum air-inlet model.](image)

The time consumed by the numerical examples using the DGTD method is a bit longer than the commercial MoM under the same circumstance, which is the platform of the ThinkPad T420 with the Intel® Core™ i7-2640M CPU with 2.80 GHz (only one core is used) and 4.0 GB RAM. However, considering the MoM is a...
frequency domain method and the models in FEKO are meshed with 0.1λ edge-length on surface, the DGTD method would be a potential tool when dealing with wideband scattering problems of electrically larger and complex media air-inlet.

Fig. 4. (a) the bistatic RCS results and (b) the inset of the bending air-inlet model.

IV. CONCLUSION

In this article, the high-order 3-D DGTD method has been introduced for the first time for the scattering analysis of air-inlets. This method has the advantages of handling electrically large, arbitrarily shaped, and complex media composition objects. The results of DGTD agree well with those of the MoM, which proves it to be a useful alternative to the traditional methods to solve the scattering problem. Considering the advantages of this method, it may be a promising method for electrically large and complex air-inlet in future work.

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REFERENCES

Analytical Solution of Scattering by a 2D Dielectric Filled Crack in a Ground Plane Coated by a Dielectric Layer: TM Case

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Abstract — In this paper, KP method is applied to study the scattering of a 2D loaded crack on a ground plane, coated by a dielectric layer for TM case. For simplicity, the geometry is divided into three regions, whose fields are expressed in terms of Bessel eigen functions. The governing equations involve several infinite summations with infinite number of unknown coefficients. By the use of Weber-Schafheitlin discontinuous integrals, these infinite summations could efficiently be truncated with high numerical accuracy. Boundary conditions are applied to determine unknown coefficients. We employ finite element method (FEM) and convergence analysis to confirm our results. Finally, the influence of coating dielectric layer and filling material is investigated on the scattered field.

Index Terms — 2D coated crack, dielectric layer, Kobayashi and Nomura method, plane wave scattering, and Weber-Schafheitlin discontinuous integrals.

I. INTRODUCTION

An assessment of the surface cracks is a significant area under discussion in nondestructive testing and evaluation (NDT/NDE). There are two main near-field category techniques reported by the engineering community for crack detection. These methods are based on waveguide techniques [1-3] and the resonator method [4-6]. These techniques are not applicable to the non-accessible cracks like those on boilers or blast furnaces, thus, far-field electromagnetic (EM) scattering measurement is recommended.

The scattering from the rectangular crack can be approached in a variety of ways including the method of moment (MoM) [7], quasi-static approach [8, 9], approximate boundary conditions (ABC) [10, 11], Fourier spectrum analysis [12], finite element boundary integral method (FE-BI) [13], transparent boundary condition (TBC) [14], and overlapping T-block method [15-17]. Additionally, Morgan and Schwering utilized mode expansion scattering solution for wide rectangular cracks in 2D [18] and cavities in 3D [19]. Deek et al. extracted the natural frequency poles with matrix pencil method (MPM) for detecting cracks in buried pipes [20]. Bozorgi et al. reported a direct integral equation solver (DIES) method for determining the backscattering signatures of a crack in a metallic surface by omitting singularities in hyper singular integrals [21, 22]. Honarbakhsh et al. presented mesh free collocation method for 2D filled crack in infinite ground [23].
The KP method is accurate and simple in the sense of not dealing with singularity of the Green’s functions. Second, the solution converges rapidly due to the satisfaction of a part of the boundary condition by each basis function involved in the integrand [31].

Hongo et al. used KP method to find scattering of EM spherical wave from a PEC disk [24]. Imran et al. utilized this method to compute diffraction of plane wave from a perfectly electromagnetic conductor (PEMC) strip [25]. Sato et al. used KP method to analyze TM plane wave scattering by a 2D filled rectangular crack on a ground plane without any dielectric coating [26]. They applied KP method to two rectangular troughs on a ground plane [27] with a standard impedance boundary condition (SIBC) [28] and estimated the depth of the crack [29]. They also used KP method to model the propagation through slits array [30].

In most cases, paint, primer, rust, and oil coat the corrosion (crack) and it cannot be visually detected. Near-field techniques for detecting cracks under paint were applied [1, 3] but a fast, accurate and rigorous method for analyzing the scattering signature of the coating crack with far-field methods is in demand. Previously, EM plane wave scattering by a 2D rectangular gap in a PEC ground plane, coated by a dielectric layer was reported for TE case [32]. In this paper, the TM case of this problem is investigated.

The paper is organized as follows. In section II the KP method is used to derive the governing field equations with unknown excitation coefficients and truncated unknown excitation coefficients are computed. The numerical results and validations are shown in section III. Conclusion remarks are provided in section IV. Here, the time harmonic factor $e^{-j\omega t}$ is assumed throughout the context.

II. PROBLEM DESCRIPTION AND FORMULATION

We assume a dielectric rectangular crack that is filled by a dielectric material and is coated by a dielectric slab. The cross section for the crack is $2a \times b$ and the height of the slab is $y_t$ as shown in Fig. 1. The relative permittivity and permeability of the filling material are $\varepsilon_r$ and $\mu_r$, respectively, and $(\varepsilon_t, \mu_t)$ are of the coating material. The filling and the coating materials could be both lossy, meaning that $\varepsilon_r, \mu_r, \varepsilon_t$, and $\mu_t$ could be complex.

![Observation point](observation_point.png)

Fig. 1. Geometry of the filled rectangular crack underneath a coating layer in an infinite ground plane.

The incident angle is $\theta_0$ and the observation point is represented by $\rho$ and $\theta$ in the cylindrical coordinate system. Assuming $\psi$ is the total electric field in a dielectric slab. The crack is filled by a material with relative permittivity and permeability of $\varepsilon_r$ and $\mu_r$, respectively. The relative permittivity and permeability of the slab are $\varepsilon_t$ and $\mu_t$, respectively.

A. Expansion of electromagnetic fields

The geometry of the problem is divided into three regions, which are described as follows.

Region I: Semi-infinite half space ($y > y_t$)

In this region the total z-component of the electric field is denoted by $E_z$ which is,

$$\phi_i^r + \phi_i^s$$

where, $\phi_i^r$ and $\phi_i^s$ represent the incident and the reflected field, respectively. Additionally, $\phi_i^s$ characterizes the scattering contribution of the crack in this region. The material in this region is free space ($\varepsilon_0, \mu_0$).

Region II: Slab Region ($y_t > y > 0$)

The total z-component of the electric field in this region is given by,
\[ \phi_i' = \psi + \phi_i^s. \]  

Here, \( \psi \) is the total electric field in the dielectric slab and its calculation is given in the Appendix. Scattering contribution of the crack in this region is denoted by \( \phi_i^s \).

Region III: Cavity Region \((-b \leq y < 0, |x| < a)\)

This region is like a parallel plate waveguide. Therefore, the total field is expressed by a summation of waveguide modal eigenfunctions. Considering the boundary conditions at \( x = \pm a \) and \( y = -b \), \( \phi_i^s \) is given by,

\[
\phi_i^s = \sum_{n=0}^{\infty} J_n \left[ \frac{e^{-i\alpha_{g}y} - e^{i\alpha_{g}(y+2b)}}{2} \right] \sin \left( \frac{n\pi}{2a} \left( 1 - \frac{x}{a} \right) \right)
\]  

where \( h_n = \sqrt{\epsilon_n \mu_n k_0^2 - (n\pi/w)^2} \) stands for the propagation constant of the \( n \)th parallel plate waveguide mode and \( J_n \) is the excitation coefficient inside cavity region.

B. Applying KP method for scattering fields

In this section, the scattering fields \( \phi_i^s (i = 1, 2) \) are derived by utilizing the KP method and the boundary conditions are applied to find the unknown coefficients. Since the scattering fields \( \phi_i^s (i = 1, 2) \) satisfy the homogeneous Helmholtz equation, they could be represented as an integral of the general solutions by using the separation of variables method [26]. Without loss of generality, all variables and parameters are normalized with respect to \( a \) as follows,

\[
u = \frac{v}{a}, \quad \alpha = \frac{\alpha}{a}, \quad \beta = \frac{\beta}{a}, \quad t = \frac{t}{a},
\]

therefore,

\[
\phi_i^s = \frac{1}{a^2} \int \left[ d(\xi/a) \cos(\xi/a) + e(\xi/a) \sin(\xi/a) \right] e^{-\sqrt{\xi^2-\alpha^2}} d\xi
\]

and

\[
\phi_i^s = \frac{1}{a^2} \int \left[ f(\xi/a) \cos(\xi/a) + g(\xi/a) \sin(\xi/a) \right] e^{-\sqrt{\xi^2-\alpha^2}} d\xi
\]

\[
+ \frac{1}{a^2} \int \left[ h(\xi/a) \cos(\xi/a) + k(\xi/a) \sin(\xi/a) \right] e^{i\beta \sqrt{\xi^2-\alpha^2}} d\xi,
\]

where, \( d(\cdot), e(\cdot), f(\cdot), g(\cdot), h(\cdot), \) and \( k(\cdot) \) denote the unknown weighting functions. It is notable that \( \phi_i^s \) includes only the up-going wave, while \( \phi_i^s \) contains both up-going and down-going waves. Noting the relation between trigonometric and Bessel functions,

\[
\begin{align*}
\cos(\xi/a) &= \frac{J_{\frac{1}{2}}(\xi/a)}{J_{\frac{1}{2}}(\xi)}, \\
\sin(\xi/a) &= \frac{J_{\frac{3}{2}}(\xi/a)}{J_{\frac{1}{2}}(\xi)}.
\end{align*}
\]

The weighting functions are expanded in terms of the Bessel functions. Thus,

\[
\begin{align*}
d(\xi/a) &= \sum_{m=0}^{\infty} \frac{D_m}{F_m} \frac{J_{2m+1}(\xi/a)}{\xi}, \\
f(\xi/a) &= \sum_{m=0}^{\infty} \frac{E_m}{G_m} \frac{J_{2m+2}(\xi/a)}{\xi}, \\
g(\xi/a) &= \sum_{m=0}^{\infty} \frac{F_m}{K_m} \frac{J_{2m+1}(\xi/a)}{\xi}.
\end{align*}
\]

By substituting equations (5) and (6) into equations (5) and (6) we have,

\[
\phi_i^s = \sqrt{\frac{\alpha}{2}} \sum_{m=0}^{\infty} \frac{1}{\sqrt{\xi}} \left[ D_m J_{2m+1}(\xi/a) J_{\frac{1}{2}}(\xi/a) - E_m J_{2m+2}(\xi/a) J_{\frac{1}{2}}(\xi/a) \right] e^{2\sqrt{\xi^2-\alpha^2}} d\xi,
\]

and

\[
\phi_i^s = \sqrt{\frac{\alpha}{2}} \sum_{m=0}^{\infty} \frac{1}{\sqrt{\xi}} \left[ F_m J_{2m+1}(\xi/a) J_{\frac{1}{2}}(\xi/a) + G_m J_{2m+2}(\xi/a) J_{\frac{1}{2}}(\xi/a) \right] e^{2\sqrt{\xi^2-\alpha^2}} d\xi.
\]

C. Boundary conditions

The unknown coefficients of the fields consisting of \( D_m, E_m, F_m, G_m, H_m, K_m, L_n \) are determined by applying the boundary conditions.
The boundary conditions at the interface between regions I and II, where $\nu = I(y) = y'$, are given by,

$$\begin{align*}
\phi_i^* &= \phi_i^*, \\ \nabla \phi_i &= \frac{\partial}{\partial \nu} \phi_i^*,
\end{align*}$$

BC.1 (12)

Also the boundary conditions at the interface between regions II and III, where $\nu = 0$, are given by,

$$\begin{align*}
\phi_j^* &= \phi_j^*, \\ \nabla \phi_j &= \frac{\partial}{\partial \nu} \phi_j^*. 
\end{align*}$$

BC.2 (13)

By substituting equations (12) and (13) and equations (7) and (9) into equations (10) and (11) and after some mathematical manipulation, the following equations are derived,

BC.1:

$$\sum_{m=0}^{\infty} \frac{1}{\mu} D_m G_{2m+1}^e(\xi) + E_m G_{2m+2}^e(\xi) e^{i\sqrt{\beta_m - \gamma_0} \xi} d\xi = 0,$$

BC.2:

$$\mu \sum_{m=0}^{\infty} \frac{\sqrt{\xi} - \kappa_0}{\xi} D_m G_{2m+1}^e(\xi) + E_m G_{2m+2}^e(\xi) e^{i\sqrt{\beta_m - \gamma_0} \xi} d\xi = 0,$$

BC.3:

$$\sum_{m=0}^{\infty} (-1)^m \left[ L_{2m+1}(\nu) \beta_{2m+1} \cos \left( \frac{2k+1}{2} \pi \nu \right) \right] = 0.$$
BC.3: Odd Identity:

\[ (-1)^{k} (2k+1) \frac{J_{2k}}{2k+1} (1 + 1) \pi \]

(24)

BC.4: Even Identity:

\[ \frac{1}{2} \sum_{m=0}^{\infty} \left( \frac{J_{2m+1}(k+1) \pi}{2k+1} \right) \]

(25)

BC.5: Odd Identity:

\[ \frac{1}{2} \sum_{m=0}^{\infty} \left( \frac{J_{2m+1}(k+1) \pi}{2k+1} \right) \]

(26)

where

\[ p(x) = J_{2m+1}(x) / x \]

Equations (19) to (26) are eight sets of equations to be solved for eight sets of unknown coefficients \( D_m, E_m, G_m, H_m, K_m, L_{2k}, L_{2k+1} \). In a cylindrical coordinate system where the observation point is represented by \( \rho \) and \( \theta \) the far-field scattering is [29],

\[ \phi_{\theta} = \sqrt{\frac{\pi}{4\rho}} \sum_{m=0}^{\infty} \left( \frac{D_m E_{2m+1}}{2m+1} (K_m \cos \theta) \right) \]

(28)

The above summations are all convergent and therefore, \( n \) and \( m \) are limited to \( N \) and \( M \), respectively.

III. VALIDATION AND NUMERICAL RESULTS

In this section different simulations for both filled and coated cracks are given. Two approaches are utilized for validation of this method. First, FEM calculates the equivalent magnetic current density \( |M_e| \) on the aperture for several incident angles. Second, for rigorous validation, convergence analysis is performed by changing the truncation numbers \( N \) and \( M \) [33]. Different cases of the simulations are listed in Table 1.

A. Magnetic current density analysis

Referring to Fig. 1 and Table 1, in the case (a), the non-filled crack is coated by a dielectric layer with a complex permittivity and permeability, while in the case (b), the crack is additionally filled by a complex material. Figure 2 shows the equivalent magnetic current density distribution, \( |M_e| \) on the crack \((x < a, y = 0)\) for various incident angles \((\theta_i = 15^\circ, 30^\circ, 45^\circ, 60^\circ, 75^\circ, 90^\circ)\). In this figure, truncation number of the series is assumed to be \( N, M = 14 \). Comparison of the results with the FEM solution demonstrates the accuracy of the method for all incident angles. We plot the electric field distribution, calculated by KP method, at normal incident angle for case (b) (see Fig. 3). As shown, the boundary conditions are satisfied at the edges of the crack \((x / \lambda_0 = \pm 1, y / \lambda_0 = 0)\), while the field maximum occurs near the slab layer \((y / \lambda_0 = 1)\). It can also be observed that the field values at \( y / \lambda_0 = 1 \) is equal to the black solid line in Fig. 2 where \( \theta_i = 90^\circ \).

<table>
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<tr>
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</table>

B. Convergence analysis

For rigorous validation, the error analysis is carried out and the convergence curves are represented in Fig. 4 for various cases c, d, and e. The error function and Euclidean norm are
\[
\begin{align*}
    e_r &= \left\| M'^{i+1} - M'^i \right\| / \left\| M'^i \right\|, \quad i = 1..N, \\
    \left\| M'^i \right\| &= \sqrt{\sum_{k=1}^{K} |M'_{x_k}|^2}
\end{align*}
\]

(29)

where \(x_k\) denotes the position of the \(k\)th point on the crack and \(K\) represents the total number of the observation points. The results are calculated using \(K = 25\) for all three cases.

According to Fig. 4, the summations converge rapidly, such that for \(N\) and \(M\) close to 8–10, the error is equal to \(10^{-1.7} = 0.02\). This result is expectable due to the fact that Weber-Schafheitlin type integrals satisfy the boundary condition on the PEC (\(|x| > a, \nu = 0\)) automatically. The rapid convergence of the analytic method makes it desirable for efficient calculation of the scattered field in the inverse problems.

\textbf{C. Results}

In this section, we compute backscattered RCS, bistatic RCS, and far-field scattering patterns for several filled and coated cracks. We make comparisons with other computed results of the backscattered RCS for the simpler geometry, such as the case of no coating layer. Figure 5 shows the normalized backscattered RCS of cases f and g from Table 1 and compare the results of this method with those on [26]. A very good agreement is observed between these methods. Cases of coated layer with height \(y_t = \lambda_0 / 3\) and relative permittivity \(\varepsilon_1 = 3 + 0.1i\) and relative permeability \(\mu_1 = 1.6 + 0.2i\) are also simulated. Black dash line and cyan dot line depict the results of proposed method for coated cases f and g, respectively. Observation shows that coating layer on the crack alters the RCS signature significantly.

Figure 6 shows the variation of the normalized RCS versus observation angle for case g where the crack is coated by various materials. The crack is illuminated by an incident plane wave at \(\theta_0 = 45^\circ\). Additionally, the depth of the dielectric layer is assumed \(y_t = 0.6 \lambda_0\) for all of the coating layers. As shown the dielectric constant of the layer does not have a monotonic effect on RCS. Additionally, RCS drops down when very lossy material coats the crack (solid pink line with diamonds).

Next, to show the validity of the proposed method for narrow cracks the normalized backscattering RCS of the case g is presented in Fig. 7. We also coat this case by a material with \(\varepsilon_1 = 2.7 + 0.03i, \mu_1 = 1.4 + 0.1i\) and the thickness of \(y_t = \lambda_0/4\).
plane-wave incident angle of $\theta_0 = 30^\circ$. Also, the crack is coated by a layer of salt rust with relative dielectric of $\varepsilon_1 = 5.33 + 1.53i$ height of $y_t = 0.5 \lambda_0$ for plane-wave incident angle of $\theta_0 = 75^\circ$.

The variation of the normalized RCS versus the dielectric layer thickness for various permittivities and permeability are shown in Figs. 8 and 9, respectively. The parameters of the crack are $w = 0.2 \lambda_0$ and $b = 0.2 \lambda_0$, also it is illuminated by normal plane wave. In addition, the cracks in all cases are filled by rust with $\varepsilon_r = 2.7 + 0.03i$ and $\mu_r = 1.4 + 0.1i$. As shown in Fig. 8 when the dielectric constant increases, normalized RCS almost increases. According to Figs. 8 and 9, by increasing the dielectric slab thickness RCS has oscillatory behaviour.

Next, the scattering far-field pattern for an empty and covered crack with $w = b$ and $2ka = 15$ is shown in Fig. 10. We compare our results with those on [26] for non-coated crack. The crack is coated by a common paint with relative dielectric constant $\varepsilon_1 = 3 + 0.1i$ and height of $y_t = 0.6 \lambda_0$ for paint thickness for different permeabilities.
As shown a thin layer of lossy dielectric alters the scattering pattern significantly. The maximum scattering peak value occurs at the vicinity of the corresponding specular direction for both cases of incident angles. Finally, in Fig. 11, the scattering pattern varies significantly even for a thin layer of coating layer.

**IV. CONCLUSION**

In this paper, we analyzed the EM plane wave scattering of a 2D rectangular filled and coated crack on a ground plane by the use of KP method for the TM case. The validation of the proposed method was accomplished by utilizing two techniques; consisting of FEM to investigate the equivalent magnetic current density on the aperture and the convergence analysis. The proposed method is shown to be accurate for both narrow and wide cracks and also is applicable to all lossy and lossless materials for filled and coated cracks. In addition, the sensitivity of RCS to permittivity, permeability, and thickness of the overlaying layer was presented.

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**APPENDIX**

**STANDING WAVES IN THE SLAB**

A dielectric slab on an infinite PEC ground is shown in Fig. A. The height of the slab is $y_t$ and the relative permittivity and relative permeability of $\varepsilon_r$ and $\mu_r$, respectively are the material characterization of the slab. Here, $k_0 = \omega_{0}\sqrt{\varepsilon_r\mu_r}$ and $k_1 = k_0\sqrt{\varepsilon_r\mu_r}$ are respectively the free space and the dielectric slab wave numbers. The slab is illuminated by a TM polarized EM plane wave, 

$$\phi(E_z) = e^{-ik_0(x\cos\theta - y\sin\theta)},$$

(A.1)

and the reflected plane wave is,

$$\phi'(E_z) = Re^{-ik_0(x\cos\theta - y\sin\theta)},$$

(A.2)

where, $R$ is the reflection coefficient, $\theta_0$ is the incident angle, $\theta$ is the transmission angle. Assuming $\psi$ is the total electric field in the dielectric slab. Therefore,
\( \psi = [Ae^{-ik_y \sin \theta (y - y_0)} + Be^{-ik_y \sin \theta y}] e^{-ik_z \cos \phi x}, \) \hspace{1cm} (A.3)

where \( A \) and \( B \) are unknown coefficients. The first term and the second term in (A.3) describe the down-going and the up-going wave, respectively. In order to find the aforementioned unknowns first, we note that the tangential electric field is zero over the PEC boundary \((y = 0)\), thus,

\( B = -Ae^{ik_y \sin \theta}, \) \hspace{1cm} (A.4)

Second, imposing the continuity of the tangential field components \( E_z \) and \( H_x \) at \( y = y_0 \) yields,

\[
A = \frac{2e^{-ik_0 \sin \theta_y}}{1 + \frac{k_1 \sin \theta}{\mu k_0 \sin \theta_0} + e^{ik_2 \sin \theta_y} - 1 + \frac{k_1 \sin \theta}{\mu k_0 \sin \theta_0}},
\]

and

\[
R = \frac{k_1 \sin \theta}{\mu k_0 \sin \theta_0} \left[ e^{ik_2 \sin \theta_y} - 1 + e^{ik_2 \sin \theta_y} \right] \frac{k_1 \sin \theta}{\mu k_0 \sin \theta_0} \left[ e^{-ik_2 \sin \theta_y} - 1 + e^{-ik_2 \sin \theta_y} \right].
\] \hspace{1cm} (A.5)

Thus, the electric field in dielectric slab can be expressed as,

\( \psi = Ae^{-ik_y (y - y_0) \sin \theta} - e^{ik_y \sin \theta \phi} \) \hspace{1cm} (A.6)

where \( A \) is given in equation (A.5).

Fig. A. Geometry of a dielectric slab on an infinite ground plane.

REFERENCES


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Scattering by a Metallic Sphere Coated with Chiral Metamaterials

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Abstract — Co-polarized and cross-polarized electromagnetic scattering of a metallic sphere coated with chiral metamaterials (CMMs) are simulated with Mie series solution. Firstly, based on Bohren’s decomposition technique, electromagnetic fields inside and outside of the sphere are expanded in spherical harmonics vector function. Then, the expanded coefficients are obtained in a suitable form for computation by applying the boundary conditions on the interfaces of all regions. The validity of Mie series solution is shown by computing backward scattering for a ferrite-coated metallic sphere. The effects to bistatic, forward and backward scattering caused by incident wave frequency, media parameters of a metallic sphere coated with CMMs are investigated in details.

Index Terms — Chiral, metamaterials, metallic, Mie series, and scattering.

I. INTRODUCTION

Recently, chiral metamaterials (CMMs) [1-6], which are artificial materials with large optical activity and circular dichroism have been proposed and made for polarization control applications at microwave and optical frequencies. CMMs lack any planes of mirror symmetry and possess strong ability to rotate the plane of polarization of electromagnetic waves. Due to geometric asymmetry, the cross-coupling between the electric and magnetic fields exists at the resonance. The chirality parameter \( \beta \) is used to describe the strength of the cross-coupling effect. Several geometric structures have been proposed to excite cross coupling, such as helices, Y structure, double-layered rosettes and crosswire structure and so on. Meanwhile negative refraction can be achieved by a chiral route. Due to the potential applications ranging from cloaking devices, sub-wavelength optical waveguides, to circular polarizer etc., interest in the study of CMMs has been growing both theoretically and experimentally. Analytical and numerical methods have been used to investigate wave propagation in chiral media [2-6] or metamaterials [7-9] such as Mie series solution, invariant embedding method, finite-difference time-domain method [10], and method of moments, etc. For three-dimensional structures, analytical Mie series solution [11-19] is more efficient and accurate than the others.

This paper is organized as follows: according to Bohren’s decomposition technique, Mie series solution for a metallic sphere coated with chiral metamaterials is firstly deduced by applying electromagnetic fields expanded in spherical harmonics vector function inside and outside of the CMMs-coated metallic sphere to boundary conditions. Meanwhile, how to overcome the numerical instability of the Bessel function in the Mie series formula is presented. In section 3, co-polarized and cross-polarized bistatic forward and backward scattering of a metallic sphere coated with chiral metamaterials are calculated with Mie series solution to study its application in the cloak. Finally, conclusions are given.
II. THEORY

Figure 1 presents the geometry of the electromagnetic wave incident on a coated sphere with inner radius \( b \) and outer radius \( a \) \([13, 16]\). The time harmonic dependence \( e^{i\omega t} \) is assumed for all fields. The incident electromagnetic wave can be expanded in the vector spherical harmonics functions as,

\[
E^{\text{inc}} = \sum_{n=1}^{\infty} E_n \left[ M_{\text{elm}}^{(i)}(k_b) - iN_{\text{elm}}^{(i)}(k_b) \right]
\]

\[
H^{\text{inc}} = -\frac{k_3}{\omega \mu_3} \sum_{n=1}^{\infty} E_n \left[ M_{\text{elm}}^{(i)}(k_b) + iN_{\text{elm}}^{(i)}(k_b) \right], \tag{1}
\]

where \( E_n = i^n E_0(2n+1) / [n(n+1)] \). The notations \( o1n \) and \( e1n \) mean the summation form of both, the even and odd modes, respectively.

![Incident plane wave](image)

**Fig. 1.** A plane wave is incident on a metallic sphere coated with chiral metamaterials.

According to the Bohren’s decomposition technique \([13]\), the eigenfunction expansion in asymmetry chiral metamaterials can be written as a superposition of a left-handed and right-handed circularly polarized wave functions \( \psi_{\text{elm}}^{(i)} = M_{\text{elm}}^{(i)} + N_{\text{elm}}^{(i)} \), \( \psi_{\text{elm}}^{(o)} = M_{\text{elm}}^{(o)} - N_{\text{elm}}^{(o)} \), where \( i \) equals 1 or 3. The superscript “1” relates to the first type of spherical Bessel function and “3” relates the first kind of spherical Hankel function. The expansions of the scattered electromagnetic fields \( (E^*, H^*) \), and the electromagnetic fields \( (E^{\text{chiral}}, H^{\text{chiral}}) \) in the CMMs region \( b < r < a \) are,

\[
E^* = \sum_{n=1}^{\infty} E_n \left[ a_n^* M_{\text{elm}}^{(3)}(k_a) - ib_n^* N_{\text{elm}}^{(3)}(k_a) \right]
\]

\[
+ a_n^* M_{\text{elm}}^{(3)}(k_b) - ib_n^* N_{\text{elm}}^{(3)}(k_b) \right]
\]

\[
H^* = -\frac{k_3}{\omega \mu_3} \sum_{n=1}^{\infty} E_n \left[ b_n^* M_{\text{elm}}^{(3)}(k_b) + ia_n^* N_{\text{elm}}^{(3)}(k_b) \right]
\]

\[
+ b_n^* M_{\text{elm}}^{(3)}(k_a) + ia_n^* N_{\text{elm}}^{(3)}(k_a) \right],
\]

\[
E^{\text{chiral}} = \sum_{n=1}^{\infty} E_n \left[ c_n^* \psi_{\text{elm}}^{(3)}(k_a) + c_n^* \psi_{\text{elm}}^{(3)}(k_a) \right]
\]

\[
+ c_n^* \psi_{\text{elm}}^{(3)}(k_a) + c_n^* \psi_{\text{elm}}^{(3)}(k_a) \right] / \eta, \tag{2}
\]

\[
H^{\text{chiral}} = \sum_{n=1}^{\infty} E_n \left[ d_n^* \psi_{\text{elm}}^{(3)}(k_a) + d_n^* \psi_{\text{elm}}^{(3)}(k_a) \right]
\]

\[
+ d_n^* \psi_{\text{elm}}^{(3)}(k_a) + d_n^* \psi_{\text{elm}}^{(3)}(k_a) \right],
\]

where \( \eta = (\mu / \epsilon)^{1/2}, k = k_0(\epsilon_0 / \mu_0)^{1/2} \), \( k_0 = k(1+\beta k) \), \( v_r, \mu_r \) and \( \beta \) are the relative permittivity, relative permeability and chirality parameter of CMMs, respectively.

The unknown coefficients \( a_n^*, b_n^*, c_n^*, d_n^* \) of the scattered fields can be obtained by applying the boundary conditions of continuous tangential electric and magnetic fields at \( r = a \) and the tangential electric field of the metallic boundary being vanished at \( r = b \) \([8]\). In order to avoid computing Bessel functions with complex components that produce numerical instabilities, the coefficients of the scattered fields can be rearranged in a suitable form for computation as below,

\[
a_n^* = \frac{\psi_n(x)}{\xi_n(x)} \left[ \eta_1 P_{\text{elm}}^{(1)}(R) D_n(x) - P_{\text{elm}}^{(2)}(R) \right] \left[ P_{\text{elm}}^{(1)}(L) F_n(x) - \eta_1 P_{\text{elm}}^{(2)}(L) \right]
\]

\[
+ \left[ \eta_1 P_{\text{elm}}^{(1)}(L) D_n(x) - P_{\text{elm}}^{(2)}(L) \right] \left[ P_{\text{elm}}^{(1)}(R) F_n(x) - \eta_1 P_{\text{elm}}^{(2)}(R) \right]
\]

\[
+ \left[ \eta_1 P_{\text{elm}}^{(1)}(R) D_n(x) - P_{\text{elm}}^{(2)}(R) \right] \left[ P_{\text{elm}}^{(1)}(L) F_n(x) - \eta_1 P_{\text{elm}}^{(2)}(L) \right],
\]
with
\[ \pi_n = \frac{P_n^0(\cos \theta)}{\sin \theta}, \]
\[ \tau_n = -\sin \theta P_n^\mu(\cos \theta), \] (7)
where \( P_n^\mu \) is the Legendre function.

### III. NUMERICAL RESULTS

In this section, numerical results about scattering by a metallic sphere coated with CMMs are illustrated. Bistatic, forward and backward radar cross sections, which are generally dependent upon various parameters characterizing the geometry, material properties, and incident fields, are discussed below.

#### A. Example verification

The validity of Mie series solution in the paper is verified with the results in reference [11]. Figure 2 presents the backward scattering versus the radius for a 0.01 m depth metallic sphere coated with different kinds of media. The wavelength of the incident wave \( \lambda_0 \) is chosen to be 0.01 m, the thickness \( t = a - b \) of the media coating layer is 0.05\( \lambda_0 \). The curve consisting of crosses represent backward scattering of a bald metallic sphere. The solid line, dash line, dotted line, and circular curve represents the backward scattering of a metallic sphere coated with lossless ferrite \( (\varepsilon_r = 2.5, \mu_r = 1.6) \), lossy ferrite \( (\varepsilon_r = 2.5+i1.25, \mu_r = 1.6+i0.8) \), lossy metamaterials \( (\varepsilon_r = -2.5+i1.25, \mu_r = -1.6+i0.8) \), and lossy chiral media \( (\varepsilon_r = 2.5+i1.25, \mu_r = 1.6+i0.8, \beta = 9\times10^{-4}) \), respectively.

In Fig. 2, the dash line has an excellent agreement with the asterisk for the backward scattering data in reference [11]. Lossy ferrite, metamaterials, and chiral media can make backward scattering decrease at relatively wide electrical size. The backward RCS of a metallic sphere coated with lossy metamaterials and lossy chiral media vary relatively slower as the radius increases. Though the skin depth of each kinds of media coating and the incident wave frequency are numerically identical, it may be noted in Fig. 2 that the backward scattering of a metallic sphere coated with lossy chiral media is significantly smaller than the other media coating.

![Fig. 2. Backward scattering versus radius for a metallic sphere with ferrite, metamaterials, or chiral media coating.](image)

#### B. Bistatic RCS

Figure 3 presents the bistatic co-polarized E-plane with a bistatic RCS of \( \sigma_{\theta\theta} \) and a co-polarized H-plane with a bistatic RCS of \( \sigma_{\phi\phi} \). In addition to the cross-polarized RCS patterns for a metallic sphere coated with CMMs, having \( \varepsilon_r = -4.0, \mu_r = -1.0, \) and \( \beta = 0.006 \). The radius \( b \) of the metallic sphere is 0.382 cm and the outer radius \( a \) of the chiral metamaterials shown in Fig. 1 is 1.528 cm [20]. The arrow indicates the direction of the plane wave incidence. The Mie series solution spans incident wave frequencies 3 GHz, 9.375 GHz, and 18 GHz. For the sake of brevity in the paper, only half of the bistatic scattering patterns are shown.

As shown in Fig. 3, the co-polarized and cross-polarized bistatic radar cross sections are relatively smaller at most angles as the 3GHz electromagnetic wave incident. When the incident wave frequency increase, both co-polarized forward scattering and resonant characteristic of a metallic sphere coated with CMMs obviously increase.
Fig. 3. Bistatic RCS patterns for a metallic sphere coated with CMMs for the (a) co-polarized E-plane, (b) co-polarized H-plane, and (c) cross-polarized RCS.

C. Forward RCS

Figure 4 compares the forward scattering response of a 10 cm radius metallic sphere and a 10 cm radius metallic sphere coated with 1 cm thickness CMMs as a function of electrical size. The cross-polarized scattering of a bald metallic is zero. The circular curve, curve consisting of crosses, solid line, and dotted line represent the imposed condition without the coating layer, coated with lossy chiral metamaterials case I ($\varepsilon_r = \mu_r = -1, \beta = 0.001$), case II ($\varepsilon_r = \mu_r = -2, \beta = 0.001$), case III ($\varepsilon_r = \mu_r = -0.5, \beta = 0.001$), respectively. As can be seen from Fig. 4, a metallic sphere coated with CMMs cast a larger shadow than a metallic sphere. Though the introduction of chiral parameter destroy the impedance match characteristic of matched metamaterials with $\varepsilon_r = \mu_r, \beta = 0$, the co-polarized, and cross-polarized forward scattering of a metallic sphere coated with lossy CMMs case I has a well-defined trend, in a manner consistent with the forward scattering of a metallic sphere. Compared to the co-polarized, the cross-polarized forward scattering is relatively smaller. A metallic sphere coated with chiral metamaterials case III ($\varepsilon_r = \mu_r = -0.5, \beta = 0.001$) has relatively more surface modes, due to the resonant effect related to the Mie scattering coefficients.

Fig. 4. Forward scattering from a 10 cm radius metallic sphere coated with CMMs for both the (a) co-polarized and the (b) cross-polarized.

D. Backward RCS

Figure 5 illustrates the co-polarized and cross-polarized backward scattering of a relatively large 10 cm radius metallic sphere coated with 1 cm thickness for different kinds of media. In Fig. 5 (a), the curve consisting of crosses and circular curve represent the co-polarized backward scattering of a bald metallic sphere and a metallic sphere coated with chiral metamaterials ($\varepsilon_r = -2.5, \mu_r = -1.6, \text{ and } \beta = 0.005$). From 2.2 GHz to 2.7 GHz, the chiral metamaterials make the backward RCS of metallic sphere evidently decrease. One of the possible reasons is the negative refractive properties of the chiral metamaterials, which makes the refracted wave go back to the front surface of the metallic sphere and produce a shadowing effect on the back region. The other possible reason is the chirality parameter, which
induces the cross-polarized wave. The cross-polarized scattering in Fig. 5 (b) is nearly negligible as the value of chirality parameter $\beta$ is relatively small.

Fig. 5. Backward scattering response of a metallic sphere coated with different kinds of media for both (a) co-polarized and (b) cross-polarized.

**IV. CONCLUSIONS**

This paper presents Mie theory for electromagnetic scattering by a perfectly metallic sphere with a uniform coating of chiral metamaterials. How to overcome the numerical instability of the Bessel function in the series formula is given. Co-polarized and cross-polarized bistatic scattering patterns, forward and backward radar cross section of a metallic sphere coated with chiral metamaterials are illustrated. Numerical results show that the co-polarized forward scattering and the resonant surface modes of a metallic sphere coated with CMMs increase with increasing the frequency of the incident wave. Compared to the co-polarized scattering, the cross-polarized scattering are relatively smaller. Due to the negative refractive property and giant optical activity, CMMs can make the echo of a metallic sphere decrease to a certain degree.

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**REFERENCES**

[10] J. A. Pereda, A. Grande, O. González, and Á. Vegas,


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A Novel Wilkinson Power Divider Using Open Stubs for The Suppression of Harmonics

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Abstract — In this paper, the design process of a novel Wilkinson power divider is presented. The proposed power divider features a simple structure with open stubs at each port. With slight changes of the dimensions of open stubs, designed power divider can suppress combinations of each two desired order harmonic simultaneously. From the measured results, 45 dB and 43 dB suppression for 3rd and 5th harmonics is obtained, respectively. The proposed power divider has an insertion loss less than 0.1 dB, input return loss better than 31 dB, output return loss better than 51 dB, and better than 43 dB of isolation at 1.65 GHz.

Index Terms — Harmonic suppression, open stub, and Wilkinson power divider.

I. INTRODUCTION

Wilkinson power dividers are widely applied in microwave communication such as power amplifiers, mixers, and frequency multipliers. Wilkinson power divider is designed for the single/dual band applications [1-2].

In many applications, the unwanted harmonics caused by nonlinear property of the active circuit elements be removed. Minimizing harmonics distortion is a great challenge in modern wireless communications with the high data-rate. It is cost-effective if the unwanted harmonics are suppressed in the power divider or the combiner structure [3]. Several methods have been proposed so far to design miniaturized harmonic suppressed power dividers with improved performance [3-17]. In [3-6] power dividers with two microstrip electromagnetic band-gap (EBG) cells for harmonics suppression are presented. In [7, 8] harmonics suppression is demonstrated with defected ground structure (DGS). Nevertheless, DGS and EBG, need etching process on backside ground plane and accurate position calibration, which improve time-consumption and difficulty in machining [9]. Nowadays resonators, filters [10-12] and shunt open stubs elements have been widely used to suppress the unwanted harmonics and size reduction. In [13, 14] a compact size Wilkinson power divider, based on non-uniform transmission lines is presented and in [15-17], Π- and T-shaped shunt open-stubs are used for harmonics suppression.

However, in these works, obtaining harmonics suppression with high level of attenuation is still subject of discussion and challenge. In this paper, a novel Wilkinson power divider for harmonics suppression with high level of attenuation is presented. This structure has significant advantages in terms of simple topology and superior harmonic suppression. The major advantage of the new structure is its high flexibility capability. The power divider is fabricated based on 3rd and 5th harmonics suppression. Moreover, simulation results show that the proposed structure can suppress the 2nd and 3rd harmonics.

II. POWER DIVIDER DESIGN

Figure 1 (a) shows the conventional Wilkinson
power divider that consists of two quarter-wavelength transmission lines ($\sqrt{2} Z_0$) and an isolation resistor (100 ohms). Figure 1 (b) shows the structure of the proposed Wilkinson power divider. It consists of two quarter-wavelength transmission lines, two branch-lines ($\theta_3$), three open shunt stubs (two $\theta_2$ and one $\theta_1$) and an isolation resistor. This power divider is symmetric, so the odd- and even-mode analyses can be used to determine the circuit parameters for harmonic suppression [18].

A. Odd-mode analysis

With referring to the diagram shown in Fig. 2 (a), the output admittance of the half-circuit is simply equal to,

$$Y_A = -\frac{j\cot 90^0}{Z} = 0 \quad (1)$$

$$Y_B = \frac{j\tan \theta_2}{Z}, \quad (2)$$

$$Y_c = \frac{Z_0 + jZ_0 \tan \theta_3}{Z_0 + jZ_0 \tan \theta_3}, \quad (3)$$

$$Y_0 = Y_A + Y_B + Y_C. \quad (4)$$

The real part of equation (4) becomes,

$$R = 2Z_0(1 - \tan \theta_2 \tan \theta_3), \quad (5)$$

while the imaginary part yields

$$Z_0 \tan \theta_3 = \frac{R}{Z_0}(\tan \theta_2 + \tan \theta_3). \quad (6)$$

Substituting equation (5) into equation (6), results in

$$Z = Z_0 \sqrt{(\tan \theta_2 + \tan \theta_3)(\cot \theta_3 - \tan \theta_2)}. \quad (7)$$

B. Even-mode analysis

According to Figure 2 (b) under even mode excitation, the ABCD matrix can be expressed for the equivalent circuit of the proposed power divider as follows,

$$\begin{bmatrix} 1 \\ jY \tan \theta_1 \\ 0 \\ \frac{1}{Z} \\ \frac{1}{Z} \end{bmatrix} \times \begin{bmatrix} 0 \\ jZ \\ 0 \\ 0 \\ 1 \end{bmatrix} \times \begin{bmatrix} jY \tan \theta_2 + jY \tan \theta_3 \\ 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix}. \quad (8)$$

Subsequently, the ABCD parameters can be obtained as,

$$A = -(\tan \theta_2 + \theta_3) \quad (9)$$

$$B = jZ, \quad (10)$$

$$C = jY - \frac{jY}{Z} \tan \theta_1 \tan \theta_2 - \frac{jY}{Z} \tan \theta_1 \tan \theta_3, \quad (11)$$

$$D = -\frac{\tan \theta_1}{2}. \quad (12)$$

Fig. 1. Schematic diagram of the (a) conventional Wilkinson power divider and the (b) proposed power divider.

The input impedance of the even mode equivalent circuit is expressed as [18],

$$Z_{in} = 2Z_0 \frac{AZ_0 + B}{CZ_0 + D}. \quad (13)$$

Assuming the network is reciprocal and lossless, then equation (13) can be written as,

$$A = 2D \quad (14)$$

and

$$A^2 - \frac{B^2}{Z_0^2} = 2. \quad (15)$$

Using equations (9) - (12), equations (14) and (15) can then be modified as follows,

$$\tan \theta_1 = \tan \theta_2 + \tan \theta_3 \quad (16)$$

and

$$\tan \theta_2 + \tan \theta_3 + \frac{Z^2}{Z_0^2} = 2. \quad (17)$$

Substituting equations (16) and (7) into equation (17), yields,

$$\tan \theta_1^2 + \tan \theta_1(\cot \theta_3 - \tan \theta_2) = 2. \quad (18)$$

Since n\textsuperscript{th} harmonic suppression is desired, $\theta_1$ and $\theta_2$ are assigned to be $\pi/2n$ [19]. For the 3\textsuperscript{rd} and 5\textsuperscript{th}
harmonic suppressions, $\theta_1$ and $\theta_2$ are obtained to be $\pi/6$ and $\pi/10$, respectively. Substituting these values into equation (16), $\theta_3$ is obtained, which is $14.1^\circ$. The value of $R$ and $Z$ are obtained from equations (5) and (7), as 92 ohms and 72 ohms, respectively.

![Fig. 2. Half-circuit of the proposed power divider for the (a) odd mode and the (b) even mode.](image)

III. IMPLEMENTATION AND RESULTS

To demonstrate the proposed circuit, a power divider with a center frequency fixed at 1.65 GHz for harmonics suppression was designed and implemented, as shown in Fig. 3. It was fabricated on an RT/Duroid 5880 substrate with a relative permittivity of 2.2, thickness of 0.381 mm and loss tangent of 0.0009. The overall dimension of the circuit was about 24 mm × 16 mm (384 mm$^2$), which demonstrates a 35% size reduction compared to the conventional microstrip Wilkinson power divider with the same center frequency. The S-parameters were measured using an Agilent N5230A network analyzer. Figure 4 illustrates the simulated and measured S$_{21}$ as a function of frequency.

![Fig. 3. Photograph of the fabricated power divider.](image)

![Fig. 4. Measured and simulated insertion loss of power divider for the 3rd and 5th harmonics suppression mode.](image)

The simulations were performed using ADS (advanced design system by Agilent technologies). From the measured results, it can be found that the power divider passes the 1.65 GHz fundamental signal and suppresses the 4.95 GHz third-order harmonic and the 8.25 GHz fifth-order harmonic, simultaneously. From Fig. 4, the insertion loss at 1.65 GHz is 0.1 dB, the suppression for the third- and fifth-order harmonics are 43 dB and 41 dB, respectively. However, the measured S-parameter is shifted from 8.25 GHz to 8 GHz for the fifth-order harmonic suppression. This error is due to the high-frequency parasitic effect [3].

The S$_{21}$ response of the conventional Wilkinson power divider is also shown in Fig. 4. From the simulated and measured results, as shown in Fig. 5, the circuit provides good input return loss. The measured S$_{11}$ is about 31 dB at the operation frequency of 1.65 GHz. Figure 6,
demonstrates the simulated and measured output return loss. As seen from Fig. 6, the measured $S_{22}$ is better than 51 dB at the operation frequency of 1.65 GHz.

Therefore, the designed circuit is well matched to the input and two output ports. In Fig. 7, the simulated and measured isolations of the two output ports are shown.

![Figure 5](image1.png)  
Fig. 5. Measured and simulated input return loss of power divider for the 3rd and 5th harmonics suppression mode.

The measured isolation between ports 2 and 3 is better than 43 dB. A comparison of the power dividers for the $n^{th}$ harmonics suppression is summarized in Table 1. As the results show, this work presents significant third- and fifth-order harmonic suppressions as compared to the reported works. The most significant advantage of this structure is that only by changing the dimensions of $\theta_1$ and $\theta_2$, it can suppress each two desired harmonics. With $\theta_1 = 45^\circ$ ($L_1 = 15.3$ mm) and $\theta_2 = 22.5^\circ$ ($L_2 = 7.6$ mm), 2nd and 4th harmonics are suppressed.

![Figure 6](image2.png)  
Fig. 6. Measured and simulated output return loss of power divider for 3rd and 5th harmonics suppression mode.

Moreover, 3rd and 4th harmonics suppression is achieved with $\theta_1 = 30^\circ$ ($L_1 = 10.2$ mm) and $\theta_2 = 22.5^\circ$ ($L_2 = 7.6$ mm). With $\theta_1 = 45^\circ$ ($L_1 = 15.3$ mm) and $\theta_2 = 30^\circ$ ($L_2 = 10.2$ mm), after fine adjustment 2nd and 3rd harmonics suppression is occurred as shown in Fig. 8. The power divider passes the same fundamental signal (1.65 GHz) and suppresses the 3.3 GHz second-order harmonic and the 4.95 GHz third-order harmonic, simultaneously. The simulated $S_{21}$ parameter at 1.65 GHz shows a power split of 3.04 dB. Furthermore, over than 70 dB suppression for the second- and third-order harmonic is obtained. Figure 9 shows that the isolation between the two ports, which is over 34 dB and the output return loss is more than 36 dB.

![Figure 7](image3.png)  
Fig. 7. Measured and simulated isolation of power divider for 3rd and 5th harmonics suppression mode.

![Figure 8](image4.png)  
Fig. 8. The simulated results of $S_{11}, S_{21}$ for 2nd and 3rd harmonics suppression mode.
IV. CONCLUSION

A new Wilkinson power divider with novel structure for harmonics suppression is designed, simulated, and measured. This structure enables the power divider to work as harmonics suppressor with capability of suppressing each two desired harmonics. The proposed power divider with such performance can answer the demands of modern communication systems.

REFERENCES


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A Linear-to-Circular Polarizer Using Split Ring Resonators

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Abstract — A transmission polarizer with one layer of splitting ring resonator to realize a linear-to-circular polarization rotator is presented. Based on the accurate design of anisotropic metamaterials, high conversion efficiency and 8 % frequency band are achieved. Microwave experiments were performed to realize these ideas successfully and results are in excellent agreement with numerical simulations.

Index Terms — Circularly polarized, linearly polarized, metamaterial, polarizer, and split ring resonators.

I. INTRODUCTION

Polarization is an important characteristic of electromagnetic (EM) waves and is often utilized in microwave and optical systems. It is always desirable to have full control of polarization in transmission and reflection of waves. Conventional methods to manipulate polarization include using optical gratings, dichroic crystals, or employing the Brewster and birefringence effects [1, 2]. Recently, metamaterials have been proposed to manipulate EM wave polarizations [3-8]. Metamaterials have drawn much attention recently due to its many fascinating properties, such as the negative refraction, the in-phase reflection, and the axially frozen modes, etc [9, 10]. A metamaterial reflector has been employed to manipulate the polarization state of an incident EM wave [6]. A near-complete cross polarization conversion has been achieved with anisotropic metamaterials. It is due to the reflection phase difference in the two orthogonal polarizations. The disadvantage of the reflector polarizer is that the incoming and outgoing waves are difficult to separate. To overcome this, a metamaterial transmission polarizer has been proposed [7]. It can complete conversions from a linear polarization to a circular polarization and to its cross linear polarization effectively. Compared to the reflector polarizer, the incoming and outgoing waves in the transmission polarizer are naturally well separated, and therefore do not interfere with each other. However, in the transmission polarizer, it needs two (for the liner-to-circular polarizer) or four (for the liner-to-liner polarizer) pieces of substrate fixed with certain spacing. These substrates bring many reflections, which make the transmission efficiency of the polarizer restricted. Another alternative approach to the polarization conversion is by using a bilayered chiral metamaterials [8]. It is composed of a substrate coated on both surface with some enantiomeric patterns. In this polarization rotator, a 90° polarization rotation with high polarization conversion efficiency is obtained, but the bandwidth is only about 3 %.

In this paper, we propose a new transmission polarizer in which only one layer of splitting ring resonator (SRR) is fabricated. It completes the conversion from a linearly polarized wave to a circularly polarized wave successfully. The transmission efficiency of the polarizer can be controlled and the frequency band is extended to about 8%. Microwave experiments were performed and the results are in agreement with numerical simulations. Both the results of the simulations and the experiments show that highly efficient conversion from a linear polarization to a circular polarization has been accomplished.

II. NUMERICAL ANALYSIS

Figure 1 (a) shows the schematic diagram of one unit cell of the present polarizer. The
The dimension of the unit cell is $11 \times 11$ mm$^2$. The dielectric constant of the substrate is $\varepsilon_r = 2.65$ and its thickness $t$ is 1 mm. The SRR with 0.1 mm thick is coated on one side of the substrate. Both the length $l$ and width $w$ of the SRR are 9 mm. The width of the wires is $w_1 = 0.75$ mm. The air gap $g$ between two adjacent cut-wires is 1.2 mm. The incident wave $\vec{E}^{\text{in}}$ normally impinged on the sample can be decomposed into two modes with the electric fields along the $x$ axis and the $y$ axis ($\vec{E}^{\text{in}} = \hat{x} E_x^{\text{in}} + \hat{y} E_y^{\text{in}}$, as shown in Fig. 1 (b)). The incident wave is linearly polarized with,

$$|E_x^{\text{in}}| = |E_y^{\text{in}}|$$

$$\arg(E_x^{\text{in}}) = \arg(E_y^{\text{in}}).$$

The transmitted wave is $\vec{E}^{\text{out}} = \hat{x} E_x^{\text{out}} + \hat{y} E_y^{\text{out}}$. For the two wave modes, the transmission coefficients $T_x$ and $T_y$ are defined as,

$$T_x = \left|E_x^{\text{out}} \right| / \left|E_x^{\text{in}} \right|$$

$$T_y = \left|E_y^{\text{out}} \right| / \left|E_y^{\text{in}} \right|.$$  

The axial ratio $p$ and phase difference of the transmitted wave are defined as [11],

$$p = 20 \log \left( \left| E_x^{\text{out}} / E_y^{\text{out}} \right| \right)$$

$$\text{phase difference} = \left| \arg(E_x^{\text{out}}) - \arg(E_y^{\text{out}}) \right|,$$

when $p = 0$ and phase difference $= \pi/2$, the transmitted wave becomes circularly polarized wave. The transmission coefficients $T_x$ and $T_y$ represent the conversion efficiency of the polarizer. If we are able to control $T_x$ and $T_y$ to be close to -3 dB, nearly all the energy will be transmitted and no wave will be reflected.

We use the commercial software CST Microwave Studio to simulate the unite cell shown in Fig. 1. The SRR is modeled as perfect electrically conducting material. Along the $x$ and $y$ axes, periodic boundary conditions are applied. The calculated transmission coefficients and the axial ratio of the transmitted wave are shown in Fig. 2 (a). It can be seen from this figure that both the transmission coefficients of $T_x$ and $T_y$ are close to -3 dB in the frequency range 12 GHz - 13 GHz, which is a direct evidence of small loss and little reflections of the polarizer. The axial ratio of the transmitted wave is below 2 dB in this frequency range. Meanwhile, an obvious zero value in the axial ratio can be observed around 12.6 GHz, which indicates that the two wave modes of the transmitted waves have equal amplitudes. The phases of the two modes of the transmitted wave obtained using CST calculations are shown in Fig. 2 (b). The phase difference between the $E_x^{\text{out}}$ and $E_y^{\text{out}}$ is also shown in the same figure. It can be seen from this figure that in the frequency range of 12 GHz - 13 GHz near 90° phase difference in the two orthogonal components is achieved. These simulated results confirm a fact that in the frequency range of 12 GHz - 13 GHz the linearly polarized wave is conserved to a circularly polarized wave by the transmission polarizer. The bandwidth can reach to 8 %.

The conversion efficiency (defined as $\sqrt{(E_x^{\text{out}})^2 + (E_y^{\text{out}})^2 / (E^{\text{in}})^2}$) is plotted in Fig. 3. It
can be seen from this figure that the conversion efficiency of the polarizer exceeds 99% in the frequency range of 12 GHz - 13 GHz and reaches its maximum value at around 12.6 GHz, which shows that highly efficient conversion from a linearly polarized wave to a circularly polarized wave has been accomplished.

III. EXPERIMENT VALIDATION

In order to confirm this expected behavior experimentally, we have fabricated a sample composed of 30 x 30 unit cells (see Fig. 4 (a)). The picture of the experimental setup is shown in Fig. 4 (b). The reflection and transmission waves were measured using a pair of horn antennas connected to the vector network analyzer (Agilent E83638). The horns antennas was fixed on a fixator, which had angle calibration to ensure that horn alignments were at the exact angles. The electric field of the transmitting antenna was polarized to the direction illustrated in Fig. 1 (b), which had a 45° angle with respect to the vertical direction, so that the electric fields of the two modes for incident waves were related by $|E_x^{in}| = |E_y^{in}|$ and $\arg (E_x^{in}) = \arg (E_y^{in})$ and. A calibration was conducted by removing the sample and having the receiving antenna aligned at the same direction with the transmitting antenna. Then we rotated the receiving antenna from 0° to 90° to achieve the $E_x^{out}$ and $E_y^{out}$ of the transmitted wave. All the measurements were performed in an anechoic chamber.

Fig. 2. (a) The simulated transmission and axial ration of the transmitted wave and (b) the simulated phase difference of the two wave modes of the transmitted wave.

Fig. 3. The conversion efficiency of the polarizer.

Fig. 4. (a) The top view of the fabricated sample and (b) the picture of the experimental setup.
The measured axial ratio of the electric field is shown in Fig. 5 (a). For circular polarization, the amplitude of the electric field is supposed to be invariant and in our measurement the variation is less than 2 dB. The measured phase difference between the $E_{x\text{ out}}$ and $E_{y\text{ out}}$ components is shown in Fig. 5 (b). It can be seen from this figure that the phase difference is also around 90°. For the sake of comparison, the simulated results of the axial ratio and phase difference are also plotted in Fig. 5. It can be seen from this figure that although the measured result deviates from the simulated result in some frequencies (in fact, it revolves around the simulation result), it also indicates a fact that a full conversion from a linearly polarized wave to a circularly polarized wave is achieved. The deviations between the simulated value and the measured result are mainly due to the fact that, in the simulated model, the unit cells are periodically arranged and the substrate is infinite, while, in the experiment, the sample is composed of 30 $\times$ 30 unit cells and its size is only 33 $\times$ 33 cm$^2$, which is slightly larger than the aperture of the horn antenna. The small size of the sample results is due to the fact that some diffracted wave from the transmitting antenna reaches the receiving antenna directly. If we increase the size of the sample, the deviation between the simulated value and the measured result will be reduced.

**IV. THE APPLICATION OF THE POLARIZER TO A HORN ANTENNA**

To demonstrate the function of the metamaterial as a circular polarizer, we integrate the polarizer to a conventional horn antenna. The aperture of the horn antenna is 19.05 mm $\times$ 9.525 mm. It radiates a linearly polarized wave at 12.6 GHz. We arrange the structure periodically on the aperture of the antenna, as shown in Fig. 6. The horn needs to be rotated 45° to the $x$-axis to make sure that the electronic field has the same component along the $x$ and $y$ directions.

The simulated normalized radiation pattern of the integrated horn antenna is shown in Fig. 7. The simulation frequency is 12.6 GHz. For the sake of comparison, the radiation pattern of the conventional horn antenna is also plotted in this figure. It can be seen from this figure that the novel integrated horn has almost the same gain with the conventional horn, but it radiates a left handed circularly polarized (LHCP) wave. The gain-difference between the LHCP wave and the right handed circularly polarized (RHCP) wave of the integrated horn is 21.9 dB in the E-plane, and 20.3 dB in the H-plane.

![Fig. 5. (a) The measured axial ration of the transmitted wave and (b) the measured phase difference of the transmitted wave.](image)

![Fig. 6. The schematic picture of the polarizer integration to a horn antenna.](image)
Fig. 7. (a) The simulated radiation patterns in the E-plane at 12.6 GHz and (b) the simulated radiation patterns in the H-plane at 12.6 GHz.

The simulated axial ratio of the integrated horn in both E- and H-planes are shown in Fig. 8. The axial ratio is below 3 dB from about -10° to 10° at 12.6 GHz and the 3 dB angle band covers the main lobe. The results in the presented simulations demonstrate the function of the metamaterial as a circular polarizer. It can turn a conventional horn antenna, which radiate linearly polarized wave into a circularly polarized antenna.

V. CONCLUSION

This paper presents a new transmission polarizer with one layer of SRR to realize a linear-to-circular polarization rotator. Both the simulated and the measured results show that highly efficient conversion is achieved. Due to its thin thickness and high polarization conversion efficiency, the present polarizer may have potential applications in many situations and will find broad applications in various radio frequency and optical devices.

Fig. 8. The axis ratio of the circular polarized horn at 12.6 GHz.

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REFERENCES


Compact Microstrip Lowpass Filter with Wide Stopband and Sharp Roll-off using Triple Radial Stubs Resonator

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Abstract — A novel microstrip lowpass filter with good specifications such as sharp cutoff, wide stopband, low insertion loss, and high return loss is proposed. The proposed lowpass filter is realized using triple radial stubs resonator, i.e., three 60° radial stubs and harmonic attenuator, i.e., T shaped cell loaded by the semicircle. The cutoff frequency of the proposed filter is adjusted to 1.39 GHz. The transition band is approximately 0.21 GHZ from 1.39 GHz to 1.6 GHz with corresponding attenuation levels of -3 dB and -20 dB. The stopband with better than -20 dB rejection is from 1.6 GHz to 12.36 GHz, insertion loss in the passband is less than 0.1 dB, return loss is less than -25 dB and the overall size of the filter is 0.0074 λg2 ( 15 × 12.3 mm2 ). The proposed filter is fabricated and measured. The simulation and measurement results are in good agreement.

Index Terms — Lowpass filter, microstrip, radial stub, sharp roll-off, and wide stopband.

I. INTRODUCTION

Due to increasing constraint of reduction in size with optimum performance such as sharp cut-off, wide stopband, low insertion loss, and high return loss designs of lowpass filters are done with different methods. The sharp cut-off shows a sharper transition band, which indicates the higher selectivity; wide stopband shows the band with more than -20 dB harmonic suppression; low insertion loss shows high passing signals in the passband and high return loss refer to low return signals in the passband.

The conventional filter design method is normally not used, due to inherited deficiencies like the slow roll-off, poor frequency response in the passband and narrow stopband [1]. The Radial patches are presented in [2], which has good specification such as sharp roll-off and wide stopband, but the return loss in the pass band and the size of the filter is not satisfactory. A compact LPF using front coupled tapered compact microstrip resonator cell (FCTCMRC) is presented in [3], which despite the small size, neither the passband performance nor the stopband widths are good. Another method is to use complementary split ring resonators [4], which present sharp response and compact size, but fabrication of this structure because of its 3D configuration is difficult. A LPF with wide stopband using coupled line hairpin unit is demonstrated in [5]. In this filter, the insertion loss and return loss in the passband and the attenuation level in the stopband is not adequate. Later, LPF with novel patch resonator in [6] has been presented, while this filter has large circuit size. New ultra wide stopband LPF using transformed radial stubs (TRS) is introduced and investigated in [7], which has bad return loss in both passband and stopband, and the insertion loss in the passband is not good. A new compact defected ground structure (DGS) lowpass filter using a crescent shape structure etched in the ground plan is introduced in [8]. This filter has a gradual roll-off and narrow stopband.
In this paper, a microstrip LPF having compact size, sharp roll-off, wide stopband, low insertion loss, and high return loss in the passband is presented.

II. FILTER DESIGN

The design process for the proposed filter is as follows:

1- Design of the proposed three 60° radial stub resonator to achieve sharp roll-off response and to eliminate harmonics that appear near the cutoff frequency.

2- Suppressing Cells design and its addition to the proposed resonator in order to extend the stopband.

3- Combination of the proposed resonator and suppressing the cell to have a LPF with a wide stopband, sharp response, and good passband performance.

A detailed description of these steps is presented.

A. Proposed resonator

The 180° radial stub resonator and its LC equivalent circuit are shown in Figs. 1 and 2, respectively. The capacitance of $C_r$ in Fig. 2 would be lumped capacitor or other circuit’s capacitance like straight or radial stubs.

Figure 3 shows two types of capacitive elements, i.e., radial and straight stubs and their equivalent circuit. The parameter of the distributed stub section, which includes radial and the straight stubs of Fig. 3, can be modeled approximately as a lumped element.

A distributed transmission line, when the effective electric length is less than a quarter wavelength, can be modeled as a lumped elements. The proposed three 60° radial stub is shown in Fig. 4. The simulated S-parameters of the proposed resonator with different dimension of $W$, $L$ and, $R$ are illustrated in Figs. 5, 6, and 7, respectively. As seen in Fig. 5, by increasing $W$ from 0.1 mm to 0.5 mm with steps of 0.2 mm, the inductance of the resonator will be decreased, which makes the transmission zero move away from the lower frequency. Similarly, as shown in Fig. 6, when $L$ increases from 10.5 mm to 12.5 mm with step of 1 mm, the inductance of the resonator will be increased, which result in moving the transmission zero to the lower frequency. As shown in Fig. 7, when $R$ decreases from 3 mm to 2.2 mm with steps of 0.4 mm, the capacitance of the proposed resonator decreases so the cutoff frequency move to the higher frequency.
Fig. 4. The proposed three 60° radial stub resonator.

Fig. 5. Frequency response of the proposed resonator with different dimensions of W.

Fig. 6. Frequency response of the proposed resonator with different dimensions of L.

Fig. 7. Frequency response of the proposed resonator with different dimensions of R.

Frequency response of the proposed resonator with different dimensions of Lf is shown in Fig. 8. As it is seen, when Lf increases the suppression level increases without change in the location of the transmission zero. But increment of Lf result in the size increment. The decrement of Wf increment the inductance of the transmission line, which result in the increment of suppressing level as shown in Fig. 9. Therefore, the optimum value for Wf and Lf with respect to suppression level and filter size are selected.

Fig. 8. Frequency response of the proposed resonator with different dimensions of Lf.

Fig. 9. Frequency response of the proposed resonator with different dimensions of Wf.

As seen in Fig. 10 the cut-off frequency of the proposed resonator is adjusted to 1.49 GHz and the transition band is approximately 0.2 GHz from 1.5 GHz to 1.7 GHz with corresponding attenuation levels of -3 dB and -20 dB. The dimensions of the proposed resonator are as follows: R = 3 mm, W = 0.1 mm, L = 10.5 mm, Lf = 2.75 mm, Wf = 0.1 mm.
Fig. 9. Frequency response of the proposed resonator with different dimensions of Wf.

Fig. 10. The frequency response of the proposed three 60° radial stub resonator.

B. Suppressing cell design

To obtain a LPF with wide stopband, a suppressing cell to suppress the harmonics in the stopband is required. It is realized by a T shaped cell that is loaded by the semicircle. Figure 11 shows the single T shaped cell and T shaped cell loaded by the semicircle. Their frequency response is shown in Fig. 12. As it is seen from Fig. 12, when T shaped cell is loaded by the semicircle, the suppression level in the stopband is increased.

C. Proposed filter

To have a LPF with a wide stopband, sharp response and good passband performance, the proposed suppressing cell and the proposed resonator are combined. The proposed filter and its frequency response are shown in Figs. 13 and 14, respectively.

Fig. 11. The single T shaped cell and T shaped cell loaded by semicircle.

Fig. 12. Frequency response of the single T shaped cell and T shaped cell loaded by semicircle.
As shown in Fig. 15 when Lt is increased from 10.95 mm to 19.95 mm with steps of 3 mm, the stopband will be increased but the return loss and the insertion loss performance is decreased. Therefore, the optimum value for Lt with respect to its passband and stopband performance is selected.

The main transmission line in the proposed filter is bended, which results in size reduction. This work increases the inductance effect in the main transmission line, so the rejection level in the stopband is increased. Bending the transmission line has reduced the overall filter size by 52% and increased the suppression level in the stopband. The proposed LPF with bended transmission line and its frequency response are shown in Figs. 16 and 17, respectively.

Fig. 13. The proposed filter in the straight form.

Fig. 14. Frequency response of the proposed filter in the straight form.

Fig. 15. Frequency response of the proposed filter in the straight form with different dimensions of Lt.
The proposed LPF is designed and optimized using EM-simulator of ADS. The main transmission line has been bended, which results in size reduction. The microstrip LPF is fabricated on a substrate with dielectric constant of $\varepsilon_r = 2.2$, thickness of $h = 15$ mil and loss tangent equal to 0.0009. The source and the load of the structure have characteristic impedance of $Z_0$ equal to 50 Ω with width of 1.1 mm. The photograph and the simulated and measured results of the proposed filter are illustrated in Figs. 18 and 19, respectively. It is seen that the attenuation level in the stopband is higher than -20 dB, which is achieved from 1.6 GHz to 12.36 GHz and present the wide stopband. The proposed filter has low insertion loss of less than 0.1 dB and return loss of more than 25 dB in the passband. The frequency response of the filter is very sharp with the transition band equal to 0.21 GHz from 1.39 GHz to 1.6 GHz with corresponding attenuation levels of -3 dB and -20 dB.

The performance comparison between the proposed LPF and other works is presented in Table 1, where $\xi$, RSB, NCS, SF, AF, FOM, RL, and IL correspond to the Roll-off rate, relative stopband width, normalized circuit size, suppressing factor, architecture factor, figure of merit, return loss, and insertion loss, respectively. These parameters are defined as follows:

Roll-off rate $\xi$ is

$$\xi = \frac{a_{\text{max}} - a_{\text{min}}}{f_s - f_c},$$

(1)
where $\alpha_{\text{max}}$ is the -20 dB attenuation point; $\alpha_{\text{min}}$ is the -3 dB attenuation point; $f_s$ is the -20 dB stopband frequency, and $f_c$ is the -3 dB cut-off frequency. Therefore, the high roll off rate shows a sharper transition band, which indicates the higher selectivity.

The relative stopband width (RSB) is

$$\text{RSB} = \frac{\text{stopband} \ (-20\text{dB})}{\text{stopband center frequency}}, \quad (2)$$

where the high RSB shows the high stopband that is the band with more than -20 dB harmonic suppression.

The normalized circuit size (NCS) is

$$\text{NCS} = \frac{\text{physical size (length x width)}}{\lambda_g^2}, \quad (3)$$

where the lower NCS indicates the size of the filter is compact. The suppressing factor (SF) is based on the suppression in the stopband and is calculated as,

$$\text{SF} = \frac{\text{rejection level}}{10}. \quad (4)$$

The architecture factor (AF) for a planar and 3-D structure is defined as 1 and 2, respectively. Finally, the figure of merit (FOM) is defined as,

$$\text{FOM} = \frac{\xi \times \text{RSB} \times \text{SF}}{\text{NCS} \times \text{AF}}. \quad (5)$$

The FOM shows the overall performance of a LPF, where the filter with compact size, sharp transition band, high suppression level, and high stopband leads to a high FOM.

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<td>4159</td>
<td>12</td>
<td>1.5</td>
</tr>
<tr>
<td>Proposed filter</td>
<td>80.95</td>
<td>1.59</td>
<td>0.0074</td>
<td>2</td>
<td>1</td>
<td>34550</td>
<td>25</td>
<td>0.1</td>
</tr>
</tbody>
</table>

In the structure of the proposed filter, the three $60^\circ$ radial stub resonator is used to control the transition band, which result in increasing roll-off rate ($\xi$) i.e., equal to 80.95. The stopband is extended to 12.36 GHz using T shaped cell loaded by semicircle as suppressing cell, so the RSB is increased. By bending the transmission lines the overall size of the filter is reduced to about 52 % that makes NCS to have a lower value among the referred filters. Finally, the comparison shows that the proposed filter has the best figure of merit (FOM), $\xi$, NCS, return loss (RL), and insertion loss (IL) among the referred filters.

**IV. CONCLUSION**

A microstrip LPF with good specifications such as sharp roll-off, wide stopband, low insertion loss, and high return loss is designed and optimized. The three $60^\circ$ radial stubs resonator added to the T shaped cell loaded by the semicircle, results in sharp cutoff and wide stopband. The measurement results are in good agreement with the simulation results, and the proposed filter has very high FOM in comparison with the other works that is presented in recent years. This Filter with such features is a good candidate for modern communication system.

**REFERENCES**


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A Microstrip Printed Band-Notched UWB Antenna Using Modified CSRR Structure

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Abstract — A compact triple band-notch ultra-wideband (UWB) antenna with microstrip-feed is presented. The desired band-notch antenna is achieved by etching a narrowband triple complementary split-ring resonator into the radiating element of an existing UWB antenna. By attenuation of the measured return, the new antenna reduces interference from UWB in the C-band (3.7 GHz – 4.2 GHz) satellite communication systems and wireless local area network (5.15 GHz - 5.35 GHz, 5.725 GHz - 5.825 GHz bands). The built prototypes have a compact size of 25 × 27.9 mm² including the ground plane. This miniature size also delivers advantageous radiation patterns with good mono-polar characteristics across the UWB band with the gain attenuated within the desired notch bands. The antenna demonstrates omnidirectional and stable radiation patterns across all the relevant bands. Moreover, a prototype of the proposed antenna is fabricated, and the measured results are shown to be in good agreement with the simulated results.

Index Terms — Multiband, notch bands, printed slot antenna, and ultra-wideband (UWB).

I. INTRODUCTION

As the need for high-data-rate wireless communication becomes more urgent, various solutions have been suggested. Ultra-wide band (UWB) radio is a good candidate technology that has the advantages of higher data rates; good immunity to multi-path cancellation; a possible increase in communication operational security and low interference into legacy systems [1]. As they are required to be small and operate relative bandwidths, antennas are a particularly challenging aspect of UWB technology. The Federal communications commission (FCC) version of UWB radio has within its spectrum (3.1 GHz – 10.6 GHz), C-band (3.7 GHz – 4.2 GHz) satellite communication systems and the IEEE802.11a frequency band (5.15 GHz – 5.825 GHz), which are also a low-power technology. Therefore FCC UWB may be seen as an interferer for both the IEEE802.11a and C-band satellite communication systems. To address this problem, various UWB antennas with multi-notch band-stop characteristics have been proposed [2-5].

In this paper, a new band-notched printed monopole antenna with good gain characterization over a wide bandwidth is presented. By using a co-directional hexagon complementary split-ring resonators strip and by inserting a wave strip in the ground plane, the gain of the square antenna is enhanced, and also much wider impedance bandwidth can be produced, especially at the higher band. Different from the conventional structure, the notched band, covering the 3.68 GHz - 4.25 GHz, 5.05 GHz - 5.38 GHz, 5.7 GHz - 6.12 GHz band, is provided by electromagnetically adjusting coupling between a pair of co-directional hexagon complementary split-ring resonators strips protruded inside the swallow radiation pattern in our model. Experimental and simulated results of the constructed prototype are presented. The size of the designed antenna is smaller than the UWB antennas with band-notched function reported recently [6-9].

II. ANTENNA DESIGN

Microstrip antennas are key components in 1 GHz - 50 GHz frequency range. Compared with normal microwave antennas, the microstrip
antennas have several advantages, including low loss, high integration, low profile, and compact size. To fabricate swallow-shaped microstrip triple band-notched antenna mentioned in this paper, a half ellipse is cut from a rectangle shape radiating patch firstly and then moved into the bottom side of the radiating patch. This new shape with a gradient structure has the same area as the rectangle shape. In addition, the ground of the antenna has wave-like shape so that this ground also has a gradient structure. Since both the swallow-shaped radiating patch and the wave-like shape ground have a gradient structure, the antenna can ensure a smooth transition from one mode to another. In this case, the antenna will have a good impedance matching within a broad bandwidth.

The quarter wavelength corresponding to the lowest cutoff frequency can be derived using equation (1)

\[ \frac{\lambda}{4} = \frac{c}{4f} \]  

(1)

where \( \lambda \) represents the wavelength in free space, \( f \) is the frequency, and \( c \) is the speed of light. In this case, the radiating patch is similar to a disk. The lowest cutoff frequency of the corresponding quarter wavelength is equal to twice the radius of this disk,

\[ 2R = \frac{\lambda_p}{4} \]  

(2)

Therefore, the width of the antenna \( W < 2R \).

According to earlier research, the band-notched can be introduced by the complementary split ring resonator (CSRR) structures in the radiating patch. If the length of the CSRR is roughly the same as the half wavelength of the corresponding central band-notched frequency, the currency is restricted around the CSRR, resulting in a no radiating antenna, which is due to band-notched [10-12]. In order to achieve three bands, three co-directional hexagon complementary split-ring resonators, are embedded into the radiating patch in the antenna. This can be expressed by,

\[ L = \frac{c}{2f_{\text{notch}}} \sqrt{\varepsilon_r} \]  

(3)

where \( c \) represents the speed of light, \( f \) is the central frequency of the notched band, and \( \varepsilon_r \) is the effectively dielectric constant.

In order to reduce the interference from the UWB in the C-band (3.7 GHz – 4.2 GHz) satellite communication systems and wireless local area network (5.15 GHz – 5.35 GHz, 5.725 GHz – 5.825 GHz). Parameters like the radius of the complementary split ring resonator (CSRR), position of the CSRR, and the width of the CSRR have been optimized. These optimization works were managed by using commercial 3-D electromagnetic software HFSS [13-15].

The geometry of the proposed antenna is shown in Fig. 1. The overall antenna size is 25×27.9 mm². As can be seen, it consists of the following major parts: main radiation patch with a microstrip feed and a wave shape conductor ground plane in the back. The radius of the swallow radiating patch is fixed at 12.5 mm. The width of the feeding microstrip line is 1.55 mm, and its characteristic impedance is 50 Ω. Meanwhile, the conducting ground plane has size of 25 × 10.78 mm². The modified wave shape ground plane is applied to achieve broadband characteristics over the entire UWB band because the truncation creates a capacitive load that neutralizes the inductive nature of the patch to produce nearly pure resistive input impedance. An SMA is connected to the port of the feeding microstrip line [16]. The specified characteristics of this substrate are 0.508 mm in thickness and 2.2 in relative permittivity (\( \varepsilon_r \)). Good performance of multiple band-notched characteristic is simply accomplished by embedding a common direction hexagon CSRR to the swallow patch.

Figure 2 shows the current distributions at three center notched bands. The dimensions of the three co-directional hexagon CSRR are corresponding to three notched bands. When the antenna is working at the center of the lower notched band near 3.9 GHz, the outer complementary SRR behaves as a separator in Fig. 2 (a), which almost has no relation to the other band-notches [17]. Similarly, the middle complementary SRR operates as a second separator for the center of the middle notched band near 5.2 GHz in Fig. 2 (b). From Fig. 2 (c), the upper notched band near 5.9 GHz is ensured by the inner complementary SRR [18]. Additionally, as a certain current crowded on the ground plane near the microstrip feed line would affect the antenna performance, we take simulation and find that the dimension of the ground plane, especially,
has a significant effect on the triple band-notches performance, as well as the impedance bandwidth.

Fig. 1. Geometry of the antenna, having $R_1 = 4.01$ mm, $R_2 = 4.83$ mm, $R_3 = 6.98$ mm, $C_1 = 0.6$ mm, $C_2 = 3.35$ mm, $C_3 = 6$ mm, $d_1 = 0.2$ mm, $d_2 = 0.32$ mm, $d_3 = 0.45$ mm, $W = 25$ mm, and $L = 27.9$ mm.

III. RESULTS AND DISCUSSION

With the optimal parameters demonstrated in Fig. 1, an example monopole antenna was fabricated, which is shown in Fig. 3. As illustrated in Fig. 4, the proposed antenna has an impedance bandwidth (VSWR < 2) from 2.4 GHz to 11.8 GHz, which covers the entire UWB frequency band. Basically, this broad bandwidth is mainly determined by a conventional UWB antenna. By attaching co-directional hexagon complementary split-ring resonators, it is clearly observed from the measured results that the designed antenna exhibits triple stop bands of 3.68 GHz – 4.25 GHz, 5.05 GHz – 5.38 GHz, 5.7 GHz – 6.12 GHz. The center frequencies of the notched bands are 3.9 GHz, 5.2 GHz, and 5.9 GHz, respectively [19].

There is good agreement between simulated and measured results; the little difference between them may be caused by the soldering effects of an SMA connector, which have been neglected in our simulations [20].

The far-field radiation characteristics at 3.5 GHz, 5.5 GHz, and 7.5 GHz are given in Fig. 5, respectively. Nearly, omnidirectional radiation patterns in the xy-plane and dipole-like radiation patterns in the yz-plane are obtained at these frequencies [21]. Due to the limitations of laboratory instruments, the radiation patterns above 12 GHz were not measured. All the obtained radiation patterns accord with those of the conventional printed UWB monopole antennas. The proposed antenna has proved to be capable of providing favorable spatial-independent band-notched characteristics [22].

Fig. 2. The current distribution of the proposed antenna at (a) 3.9 GHz, (b) 5.2 GHz, and (c) 5.9 GHz.

Figure 6 shows the measured radiation efficiency of the antenna. The proposed antenna features an efficiency between 50% and 70% over the whole UWB frequency and lower than 5% in the notch band. The features of about 60%
average radiation efficiency is good enough to satisfy an acceptable variation for practical power transmission [23]. The measured gain of the proposed antenna is illustrated in Fig. 7. It can be seen that stable antenna gain with a variation of less than 3 dBi is achieved except for smaller values in the notched band, within which the smallest one is as low as -12 dBi. This confirms that the proposed antenna provides a high level of rejection to signal frequencies within the notched band [24-25].

Fig. 3. Photograph of the proposed antenna; (a) front view and (b) bottom view.

Fig. 4. Comparison of simulated and measured VSWR of the proposed antenna.

F=3.5GHz

F=5.5GHz
Fig. 5. Measured radiation patterns at (a) yz-plane and (b) xy-plane.

Fig. 6. Measured radiation efficiency of the proposed antenna.

Fig. 7. Measured gain of the proposed antenna.
IV. CONCLUSIONS

A novel compact printed microstrip-fed monopole antenna with band-notched characteristics has been proposed for UWB applications. We showed that by embedding co-directional hexagon complementary split-ring resonators slots with proper dimensions and position in the radiation pattern, triple more resonances are excited, and as a result, wide impedance bandwidth from 2.4 GHz to 11.8 GHz is achieved, and also a rejection band around 3.68 GHz – 4.25 GHz, 5.05 GHz – 5.38 GHz, 5.7 GHz – 6.12 GHz can be achieved with the wave shape structures on the backside of the substrate. The designed antenna has a simple configuration and easy fabrication process. The experimental results show that the realized antenna with a very compact size, simple structure, and wide bandwidth can be a good candidate for UWB application. Therefore, the results of the work are useful for short-range wireless communication systems.

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REFERENCES


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Disc-Shaped Monopole Antenna with Dual Band-Notched Function for UWB Applications

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Abstract — In this paper, we present a novel design of dual band-notched printed monopole antenna for UWB applications. By cutting an anchor-shaped slit in the disc-shaped radiating patch a single frequency band-stop performance can be achieved, also in order to create dual band-notched function, we use a T-shaped strip protruded inside a rectangular slot in the ground plane that with this design, a dual band-notched operation has been obtained. Simulated and measured results obtained for this antenna show that the proposed monopole antenna offers two notched bands, covering all the 5.2/5.8 GHz WLAN, 3.5/5.5 GHz WiMAX and 4 GHz C bands range. Good antenna gains and radiation behavior within the UWB frequency range have also been obtained. The antenna has a small dimension of 12×18 mm².

Index Terms — Anchor-shaped slit, disc-shaped radiating patch, dual band-notched function, T-shaped protruded strip structure, and ultra wide band (UWB) systems.

I. INTRODUCTION

In UWB communication systems, one of the key issues is the design of a compact antenna while providing wideband characteristic over the whole operating band. Consequently, a number of printed monopole antennas with different geometries have been experimentally characterized and automatic design methods have been developed to achieve the optimum planar shape. Moreover, other strategies to improve the impedance bandwidth have been investigated [1-4]. The frequency range for UWB systems between 3.1 GHz to 10.6 GHz will cause interference to the existing wireless communication systems, such as, the wireless local area network (WLAN) for IEEE 802.11a operating in 5.15 GHz – 5.35 GHz and 5.725 GHz – 5.825 GHz bands, WiMAX (3.3 GHz – 3.6 GHz) and C-band (3.7 GHz – 4.2 GHz), so the UWB antenna with a single and dual band-stop performance is required. Lately to generate the frequency band-notch function, modified planar monopoles several antennas with band-notch characteristic have been reported [5-7]. In [5], and [6], different shapes of the slots (i.e., SIR and folded trapezoid) are used to obtain the desired band notched characteristics. Half wavelength U-shaped slots are embedded in the radiating patch to generate the single and multiple band-notched functions [7].

In this paper, a novel and compact microstrip-fed monopole antenna with dual band-notched characteristic for UWB applications has been designed and manufactured. In the proposed structure, single frequency band-notched characteristics is obtained by applying the anchor-shaped slit in the disc-shaped radiating patch and also by creating the T-shaped strip protruded inside the rectangular slot in the ground plane, dual band-notched function can be provided. The dual notch bands, covering 5.02 GHz – 5.97 GHz WLAN band, 3.3 GHz – 3.8 GHz WiMAX, and
3.7 GHz – 4.2 GHz C-Band. Details of the proposed design and experimental results are also presented and discussed. Good return loss and radiation pattern characteristics are obtained in the frequency band of interest.

II. ANTENNA DESIGN

The presented small monopole antenna fed by a microstrip line is shown in Fig. 1, which is printed on an FR4 substrate of thickness 1.6 mm, permittivity 4.4, and loss tangent 0.018. The basic monopole antenna structure consists of a disc-shaped radiating patch, a feed line, and a ground plane. The proposed antenna is connected to a 50-Ω SMA connector for signal transmission.

![Fig. 1. Geometry of the proposed monopole antenna; (a) side view and (b) bottom view.](image)

In this study, the anchor-shaped slit in the radiating patch perturbs the resonant response and also acts as a half-wave resonant structure [8-9]. At the notch frequency, the current concentrated on the edges of the interior and exterior of this slit [8]. Additionally, based on Defected Ground Structure (DGS), the rectangular slot with a T-shaped protruded strip inside the slot act as a filtering element to create a new band-notch function of the proposed antenna, because it can create additional surface current path in the ground plane. At the notch frequency, the current flows are more dominant around the modified slot, and they are oppositely directed between the protruded strip and the ground plane [10]. As a result, the desired high attenuation near the notch frequency can be produced, in addition to the modified inverted T-shaped coupled strip.

In this work, we start by choosing the dimensions of the designed antenna. These parameters, including the substrate, are \( W_{\text{sub}} \times L_{\text{sub}} = 12 \text{ mm} \times 18 \text{ mm} \) or about \( 0.15\lambda_1 \times 0.25\lambda_1 \) at 4.2 GHz (the first resonance frequency). Next step, we have to determine the radius of the radiating patch \( R \). This parameter is approximately \( \lambda_{\text{lower}} / 4 \), where \( \lambda_{\text{lower}} \) is the lower bandwidth frequency wavelength. \( \lambda_{\text{lower}} \) depends on a number of parameters, such as the radiating patch length as well as the thickness and dielectric constant of the substrate on which the antenna is fabricated [11]. The important step in the design is to choose \( L_{\text{notch}} \) (the length of the filter). \( L_{\text{notch}} \) is set to band-stop resonate at \( 0.5\lambda_1 \), where \( L_{\text{notch}} = R + 0.5[\pi \times (R_1 + R_2)] \), and \( L_{\text{notch}} = 0.5W_5 + W_1 + L_5 + L_T + W_T \), \( \lambda_{g1} \) and \( \lambda_{g2} \) correspond to the notched band frequencies wavelength (3.8 GHz is the first notched frequency and 5.5 GHz is the second notched frequency). The optimized values of the proposed antenna design parameters are as follows:

\[
W_{\text{sub}} = 12 \text{ mm}, \quad L_{\text{sub}} = 18 \text{ mm}, \quad h_{\text{sub}} = 1.6 \text{ mm}, \quad W_f = 2 \text{ mm}, \quad L_f = 3.5 \text{ mm}, \quad R = 10 \text{ mm}, \quad R_1 = 4.75 \text{ mm}, \quad R_2 = 4.5 \text{ mm}, \quad W_1 = 0.5 \text{ mm}, \quad L_1 = 1.5 \text{ mm}, \quad W_2 = 4 \text{ mm}, \quad W_5 = 10 \text{ mm}, \quad L_5 = 1.75 \text{ mm}, \quad W_1 = 4.5 \text{ mm}, \quad W_T = 9.5 \text{ mm}, \quad L_T = 0.75 \text{ mm}, \quad W_T = 4.25 \text{ mm}, \quad L_{\text{gnd}} = 0.5 \text{ mm}, \quad \text{and} \quad L_{\text{gnd}} = 3.5 \text{ mm}.
\]

III. RESULTS AND DISCUSSIONS

The proposed microstrip-fed monopole antenna with various design parameters were
constructed, and the numerical and experimental results of the input impedance and radiation characteristics are presented and discussed. The Ansoft simulation software high-frequency structure simulator (HFSS) [12] version 13, with frequency sweep from 2 GHz to 12 GHz, is used to optimize the design and agreement between the simulation and measurement is obtained. The parameters of this proposed antenna, such as $W_2$ and $W_3$, are studied by changing one parameter at a time and also changing the others. In the HFSS by default, the antenna excited by wave port that is renormalized to a 50-Ohm full port impedance. The proposed antenna is connected to a 50-Ohm SMA connector for signal transmission.

The structure of various antennas used for simulation studies is shown in Fig. 2. Return loss characteristics for the ordinary disc-shaped monopole antenna (Fig. 2 (a)), disc-shaped monopole antenna with anchor-shaped slit (Fig. 2 (b)), and the proposed antenna structure (Fig. 2 (c)) are compared in Fig. 3. As shown in Fig. 3, to generate single frequency band-notched function (3.3/4.2 GHz), we insert anchor-shaped slit in the radiating patch of the ordinary disc-shaped monopole antenna, and also by using a rectangular slot with a T-shaped protruded inside the rectangular slot in the ground plane, the dual band-notch function can be achieved, that covering all the 5.2/5.8 GHz WLAN, 3.5/5.5 GHz WiMAX and 4-GHz C band. Also the input impedance of the proposed monopole antenna structure that is shown in Fig. 1, on a Smith chart is shown in Fig. 4.

![Smith Chart](image)

**Fig. 4. Smith chart demonstration of the simulated input impedance for the proposed antenna.**

In order to know the phenomenon behind this additional resonance performance, the simulated current distributions on the patch for the proposed antenna at 3.8 GHz are presented in Fig. 5 (a). It can be observed in Fig. 5 (a), that the current is concentrated on the edges of the interior and exterior of the anchor-shaped slit at 3.8 GHz. Another important design parameter of this structure is the rectangular slot with a T-shaped protruded strip inside the rectangular slot, used in
the ground plane. Figure 5 (b) presents the simulated current distributions on the modified ground plane at the second notch frequency (5.5 GHz). As shown in Fig. 5 (b), at the second notch frequency the current flows are more dominant around the slot with T-shaped protruded strip. As a result, the desired high attenuation near the second notch frequency can be produced [13-14].

Figure 6 shows the conceptual equivalent circuit model for the proposed antenna, which has two RLC band-stop filters. When the current path in the T-shaped strip protruded inside the rectangular slot in the ground plane, which is equal to a half-wavelength at 5.5 GHz as shown in Fig. 6 (b), and in the anchor-shaped slit inside the disc shaped radiating patch, which is equal to a half-wavelength at 3.8 GHz as shown in Fig. 6 (c); the input impedance at the feeding point is equal to zero (short circuit).

Figure 7 shows the simulated VSWR curves with different values of $W_2$ and $W_5$. As shown in Fig. 6, when the width $W_2$ increases from 2 mm to 6.5 mm, the center of the first notch frequency decreases from 4.17 GHz to 3.26 GHz, also when the exterior width of the rectangular slot $W_5$ increases from 8 mm to 11 mm, the center of the second notch frequency decreases from 5.93 GHz to 4.79 GHz. From these results, we can conclude that the centers of the notch frequencies are controllable by changing these parameters [15].
The proposed antenna was built and tested. The measured and simulated VSWR characteristics of the proposed antenna are shown in Fig. 8. The fabricated antenna has the frequency band of 2.77 GHz to over 11.63 GHz with two notched-band function, covering all the 5.2/5.8 GHz WLAN, 3.5/5.5 GHz WiMAX and 4 GHz C-Band range. As shown in Fig. 8, there exists a discrepancy between the measured data and the simulated results. Figure 9 illustrates the measured radiation patterns, including the co-polarization and cross-polarization, in the H-plane (xz plane) and E-plane (yz plane). It can be seen that the radiation patterns in the xz plane are nearly omnidirectional for the three frequencies.

Figure 10 shows the effects of the anchor-shaped slit and the rectangular slot with a T-shaped protruded strip inside the rectangular slot, on the maximum gain in comparison to the same antenna without them. As shown in Fig. 10, the ordinary disc-shaped monopole antenna has a gain that is low at 3 GHz and increases with frequency. It can be observed in Fig. 10 that by using a disc-shaped radiating patch with an anchor-shaped slit and the rectangular slot with a T-shaped protruded strip inside the rectangular slot in the ground plane, two sharp decreases of maximum gain in the notched frequencies band at 3.8 GHz and 5.5 GHz are shown in Fig. 10. For other frequencies outside the notched frequency band, the antenna gain with the filters is similar to those without it.

IV. CONCLUSION

In this paper, we propose a novel design of ultra wide band monopole antenna with dual band-notch function. The presented disc-shaped monopole antenna can operate from 2.77 GHz to 11.63 GHz with two rejection bands around 3.3 GHz – 4.2 GHz and 5.01 GHz – 5.9 GHz. By inserting the anchor-shaped slit structure in the disc-shaped radiating patch a single band-stop performance can be achieved, also in order to
generate a dual band-notched function, we use the rectangular slot with a T-shaped protruded strip inside the rectangular slot in the ground plane. The proposed antenna has a simple configuration and is easy to fabricate. Simulated and experimental results show that the proposed antenna could be a good candidate for UWB applications.

Fig. 10. Maximum gain comparisons for the ordinary disc-shaped monopole antenna (simulated) and the proposed antenna (measured).

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REFERENCES
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Calculation and Analysis of Shielding Effectiveness of the Rectangular Enclosure with Apertures

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Abstract — Based on transmission line theory, an approach which combines the analytical model developed by Robinson et al. and the model which analyses the shielding effectiveness (SE) of enclosure with an off-centre aperture or aperture array is presented. The model is more general than other methods and includes the incident wave with varied polarization angles and incident angles. It is quicker to calculate the SE with this model, which on the other hand enables to investigate the effect of important design parameters on SE. This model is validated by comparing the SE predictions with those from literatures. Different aspects’ effect on the SE are investigated such as aperture dimension, enclosure dimension, position of observation point, number of apertures, polarization angles, and incident angles, etc.

Index Terms — Analytical method, numerical method, rectangular enclosure, shielding effectiveness, and transmission line theory.

I. INTRODUCTION

Shielding is a useful and simple technique in EMC field. As to common electronic equipment, its metallic enclosure usually has one or more apertures, which break the completeness of metallic enclosure. How to evaluate the shielding effectiveness (SE) of the enclosure and analyze the factors that affect the SE, becomes a practical problem.

At present, there are three kinds of methods that can be utilized to investigate the SE, including methods based on Bethe’s small hole theory, numerical methods, and analytical methods. As early as 1970’s, Mendez [1, 2] proposed an analytic shielding formulation for rectangular enclosures excited by internal sources. Using the well-known Bethe’s small hole theory [3], Mendez replaced the apertures by equivalent electric and magnetic dipoles. However, this approach is limited to small holes/apertures and is only valid for frequencies below the first resonance. To overcome the limitation of the small hole theory approximation, Wallen et al. [4] employed cavity Green’s functions to extend Mendez’s approach to include the cavity resonance region. Audone and Balma [5] also considered a similar analysis to [4] for a rectangular enclosure with an aperture using MOM along with a network formulation. However, these analyses were still limited to frequencies below the first resonance.

More recently, numerical methods such as transmission line method (TLM), finite-element method (FEM), moment method (MOM), finite-difference time-domain method (FDTD), and the hybrid methods are used in the calculation of SE [6-11]. Numerical methods can offer good accuracy over a broad frequency band but at the cost of large memory and computational time. Hence, numerical methods are severely limited when it comes to analyzing practical enclosures with large number of small holes.
Another analytical method proposed by Robinson et al. [12], is based on transmission line theory and used in the calculating of SE. Although the accuracy, this method can be only applied to simple geometries with use of approximations, while it can be used to analyze the effects of many factors on SE. The computation time and computer memory are also saved, which are very useful for the engineers that design the metallic enclosure.

In this paper, for an enclosure with apertures, an accurate aperture array admittance for use in the waveguide equivalent circuit model of Robinson et al. is presented. The enclosure is modeled as a short-circuited waveguide, the aperture array is characterized by an admittance. Additionally, the incident wave is modeled by a voltage source and free-space impedance in the equivalent circuit. Using this circuit model, SE for an off-center aperture, aperture array, high-order modes, enclosure loss, arbitrary incident angles, and polarization angles can be calculated. Then, main factors that affect the SE are analyzed, which can be referenced for the design and EMC of electronic equipment’s enclosure.

II. TRANSMISSION LINE METHOD OF CALCULATING SE OF RECTANGULAR ENCLOSURE WITH APERTURE(S)

A. Enclosure with only one aperture

Based on Robinson et al’s method [12], the enclosure with one aperture (Fig. 1 (a)) can be modeled in Fig. 1 (b). The electric shielding at a distance \( p \) from the aperture is obtained from the voltage at a point P in the equivalent circuit, while the current at P gives the magnetic shielding. The radiating source is represented by voltage \( V_0 \) and impedance \( Z_0 = 377 \Omega \), and the enclosure by the shorted waveguide whose characteristic impedance and propagation constant are \( Z_{mg} \) and \( k_{mg} \), respectively. The load impedance \( Z_l \) is included in this circuit model, which represents the loss of enclosure.

\[
Z_{oa} = 120\pi^2 \ln \left( \frac{1 + \sqrt{1 - (w_e/b)^2}}{1 - \sqrt{1 - (w_e/b)^2}} \right)^{-1} \quad (1)
\]

The effective width is given by

\[
w_e = w - \frac{5t}{4\pi} \left[ 1 + \ln \left( \frac{4\pi w}{t} \right) \right], \quad (2)
\]

where \( t \) is the thickness of enclosure wall, \( w \) is the width of the aperture.

To calculate the aperture impedance \( Z_{ap} \), we transform the load impedance \( Z_l \) at the end of the aperture in considering a distance \( l/2 \) to the centre,

\[
Z_{ap} = \frac{1}{2} C_m Z_{oa} \left( \frac{Z_j + jZ_{oa} \tan(k_{oa}l/2)}{Z_{oa} + jZ_j \tan(k_{oa}l/2)} \right) \quad (3)
\]

Figure 2 shows the coordinate system of the aperture, where \( l \) and \( w \) are the length and width of the aperture, respectively. \( X \) and \( Y \) are the aperture positions from the origin to the centre of the aperture, respectively. According to field continuity at the aperture, the coupling coefficient \( C_m \) [14] is introduced to account for higher-order modes and the coupling between the aperture and the enclosure, so the SE for off-centre aperture and higher order modes can be calculated.
In many studies, the enclosure is modeled as a perfect conductor, whose conductivity is infinite, then \( Z_l = 0 \). But for a practical material, its impedance should be described as
\[
Z_l = (1 + j) \frac{\sqrt{\mu_1} / \sigma_1}{f},
\]
where \( \mu_1 \) and \( \sigma_1 \) are magnetic permeability and conductivity of the enclosure, respectively.

Based on Thevenin’s theorem, combining \( Z_0, V_0 \) and \( Z_{ap} \) gives an equivalent voltage and its impedance
\[
\frac{V_1}{Z_1} = \frac{V_0}{Z_0 + Z_{ap}},
\]
where \( k_{ap} \) is the number of apertures. Equation (17) shows that the aperture array’s impedance is the sum of that of each aperture. By replacing \( Z_{ap} \) in section A with \( Z_{ap} \), the SE is derived.

(2) With an array of round apertures
Sometimes, the enclosure may have an array of round apertures, as shown in Fig. 4.

In Fig. 4, the array of apertures can be represented by an appropriate admittance. Taking the mutual coupling between apertures into account and the normalized shunt admittance for both configurations is [15, 16],

\[
SE = 20 \log \left| \frac{V_{\text{total}}}{V_p} \right| = 20 \log \left| \frac{V_0}{2V_p} \right|, \quad (15)
\]
\[
SM = 20 \log \left| \frac{I_{\text{total}}}{I_p} \right| = 20 \log \left| \frac{V_0}{2Z_0V_p} \right|, \quad (16)
\]
\[ Y_{ap} = -j \frac{3d_1 d_2 \lambda_0}{\pi d^3} + j \frac{288}{\pi \lambda_0 d^2} \sum_{m=0}^{\infty} \sum_{n=1}^{\infty} \left( \frac{\varepsilon_m n^2}{d_v} + \frac{\varepsilon_m m^2}{d_h} \right) J_1^2(X), \]

where \( \lambda_0 \) and \( Y_0 \) are the free-space wavelength and intrinsic admittance, respectively, \( d_v \) and \( d_h \) are the vertical and horizontal aperture separations assuming that aperture’s diameter \( d \) is smaller than the separations.

In equation (18), \( X = \left[ \frac{\pi d(m^2/d_v^2 + n^2/d_h^2)/2}{(m^2/d_v^2 + n^2/d_h^2)^{3/2}} \right]^{1/2} \), and the primes denote summation on even integers only, \( J_1 \) is the Bessel function of the first kind of the first order, and \( \varepsilon_{m,n} = 1 \) if \( m = 0 \) and \( n \neq 0 \) and \( 2 \) if \( m, n \neq 0 \). The second term in equation (18) can be neglected when \( d_v \), \( d_h \) and \( d \) are much smaller than the wavelength.

In Fig. 4, the effective wall impedance \( Z_{ap} \) is a fraction of \( Z_{ap} \). Using an impedance ratio concept, \( Z_{ap} \) becomes

\[ Z'_{ap} = Z_{ap} \times \frac{l \times w}{a \times b}, \]  

where \( l \) and \( w \) are the length and width of the array, respectively, and they are given by

\[ l = d / 2 + (k_1 - 1)d_v + d / 2, \]

\[ w = d / 2 + (k_2 - 1)d_v + d / 2, \]

where \( k_1 \) and \( k_2 \) are the number of apertures in length and width direction of the array, respectively. If the apertures are staggered arranged by an angle \( \beta \), then \( d_v = d_v \sin \beta \).

**C. SE for any polarization angles and incident angles plane wave**

It is worth noting that polarization angles are not considered in Robinson et al.’s method in the earlier analysis, and the plane wave is supposed as perpendicularly illuminating the enclosure wall with aperture(s).

If the plane wave is polarized at an angle \( \varphi \), then the incident plane wave \( E \) can be divided into two components, which are vertical polarization component \( E_v = E \sin \varphi \) and horizontal polarization component \( E_h = E \cos \varphi \). Based on electromagnetic theory, the electric field propagation coefficient is

\[ T = \frac{2Z_2}{Z_2 + Z_1}. \]

Equation (22) shows that when the wave illuminates a dividing boundary of two mediums, one part is reflected, and one part penetrates into the other medium. As to \( E_v \), the penetration part is calculated as follows. The equivalent impedance can be calculated as that in section A for single aperture and section B for aperture array.

When the plane wave obliquely illuminates the enclosure wall with aperture(s) at an angle \( \theta \), \( Z_2 \) in equation (22) is given by \( Z_2 = Z_{ap} / \cos \theta_T \), and \( \cos \theta_T = \sqrt{1 - (\varepsilon_1 \sin^2 \theta) / \varepsilon_2} \). Here, \( \varepsilon_1 \) and \( \varepsilon_2 \) are the electric permeability of the two mediums. When the plane wave propagates from air into the enclosure, \( \varepsilon_1 \) is the electric permeability of air, and \( \varepsilon_2 \) is the equivalent electric permeability of aperture(s), \( \varepsilon_2 = \mu_0 / Z_0^2 \). \( Z_0 \) is the equivalent magnetic permeability of the aperture(s) and it’s equivalent to that of air. \( Z_1 \) in equation (22) is given by \( Z_1 = Z_0 / \cos \theta \). Then, the vertical electric field propagation coefficient \( T_v \) is given by,

\[ T_v = \frac{2Z_2}{Z_2 + Z_1} = \frac{2Z_{ap} \cos \theta_T}{Z_0 / \cos \theta + Z_{ap} \cos \theta_T}. \]

The vertical polarization component of electric field after penetrating the aperture(s) is given by \( E'_v = T_v E_v \). As to \( E_h \), \( Z_2 \) and \( Z_3 \) in equation (22) are respectively given by \( Z_3 = Z_0 \cos \theta \) and \( Z_2 = Z_{ap} \cos \theta_T \). Then, the horizontal electric field propagation coefficient \( T_h \) is given by,

\[ T_h = \frac{2Z_2}{Z_2 + Z_1} = \frac{2Z_{ap} \cos \theta_T}{Z_0 \cos \theta + Z_{ap} \cos \theta_T}. \]

The horizontal polarization component of electric field penetrating the aperture(s) is given by \( E'_h = T_h E_h \). The equivalent circuits of the vertical polarization and horizontal polarization components of electric field propagating in the enclosure are given by Figs. 5 (a) and 5 (b), respectively.

![Fig. 5. Equivalent circuits of vertical polarization and horizontal polarization components of electric field propagating in the enclosure.](image-url)
The electric voltage at P can be calculated as that in section A. For vertical polarization and horizontal polarization components of electric field, the total voltage are respectively given by

\[ V_{v\text{total}} = \sum V_{p,m}^{v} \] and \[ V_{h\text{total}} = \sum V_{p,m}^{h} \]. Then the total voltage at P is given by

\[ V_{\text{total}} = \sqrt{(V_{v\text{total}})^2 + (V_{h\text{total}})^2} \], and the SE can be calculated using equations (15) and (16).

**III. EXAMPLE AND ANALYSIS**

Unless other specified, the simulation parameters are characterized as: the dimensions of enclosure is \(300 \times 120 \times 300 \text{ mm}^3\), thickness of enclosure wall made of copper is \(t = 1.5 \text{ mm}\). The coordinate of observation point P is \(x = 225 \text{ mm}, y = 60 \text{ mm}\) and \(z = 140 \text{ mm}\). The plane wave perpendicularly illuminates the enclosure wall with aperture(s).

**A. Single aperture case**

For the validation of the proposed method, we consider a rectangular aperture, whose dimensions are \(50 \times 5 \text{ mm}^2\) (unless other specified, the aperture dimensions in the following is stationary). From Fig. 6, it can be observed that the calculated result using the proposed method is in well agreement with the results from [17].

\[ f = \frac{1}{2\sqrt{\mu\varepsilon}} \left( \frac{m}{a} \right)^2 + \left( \frac{n}{b} \right)^2 + \left( \frac{l}{c} \right)^2 \], \hspace{1cm} (25)

where \(m, n, l\) are determined by the wave modes in the enclosure. Using equation (25), we can get the resonance frequency point is 707 MHz for TE\(_{101}\) mode, and 1.12 GHz for TE\(_{201}\) mode. Based on microwave theory, it is known that the SE at resonance frequency will become negative which leads to the least value of SE.

(2) **Effect of enclosure dimension on SE**

The thickness of enclosure wall is \(1 \text{ mm}\), Fig. 8 shows SE for different enclosure dimensions.

\[ f = \frac{1}{2\sqrt{\mu\varepsilon}} \left( \frac{m}{a} \right)^2 + \left( \frac{n}{b} \right)^2 + \left( \frac{l}{c} \right)^2 \], \hspace{1cm} (25)

where \(m, n, l\) are determined by the wave modes in the enclosure. Using equation (25), we can get the resonance frequency point is 707 MHz for TE\(_{101}\) mode, and 1.12 GHz for TE\(_{201}\) mode. Based on microwave theory, it is known that the SE at resonance frequency will become negative which leads to the least value of SE.

**Fig. 7. Effect of aperture dimensions on SE.**

**Fig. 8. Effect of enclosure dimensions on SE.**

Using equation (25), we can deduce that in the frequency band of 0~1.2 GHz, the three enclosures all have two resonance frequencies. The resonance frequencies of first enclosure are about 707 MHz and 1.12 GHz, those of the second are about 312.3 MHz and 624.6 MHz, and those of the third are about 249.9 MHz and 499.7 MHz. All the upper resonance frequencies can be found from Fig. 8. The SE is negative at resonance frequencies, and
does not change monotonously as the enclosure is enlarged.

(3) Effect of observation point’s position on SE

When the frequencies of the plane wave is \( f = 0.75 \) GHz, 0.90 GHz or 1.20 GHz, as \( p \) changes, the SE at point P is shown in Fig. 9.

![Fig. 9. Effect of observation point’s position on SE.](image)

It is shown that the SE does not change as intuition or literatures [18, 19]: the SE is better when \( p \) is larger. The SE does not monotonously reduce or increase as \( p \) changes. When the frequency of the incident plane wave is \( f = 0.75 \) GHz, there is only TE\(_{10}\) mode in the enclosure, the SE is best when \( p = 32 \) mm, and worst when \( p = 164 \) mm. When \( f = 0.90 \) GHz, there is also only TE\(_{10}\) mode in the enclosure, the SE is best when \( p = 100 \) mm, and worst when \( p = 201 \) mm. When \( f = 1.20 \) GHz, there are TE\(_{10}\) and TE\(_{20}\) modes in the enclosure, the SE is best when \( p = 128 \) mm, and worst when \( p = 216 \) mm. So we know that the SE is not only related with \( p \), but also with frequency of incident plane wave. Based on electromagnetic theory, we can get the following laws.

For the TE\(_{mn}\) or TM\(_{mn}\) mode in the enclosure, the SE is worst when

\[
p_{\text{min}} = c - i \lambda_y / 4, \quad i = 1, 3, 5, \cdots
\]

and the SE is best when

\[
p_{\text{max}} = c - i \lambda_y / 2, \quad i = 0, 1, 2, \cdots
\]

where \( \lambda_y = 2 / \sqrt{(2f / c)^2 - (m/a)^2 - (n/b)^2} \).

It can be observed that the sensitive component can be set based on the upper laws.

(4) Effect of aperture’s position on SE

Figure 10 shows the SE for the same aperture at three different positions. In conclusion, the SE of the middle aperture is the worst. The nearer the aperture is to the edge the better SE is obtained. This model allows us to determine the SE not only in the centre of the enclosure but also for any other positions, which is impossible with Robinson et al.’s model. Based on the results, electronic engineers should place apertures at the edges of the enclosure.

![Fig. 10. Effect of aperture’s position on SE.](image)

(5) Effect of enclosure wall’s thickness and material conductivity on SE

When the enclosure wall’s thickness \( t \) and material conductivity are changed, respectively, the SE are shown in Figs. 11 (a) and 11 (b). Figure 11 (a) shows that the SE is better as \( t \) is increased. This is because when \( t \) is increased, electromagnetic energy penetrating into the enclosure is decreased. But \( t \) only has a little effect on SE. Figure 11 (b) shows when increasing the material conductivity, the SE is stationary.

(6) Effect of ratio between aperture’s length and width

The thickness of enclosure wall is 1 mm. The area of aperture is 250 mm\(^2\), and the dimensions of aperture is 50 \( \times \) 5 mm\(^2\), 15.8 \( \times \) 15.8 mm\(^2\) or 5 \( \times \) 50 mm\(^2\), respectively. Figure 12 shows that SE is better when the ratio of aperture’s length and width is reduced. This is because electromagnetic energy transmitted into the enclosure is decreased when decreasing the ratio.

B. An array of apertures case

For the validation of the proposed method in the case of apertures array, we consider an enclosure with one large aperture or three smaller ones located at center of its side wall. The three
smaller apertures are identical, with dimensions of 10 \times 1.0 \text{ cm}^2\) and their vertical separation \(d\) is 2 cm. The area of the large aperture is equal to the total areas of the three apertures. Figure 13 shows that the results calculated by present method are in well agreement with the results from [20].

Fig. 13. Validation of present method for aperture array case.

(1) Effect of aperture shape on SE
Case 1: the number of rectangular apertures is \(k = 3\), and the dimensions of each aperture is 50 \times 10 \text{ mm}^2. Case 2: the number of square arrangement round apertures shown in Fig. 4 is 5 \times 3, the distance between two adjacent apertures is \(d_v = d_h = 20 \text{ mm}\), the radius of each aperture is about 5.64 mm in order to guarantee that the total area of round apertures is equivalent to that of rectangular apertures in case 1. Figure 14 shows that if the area of rectangular and round apertures are equivalent, the SE is better for round apertures.

Fig. 14. Effect of aperture shape on SE.

(2) Effect of number of round apertures on SE
An enclosure wall has an array of round apertures, when \(d_v, d_h\), and the total area of apertures \(S_1\) are stationary, only the diameter of aperture \(d\) is variable, Fig. 15 (a) shows the SE for three cases. When the area of apertures array \(S_2\) and the diameter of aperture \(d\) are stationary, only the number of apertures is variable, Fig. 15 (b) shows the SE for this case.
(a) $d_v, d_h$ and $S_1$ are stationary, only the number of apertures is variable.

(b) $S_2$ and $d$ are stationary, only the number of apertures is variable.

Fig. 15. Effect of number of round apertures on SE.

Figure 15 (a) shows that when $d_v, d_h$ and $S_1$ are stationary, by reducing the diameter of round aperture, the SE can be improved. Figure 15 (b) shows that when $S_2$ and $d$ are stationary, by reducing the distance $d_v$ and $d_h$, and increasing the number of apertures, the SE is reduced.

(3) Effect of rectangular apertures' number on SE

The enclosure has an array of rectangular apertures, and there are three cases of the array. Case 1: dimensions of aperture is $l \times w = 50 \times 5 \text{ mm}^2$, the apertures' number $k$ is variable. Case 2: total area of apertures and aperture length $l$ are stationary, aperture width $w$ and number of apertures $k$ are variable. Case 3: total area of apertures and aperture width $w$ are stationary, the aperture length $l$ and number of apertures $k$ are variable. Figures 16 (a), (b), and (c) shows the SE for the three cases, respectively.

(a) The area of single aperture is stationary, and number of apertures is variable.

(b) Total area of apertures is stationary, the width of aperture and number of apertures are variable.

(c) Total area of apertures is stationary, the length of aperture and number of apertures are variable.

Fig. 16. Effect of rectangular apertures’ number.

Figure 16 (a) shows that if the area of single aperture and ratio of aperture length and width are stationary, the SE is reduced with increasing the number of apertures. Figure 16 (b) shows that if the area of apertures and aperture length are stationary, by reducing the aperture width, the
number of apertures is increased, but the SE is not changed monotonously for this case. Figure 16 (c) shows that if the area of apertures and aperture width are stationary, by reducing the aperture length, the number of apertures is increased, then the SE is improved.

(4) **Effect of aperture array’s arrangement on SE**

There is an aperture array that contains square and round apertures, and it is arranged by two styles. The radius of round aperture is \( r = 5 \text{ mm} \), and the length of square aperture is \( w = 1 \text{ cm} \). The adjacent apertures are distant from each other. Figure 17 shows the SE is stationary when the arrangement of apertures is changed.

![Fig. 17. Effect of aperture array’s arrangement on SE.](image)

**C. Effect of polarization angles and incident angles on SE**

Suppose that there is an aperture at the center of the enclosure wall. The dimensions of the aperture are \( 100 \times 5 \text{ mm}^2 \). The frequency and incident angle \( \theta \) of incident plane wave is 700 MHz and 90\(^\circ\), respectively, when polarization angle \( \phi \) varies from 0\(^\circ\) to 88\(^\circ\), the SE is depicted in Fig. 18 (a). It can be observed that the results calculated by present method and that from [21] are consistent, which validates the proposed method.

Figure 18 (b) shows the SE for the case that polarization angle \( \phi \) of incident plane wave is 30\(^\circ\), 45\(^\circ\), and 60\(^\circ\), respectively, and incident angle \( \theta \) changes from 0\(^\circ\) to 180\(^\circ\). It’s shown that when \( \theta \) changes from 0\(^\circ\) to 90\(^\circ\), the SE is improved. When \( \theta \) changes from 90\(^\circ\) to 180\(^\circ\), the SE is reduced.

![Fig. 18. Effect of polarization angles and incident angles on SE.](image)

**IV. CONCLUSION**

In this paper, an efficient analytical approach based on Robinson et al.’s model has been presented to predict the SE of enclosures with off-centre apertures, numerous apertures, and for any polarization angles and incident angles plane wave. The calculation of the electric shielding depends on the frequency, polarization, and incident angles of the incident wave, the dimensions of the enclosure and the aperture(s), the number of apertures, the degrees of closeness, the position of aperture(s), etc. The method described in this paper has good agreement with other methods over a wide frequency range. The estimation of the SE based on the proposed method has offered a cost-effective alternative to the numerical techniques through saving computing resources. Solution time is the key advantage of the proposed model. Therefore, this study may be helpful in designing an effective shield to achieve better shielding performance.
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REFERENCES

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Multi-Resonance Monopole Antenna with Variable Band-Notch Performance for UWB Applications

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Abstract — In this paper, a novel multi-resonance monopole antenna with frequency band-notched function is presented. By cutting a pair of rotated \( \Omega \) -shaped slots in the ground, the bandwidth is improved, that achieves a fractional bandwidth with multi resonance performance of more than 160 \%. In order to achieve single band-rejected function an S-shaped parasitic structure was inserted in the ground plane and a frequency notched band of 5.03 GHz – 5.98 GHz has been received. The measured results reveal that bandwidth of proposed antenna is from 2.75 GHz to 18.73 GHz for VSWR < 2. Simulated and experimental results obtained for this antenna show that it exhibits good radiation behavior within the UWB frequency range. The designed antenna has a small size of 12×18 mm\(^2\).

Index Terms — Band-notched performance, square monopole antenna, S-shaped parasitic structure, and ultra-wideband systems.

I. INTRODUCTION

In UWB communication systems, one of the key issues is the design of a compact antenna while providing wideband characteristic over the whole operating band. Consequently, a number of planar monopoles with different geometries have been experimentally characterized [1-2]. Moreover, other strategies to improve the impedance bandwidth have been investigated [3-7].

The federal communication commission (FCC)'s allocation of the frequency range 3.1 GHz – 10.6 GHz for UWB systems, which will cause interference to the existing wireless communication systems, such as, the wireless local area network (WLAN) for operating in 5.15 GHz – 5.35 GHz and 5.725 GHz – 5.825 GHz bands. Thus, the UWB antenna with a single band-stop performance is required. Lately to generate the frequency band-notch function, several modified planar antennas with band-notch characteristic have been reported [8-11]. In [8-10], different shapes of the slits (i.e., square ring, W-shaped, and folded trapezoid) are used to obtain the desired band notched characteristics. Single and multiple half-wavelength U-shaped slits are embedded in the radiation patch to generate the single and multiple band-notched functions, respectively [11].

In this paper, a new multi-resonance small square monopole antenna with a frequency-notch function is presented. In the proposed structure, by inserting two rotated \( \Omega \) -shaped slots in the ground plane, multi-resonance characteristic can be achieved where the proposed antenna can operate from 2.75 GHz to 18.73 GHz. In order to generate a single notch function we insert an S-shaped parasitic structure in the ground plane. The designed antenna has a small size of 12×18 mm\(^2\). Good VSWR and radiation pattern characteristics are obtained in the frequency band of interest.
II. ANTENNA DESIGN

Figure 1 shows the geometry of the proposed planar monopole antenna that fed by a microstrip line, which is printed on an FR4 substrate of thickness 1.6 mm, permittivity 4.4, and loss tangent 0.018. As shown in Fig. 1, the presented antenna consists of a square radiating patch and modified ground plane with a pair of rotated \(\Omega\) -shaped slots and an S-shaped parasitic structure. The basic antenna structure consists of a square patch, a feed line, and a ground plane. The square patch has a width \(W\). The patch is connected to a feed line of width \(W_f\) and length \(L_f + L_{gnd}\). On the other side of the substrate, a conducting ground plane of width \(W_{sub}\) and length \(L_{gnd}\) is placed. The proposed antenna is connected to a 50 \(\Omega\) SMA connector for signal transmission.

In this design, to achieve a multi-resonance function and provide a bandwidth enhancement performance, two rotated \(\Omega\)-shaped slots are inserted in the ground plane. By adding an S-shaped parasitic structure in the ground plane, frequency band notch function (5.03 GHz - 5.98 GHz WLAN) is generated. Regarding defected ground structures (DGS), the creating slots in the ground plane provide an additional current path. Moreover, this structure changes the inductance and capacitance of the input impedance, which in turn leads to changes in bandwidth. The DGS applied to a microstrip line causes a resonant character of the structure transmission with a resonant frequency controllable by changing the shape and size of the slots [10]. Therefore, by cutting two rotated \(\Omega\)-shaped slots at the ground plane and carefully adjusting its parameters, much enhanced impedance bandwidth may be achieved. As illustrated in Fig. 1, the S-shaped conductor-backed plane is placed under the radiating patch. The conductor-backed plane disturbs the resonant response and also acts as a parasitic half-wave resonant structure electrically coupled to the square monopole [9]. At the notch frequency, the current flows are more dominant around the parasitic element, and they are oppositely directed between the parasitic element and the radiation patch. As a result, the desired high attenuation near the notch frequency can be produced. The variable band-notch characteristics can be achieved by carefully choosing the parameter \(W_S\) and \(L_S\) for the S-shaped conductor-backed plane. In this structure, the length \(W_S\), is the critical parameter to control the filter bandwidth. On the other hand, the center frequency of the notched band is insensitive to the change of \(W_S\). The resonant frequency of the notched band is determined by \(L_S\).

In this work, we start by choosing the dimensions of the designed antenna. These parameters, including the substrate, is \(W_{sub} \times L_{sub} = 12 \text{ mm} \times 18 \text{ mm}\) or about 0.15 \(\lambda\) \(\times\) 0.25 \(\lambda\) at 4.2 GHz (the first resonance frequency). We have a lot of flexibility in choosing the width of the radiating patch. This parameter mostly affects the antenna bandwidth. As \(W_f\) decreases, so does the antenna bandwidth, and vice versa. Next step, we have to determine the length of the radiating patch \(L_f\). This parameter is approximately \(\lambda_{lower}/4\), where \(\lambda_{lower}\) is the lower bandwidth frequency wavelength. \(\lambda_{lower}\) depends on a number of parameters such as the radiating patch width as well as the thickness and dielectric constant of the substrate on which the antenna is fabricated [12]. The important step in the design is to choose \(L_{resonance}\) (the length of the resonators), \(L_{notch}\) (the length of the filter). \(L_{resonance}\) is set to resonate at 0.25\(\lambda_S\), where \(L_{resonance_3} = 2(L_X - L_{X1}) + W_{X1} + W_{X2}\), and \(L_{resonance_4} = L_{X1} + W_X\). \(\lambda_g\) corresponds to the resonance frequencies wavelength (11.2 GHz is the third resonance frequency and 17.1 GHz is the fourth resonance frequency). \(L_{notch}\) is set to band-stop resonate at 0.5\(\lambda_g\), where \(L_{notch} = L_{X1} + W_S + 2W_{S1}\). \(\lambda_g\) corresponds to notched band frequency wavelength (5.5 GHz is the notched frequency).

The optimized values of the proposed antenna design parameters are as follows: \(W_{sub} = 12\text{ mm}, L_{sub} = 18\text{ mm}, h_{sub} = 1.6\text{ mm}, W_f = 2\text{ mm}, L_f = 3.5\text{ mm}, W = 10\text{ mm}, W_S = 1.25\text{ mm}, L_s = 14\text{ mm}, W_{S1} = 0.25\text{ mm}, L_{S1} = 13.5\text{ mm}, W_{S2} = 0.5\text{ mm}, W_X = 4.5\text{ mm}, L_X = 2\text{ mm}, W_{X1} = 4\text{ mm}, L_{X1} = 1.25\text{ mm}, W_{X2} = 0.25\text{ mm}, L_{X2} = 0.25\text{ mm},\) and \(L_{gnd} = 3.5\text{ mm}\).

III. RESULTS AND DISCUSSIONS

In this section, the microstrip monopole antenna with various design parameters were constructed, and the numerical and experimental results of the input impedance and radiation characteristics are presented and discussed. The proposed microstrip-fed monopole antenna was fabricated and tested to demonstrate the effect of the presented. The parameters of this proposed
antenna are studied by changing one parameter at a time and fixing the others. Ansoft HFSS simulations are used to optimize the design and agreement between the simulation and measurement is obtained [13].

The configuration of the various antennas structures were shown in Fig. 2. VSWR characteristics for ordinary square patch antenna, square antenna with two rotated $\Omega$-shaped slots in the ground plane and the proposed antenna structure are compared in Fig. 3. As shown in Fig. 3, it is observed that the upper frequency bandwidth is affected by using a pair of rotated $\Omega$-shaped slots in the ground plane and the notch frequency, which is sensitive to the S-shaped parasitic structure.

To understand the phenomenon behind this multi resonance performance, the simulated current distributions on the ground plane for the square antenna with two rotated $\Omega$-shaped slots at 11.2 GHz and 17.1 GHz are presented in Figs. 4 (a) and (b). It can be observed in Figs. 4 (a) and (b) that the current is concentrated on the edges of the interior and exterior of the two rotated $\Omega$-shaped slots. Therefore, the antenna impedance changes at these frequencies due to the resonant properties of the rotated $\Omega$-shaped slots. It is found that by using these slots, third and fourth resonances are generated at 11.2 GHz and 17.1 GHz, respectively [14]. Another important design parameter of this structure is the S-shaped parasitic structure used in the ground plane. Figure 4 (c) presents the simulated current distributions on the modified ground plane at the
notch frequency (5.5 GHz). As shown in Fig. 4 (c), at the notch frequency the current flows are more dominant around of the S-shaped parasitic structure. As a result, the desired high attenuation near the notch frequency can be produced [11].

Fig. 4. Simulated surface current distributions on the ground plane for (a) the square antenna with a pair of $\Omega$-shaped slots in the ground plane at a third resonance frequency (11.2 GHz), (b) at fourth resonance frequency (17.1 GHz), and (c) for the proposed antenna at the notch frequency (5.5 GHz).

The simulated VSWR curves with different values of $L_S$ are plotted in Fig. 5. As shown in Fig. 5, when the height of the $L_S$ increases from 12.5 mm to 15 mm, the centre of the notch frequency decreases from 6.4 GHz to 4.9 GHz and from these results, we can conclude that the notch frequency is controllable by changing the interior height of the $L_S$. The simulated VSWR curves with different values of $W_S$ are plotted in Fig. 6. As shown in Fig. 6, when the width of $W_S$ increases from 0.75 mm to 2 mm, the filter bandwidth has a various size and with $W_S = 1.25$ mm, we provide a good bandwidth of the notch frequency.

The simulated input signal and impulse response for the proposed antenna is shown in Fig. 7. A first-order Rayleigh pulse is used as the source signal to drive the transmitter [8]. One of the characteristics of UWB signals is pulse distortion, which is inherently determined by their huge bandwidth. Good impedance matching over the operating frequency band is desired to minimize the reflection loss and to avoid pulse distortion [8]. Therefore, the signal distortions shown in Fig. 7 are mainly due to the bandwidth mismatch between the source pulse and the antenna. As a result, some frequency components of the pulse cannot be transmitted effectively by the monopole, leading to the distortions of the received signal.

Fig. 5. Simulated VSWR characteristics for the proposed antenna with different values of $L_S$.

Fig. 6. Simulated VSWR characteristics for the proposed antenna with different values of $W_S$.

Fig. 7. Simulated time-domain analysis (input signal and impulse response).
A prototype of the proposed monopole antenna was fabricated and tested in the antenna laboratory at the Microwave Technology Company (MWT), and the VSWR were measured using an HP 8720ES network analyzer in an anechoic chamber. The measured and simulated VSWR characteristics of the proposed antenna are shown on Fig. 8. The fabricated antenna has a frequency band of 2.75 GHz to over 18.73 GHz with notched-band function around 5.03-5.98. As shown in Fig. 8, there exists a discrepancy between measured data and simulated results.

The radiation patterns have been measured inside an anechoic chamber using a double-ridged horn antenna as a reference antenna placed at a distance of 2 m. Figure 9 illustrates the measured radiation patterns, including the co-polarization and cross-polarization, in the H–plane (x-z plane) and E-plane (y-z plane). It can be seen that the radiation patterns in the x-z plane are nearly omnidirectional for three frequencies.

![Fig. 8. Measured and simulated VSWR for the proposed antenna.](image1)

![Fig. 9. Measured radiation patterns of the proposed antenna at (a) 4 GHz, (b) 7 GHz, and (c) 10 GHz.](image2)

IV. CONCLUSION

In this paper, we present a novel multi-resonance microstrip-fed square monopole antenna for UWB applications with band-notch performance. The proposed antenna can operate from 2.75 GHz to 18.73 GHz with WLAN...
rejection band around 5.03 GHz – 5.98 GHz. In order to enhance the bandwidth we cut two rotated \( \Omega \)-shaped slots in the ground plane, and also by inserting an S-shaped parasitic structure, a frequency band-notch function can be achieved. The designed antenna has a small size of 12\( \times \)18 mm\(^2\). Simulated and experimental results show that the proposed antenna could be a good candidate for UWB application.

Fig. 10. Maximum gain comparisons for the ordinary monopole antenna (simulated), and the proposed antenna (measured) in the z-axis direction (x-z plane).

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REFERENCES
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High-Resolution and Jamming-Resistant Adaptive Synthetic Aperture Radar Imaging System based on UWB-OFDM Waveform

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Abstract—A novel approach for jamming-resistant and high-resolution synthetic aperture radar (SAR) imaging technique is explored based on ultra-wideband orthogonal frequency division multiplexing (UWB-OFDM) waveform. Suitable waveforms for both friendly and hostile environment are proposed based on various random sequences and tested for SAR imaging in presence of a digital radio frequency memory (DRFM) repeat jammer. Adaptivity factor is introduced to make the system consistent in both environments. Wide-band ambiguity function (WAF) has been derived and the effect of sub-carrier composition in UWB-OFDM waveform as SAR signal is analyzed to avoid ambiguity in image reconstruction. Appropriate UWB-OFDM pulse shaping is introduced for SAR imaging in jamming scenarios and in hostile environments to solve the susceptibility of conventional linear frequency modulated (LFM) chirp signal, Gaussian pulses and any other constant pulse shape to avoid the possibility of false target introduced by jammer and to achieve secured imaging in jamming scenarios. The peak side-lobe performance is examined in terms of number of OFDM sub-carriers and sub-carrier orientation.

Index Terms—Orthogonal frequency division multiplexing (OFDM), synthetic aperture radar (SAR), SAR jamming and anti-jamming, and ultra-wideband (UWB).

I. INTRODUCTION

Synthetic aperture radar (SAR) is used to obtain high resolution images of a large target area. It involves transmitting signals at spaced intervals called pulse repetition interval (PRI). The responses at each PRI are stored and processed to reconstruct a radar image of the terrain [1]. Recently, achievement of high resolution SAR images has been investigated depending on transmission of ultra-wideband (UWB) waveform as radar signals [2]. UWB technology has double advantages: good penetration capability and high resolution target detection for radar applications [3] and [4].

Conventional LFM chirp signal experiences high susceptibility to jammer because of the linear nature of the intermediate frequency (IF). Gaussian pulse exhibits constant pulse-shape make these pulses susceptible to certain forms of deception jamming. These radars may be susceptible to certain types of jammer in scenarios where multiple pulse transmissions are mandatory, as in SAR imaging. Constant pulse shape also prevents using multiple radars in same location as they could interfere with each other. Therefore, it is necessary to explore radar signals that employ wide bandwidths and have the ability to quickly adjust to any adverse situations.

Orthogonal frequency division multiplexing (OFDM) is a method of digital modulation commonly used in commercial communications, shows great potential to be used in radar pulse shaping. Although OFDM has been frequently studied and commercialized in the digital communication field, it has not so widely been studied by radar communities rather than a few efforts [5-10]. An OFDM signal consists of several orthogonal sub-carriers that are simultaneously passed over a single transmission path. Each sub-carrier contains a small portion of the entire signal bandwidth [11]. Spectral components in OFDM signals are orthogonal to each other; therefore, by
controlling the sub-carriers we can ensure that any two waveforms emitted simultaneously will have minimum interference. Essentially, the subcarriers partition the bandwidth of the signal into several smaller orthogonal blocks. The system has control over the sub-carriers and, therefore, control over the spectrum of the waveform. In radar scenarios, the spectrum can be manipulated to avoid any interference that may be introduced from hostile environments. Moreover, OFDM signals can be formed in an attempt to eliminate all forms of jamming and interference.

In some scenarios, enemy combatants may use specific electronic countermeasures (ECM) to confuse the radar by altering the radar received signal characteristics resulting in a poor reconstructed image [12]. Pulse diversity of radar signals is an effective electronic counter-countermeasures (ECCM) technique against deception jammers. Advances in sampling technology have increased sampling speed allowing for OFDM waveforms employing UWB (500 MHz and above) to be generated accurately and at relatively low costs. The wide bandwidth along with excellent pulse diversity shows clear potential for UWB-OFDM signal to be used as radar pulse in jamming scenarios. The advantages of using OFDM waveform in radar application are: a) waveforms are generated digitally with pulse-to-pulse shape variation, b) ease of jamming/interference mitigation, and c) noise-like waveforms provide low probability of interception (LPI) and low probability of detection (LPD).

The structure of the paper is as follows. UWB-OFDM signal generation is described in section II, while the proposed multi-modulation technique is presented in section III. Detailed analysis of DRFM repeat jammer is discussed in section IV. Target model based on different scenarios is presented in section V. Section VI presents the comparison of auto-correlation and cross-correlation of different pulses in radar perspective. SAR imaging in jamming scenarios is investigated in section VII and wideband ambiguity function is derived in section VIII. Conclusions are provided in section IX.

II. UWB-OFDM SIGNAL GENERATION

UWB-OFDM signal is generated according to the scheme shown in Fig. 1 by randomly populating the digital frequency domain vector as, 

$$\Psi_\omega = \begin{bmatrix} \Pi_{ns} & \Pi_0 & \Pi_{ps} \end{bmatrix}$$  \hspace{1cm} (1)$$

where, $\Pi_{ps}$ and $\Pi_{ns}$ represent the positive and negative sub-carriers, respectively, whereas $\Pi_0$ represents the baseband DC value. Inverse discrete Fourier transform (IDFT) is then applied to $\Psi_\omega$ to get the discrete time domain OFDM signal as,

$$\Psi_{tx}(t) = F^{-1}[\Psi_\omega]$$ \hspace{1cm} (2)$$

Fig. 1. UWB-OFDM signal generator.

UWB-OFDM waveforms are generated using the following parameters: number of OFDM sub-carriers = 256, sampling time, $\Delta t_s = 1$ ns results in baseband bandwidth, $B_0 = 1/2\Delta t_s = 500$ MHz, dividing by a factor of two to satisfy Nyquist criterion. Observing Fig. 2 (a) we see that when $\Pi_{ps}$ is populated with all 1’s and modulation scheme is chosen as BPSK, UWB-OFDM waveform becomes a short spike i.e., delta pulse, which can provide the best possible range resolution and exact position of the target in radar application. Hardware limitations can be an obstacle to generate this waveform, however, similar performance can be achieved by employing the samples of an LFM chirp in OFDM context as shown in Fig. 2 (b). We can consider these signals for the SAR imaging in friendly environment to obtain high resolution images. However, the constant pulse shape causes the system to suffer in jamming scenarios. Figure 3 shows an UWB-OFDM waveform when $\Pi_{ps}$ populated randomly with 1’s and 0’s and modulation scheme is chosen as BPSK. It is observed that the signal is noise-like and provides a unique signal at each PRI, ideal for the SAR system in jamming scenarios.
III. RANDOM MODULATION

Random modulation or multi-modulation modem modulates and demodulates signals using multiple modulation schemes. It includes a modulation selector unit that selects respective ones of the set of modulations to modulate the signals. Figure 4 shows the block diagram of the multi-modulated UWB-OFDM signal generator. The modulation selector fixed an arbitrary M-ary PSK from $M = 2^n$ and the random data generator generates a sample between 0 to $(M-1)$. The sample is then modulated according to the selected modulation scheme and stored in a buffer. IFFT is then applied to the frequency domain vector to obtain the discrete time-domain UWB-OFDM signal.

Figure 5 shows an UWB-OFDM waveform using multi-modulation technique in which different modulation schemes are employed for the individual OFDM sub-carriers. It is observed that the signal is noise-like and provides high degree of randomness, suitable for the SAR system in hostile environments. Even jammer cannot identify the modulation scheme used in generating the waveform because the signal is inherently multi-modulated.

IV. DRFM JAMMER CONCEPTS

Deception jammers attempt to manipulate transmitted SAR signals in order to introduce false target into the reconstructed SAR image. This type of jamming can be accomplished by using a digital radio frequency memory (DRFM) repeat jammer [12] as shown in Fig. 6. The radar transmitted signal is received and converted to baseband. Analog-to-digital conversion is then performed to produce the discrete signal. A delay is then introduced to the discrete signal creating a false range offset by means of a controller and stored in memory until the next predicted PRI.
The discrete delayed signal is then passed through a digital-to-analog (DAC) converter and is mixed with an exponential at the known center frequency results in the transmitted jammer signal (received signal for radar) given by,

\[ J_{tx}(t, u) = \sum_{n=1}^{N_j} \Psi_{txj}(t - t_{dj}) \]  

(3)

where, \( t_{dj} = \frac{2}{c} \sqrt{(X_j - x_j) + (y_j - u)^2} \) denotes the jammer introduced time delay and \((x_j, y_j)\) is the position of the false target. \( X_j \) and \( u \) represents the jammer distance to swath and the synthetic aperture positions respectively while \( j = 1, 2, 3, \ldots N_j \) are the number of false target reflections at any given synthetic aperture position and \( c \) is the speed of light. The term \( \Psi_{txj} \) is the cyclic shifted version of the radar transmitted signal.

\[
\Psi_{txj}(t, u) = \sum_{n=1}^{N_a} \sigma_n \Psi_{tx}(t - t_{dn}) + J_{tx}(t, u) + \eta(t),
\]

(4)

where, \( t_{dn} = \frac{2}{c} \sqrt{(X_c - x_n)^2 + (y_n - u)^2} \) denotes the time-delay associated with the actual target position \((x_n, y_n)\) and \( X_c \) is the range distance to center of the swath. Where, \( n = 1, 2, 3, \ldots N_a \) are the number of actual target reflections at any given synthetic aperture position while \( \sigma_n \) denotes the reflectivity of the target. The term \( \Psi_{tx} \) is the radar transmitted signal and \( \eta(t) \) denotes the additive white Gaussian noise, respectively.

**V. TARGET MODEL**

In practice, reflection from a point target is not a single peak as shown in Fig. 7 (a); the radar received signal is the combination of reflection from the target and closely surrounded scatterers of radar cross section (RCS) of a target as shown in Fig. 7 (b). Other important parameters that can be considered in target model are surface clutter and free space path loss. Table 1 shows the parameters used for simulation of the point target.

Surface clutter refers to reflections of a radar signal from land, sea or any other surfaces [13]. To detect targets above the surface, the radar must be able to distinguish between clutter and the targets of interest. For example, the radar should detect targets on the ground while accounting for radar reflect ions from trees or houses. Fig. 7 (c) shows the target profile based on surface clutter.

Propagation environments have significant effects on the amplitude, phase, and shape of propagating space-time wave-fields. If we consider a system that propagates signals through free space, we can model the free space path loss as,

\[ L = \frac{(4\pi R)^2}{\lambda^2} \]  

(5)

where, \( R \) represents the one-way distance between the target and the radar in meters, and \( \lambda \) is the signal wavelength. The target profile using free space path loss is shown in Fig. 7 (d). We observe that the maximum peak of the point target decreases as the distance increases. Figure 8 shows the clutter returns based on constant gamma model for different types of surface such as flat land, rugged mountain and sea-state.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pulse repetition frequency</td>
<td>PRF</td>
<td>300 Hz</td>
</tr>
<tr>
<td>Flight Duration</td>
<td>Dur</td>
<td>3 sec</td>
</tr>
<tr>
<td>Velocity of platform</td>
<td>( V_p )</td>
<td>200 m/s</td>
</tr>
<tr>
<td>Carrier frequency</td>
<td>( f_c )</td>
<td>7.5 GHz</td>
</tr>
<tr>
<td>Distance to target area</td>
<td>( X_c )</td>
<td>1Km</td>
</tr>
<tr>
<td>Half target area width</td>
<td>( X_0 )</td>
<td>600 m</td>
</tr>
</tbody>
</table>
VI. WAVEFORM ANALYSIS

Analysis of waveforms is presented in terms of their auto-correlation function (ACF) and cross-correlation function (CCF). The auto-correlation and cross-correlation properties of the sequences used in generating the transmitted waveform play an important role in high resolution SAR imaging and in false target rejection. Cross-correlation is the measure of similarity between two different sequences and can be expressed as,

\[
R_{xy}(m) = \begin{cases} 
\sum_{n=0}^{N-m-1} x_{n+m} y_{n} m \geq 0 \\
R_{yx}^*(-m) m < 0 
\end{cases}
\]  

(6)

where, \(x_n\) and \(y_n\) are the elements of two different sequences with period \(N\). Auto-correlation shows the measure of similarity between the sequence and its cyclic shifted copy, which can be obtained from equation (6) as a special case \((x = y)\) [14].

The sequences with better auto-correlation properties provide high resolution target detection and lower cross-correlation properties provide degradation of false target. So, our objective is to find the waveform that provides the lowest cross-correlation properties among all types of sequences. The auto-correlation is measured as the correlation between the received signal and the transmitted signal while cross-correlation is measured as the correlation between received signal and transmitted signal at previous PRI. The auto-correlation and cross-correlation properties are examined for all types of UWB-OFDM pulses in the following subsections assuming a point target at the center of the target area.

Fig. 7. Target profile for (a) ideal model, (b) RCS model, (c) clutter model, and (d) path loss model.
A. Constant pulses

The delta pulse and LFM chirp shown in Figs. 2 (a) and 2 (b) before providing the highest autocorrelation as shown in Figs. 9 (a) and 9 (b), respectively with a main lobe width of 0.32 meters, which almost matches the theoretical range resolution, \( \Delta R = \frac{c}{2B_0} = 0.30 \) meters. These pulses are best suited for the SAR system in friendly environment to obtain high resolution images. However, both pulses also exhibits highest cross-correlation makes them imperfect for the SAR system in jamming scenarios.

![Fig. 8. Clutter return versus the range for (a) flat land, (b) rugged mountain, and (c) sea-state.](image)

B. Random sequences

Random sequences such as Pseudo-noise (PN) sequences, Gold sequences and Kasami sequences are used extensively in spread-spectrum communication system [14]. We can consider these sequences for noise-like UWB-OFDM waveform generation to be used as SAR transmitted pulse in jamming scenarios. The parameter used in generating the sequences is shown in Table 2. The generator polynomial has been chosen so that the balance between number of 1’s and 0’s is maintained.

The PN sequences are almost ideal when viewed in terms of their autocorrelation function as shown in Fig. 10 (a). Unfortunately, the cross-correlation between any pair of PN sequences of the same period can have relatively high peaks that are undesirable as shown in Fig. 10 (b). A particular class of PN sequences called Gold sequences provides better cross-correlation properties and is generated by modulo-2 addition of two PN sequences of the same length. The autocorrelation and cross-correlation of Gold sequences is shown in Figs. 10 (c) and 10 (d), respectively.

![Fig. 9. Point target profile for a) UWB-OFDM pulse with all sub-carriers (ACF) and b) UWB OFDM-LFM chirp (ACF).](image)

<table>
<thead>
<tr>
<th>Sequence Generator</th>
<th>Generator polynomial</th>
<th>Initial states</th>
</tr>
</thead>
<tbody>
<tr>
<td>PN</td>
<td>[53 6 2 0]</td>
<td>[53 41 28 15 1]</td>
</tr>
<tr>
<td>Gold</td>
<td>[11 2 0]</td>
<td>[11 8 4]</td>
</tr>
<tr>
<td></td>
<td>[11 8 5 2 0]</td>
<td>[11 7 3]</td>
</tr>
<tr>
<td>Kasami</td>
<td>[12 6 4 0]</td>
<td>[12 8 2 0]</td>
</tr>
</tbody>
</table>

Kasami sequences are one of the important types of binary sequences because of their very low cross-correlation. Kasami sequences provide better cross-correlation as compared to PN sequences and Gold sequences. Figures 10 (e) and 10 (f) show the ACF and CCF of Kasami sequences, respectively.
C. Orthogonal sequences

Orthogonality is the most important properties of Walsh-Hadamard sequences. Because of this property, the cross-correlation between any two codes of the same set is zero, when the system is perfectly synchronized as shown in Fig. 11. Unfortunately, these sequences have non-zero off-peak auto-correlations and cross-correlation in asynchronous case. Figures 12 (a) and 12 (c) show the auto-correlation and cross-correlation in terms of a point target using Walsh-Hadamard sequences without spreading. By spreading Walsh sequences with a PN sequence using specific spreading factor better performance can be achieved.

The spreading uses a waveform that appears random to anyone except the intended receiver of the transmitted signal. The waveform is actually pseudo-random in the sense that it can be generated by precise rules yet has the statistical properties of a truly random sequence. Figures 12 (b) and 12 (d) show the auto-correlation and cross-correlation in terms of a point target using Walsh-Hadamard sequences with spreading by a factor of 4.

D. Multi-modulated pulse

The proposed multi-modulated UWB-OFDM pulse provides reasonable auto-correlation properties with increased main-lobe width but exhibits lowest cross-correlation as shown in Fig. 13 among all types of pulses makes this pulse ideal for the SAR system for false target rejection.
Since all cross-correlation values, not just peak values, affect the system performance, we should consider the measure as the mean cross-correlation value. Figures 14 and 15 summarize the peak auto-correlation values in terms of width of the main lobe i.e., range resolution and normalized mean cross-correlation values of different pulses, respectively.

Let us consider 2 point targets as actual target at the positions \((x_n, y_n) = [(-300\,\text{m}, 80\,\text{m}), (300\,\text{m}, 80\,\text{m})]\) and 2 point target as false target introduced by jammer at the positions \((x_j, y_j) = [(-300\,\text{m}, -80\,\text{m}), (300\,\text{m}, -80\,\text{m})]\). Stripmap SAR topology is considered and UWB-OFDM waveform is used as transmitted pulse to perform the SAR raw data generation using while Range-Doppler algorithm (RDA) is used for SAR image reconstruction [15]. The details of SAR configuration can be found in [5]. Although different techniques exist in literature for SAR image reconstruction [16] RDA is chosen to achieve exact SAR transfer function.

Reconstructed SAR image with resolved point targets in jamming scenarios is shown in Fig. 16. Because of using UWB-OFDM waveform with constant pulse shape shown in Fig. 2 (a) as transmitted SAR signal at each PRI, the signal had strong correlation with the jammer transmitted signals causing both false targets presence at their respective positions in the reconstructed SAR image.

Point targets are also resolved by using UWB-OFDM waveform with random sub-carrier compositions shown in Fig. 3 as SAR transmitted pulse in jamming scenarios. Fig. 17 shows the reconstructed SAR image using a random waveform at each PRI. Because of transmitting a next expected PRI to introduce false target in reconstructed SAR image. The objective is to investigate the performance of the UWB-OFDM waveform with constant pulse, noise-like pulses based on random sequences and multi-modulated waveform as SAR transmitted pulse in jamming scenarios.
unique UWB-OFDM signal at each PRI, the signal has weaker correlation with the jammer transmitted signals causing degraded false target appears in the reconstructed SAR image. Figure 18 shows the reconstructed SAR image using a unique UWB-OFDM waveform at each PRI employing multi-modulation technique as shown in Fig. 5. Because of transmitting a unique multi-modulated UWB-OFDM signal with high degree of randomness at each PRI, the signal has much weaker correlation with the jammer signals causing no false target appears in the reconstructed SAR image.

![Fig. 16. SAR image showing two false targets.](image1)

![Fig. 17. SAR image showing degraded false targets.](image2)

![Fig. 18. SAR image without false targets.](image3)

The degradation of false targets using different sequences can be analyzed in terms of entropy [17] by analyzing SAR images i.e., degradation of false targets will have reduction in entropy of the SAR image. Figure 19 shows the degradation of the false target in terms of entropy for different sequences as well as multi-modulation technique for different adaptivity factor. The adaptivity factor is the ratio of randomness of an UWB-OFDM waveform i.e., the ratio of 0's and 1's within the data vector that is used for waveform generation and is given by,

$$\eta = \frac{N_{0s}}{N_{sub}} \times 100$$

(7)

where, $N_{0s}$ is the number of zeros in the data vector and $N_{sub}$ is the number of sub-carrier used in generating the waveform. As we are using BPSK modulation in case of random sequences, we should increase the number of 0's within the data vector to increase the adaptivity factor and vice versa.

In Fig. 19, we observe that as long as we increase the adaptivity factor, the entropy is increased. This is because the increment in the adaptivity factor increases the correlation of a pulse with the pulse at previous PRI. On the other hand, increment in the adaptivity factor increases the occupied bandwidth by the pulse, which in turns enhances the range resolution as shown in Fig. 20. We observe that multi-modulated UWB-OFDM waveform is the best choice for false target rejection but Kasami sequences exhibits a good balance between false target degradation as well as resolution among all random sequences.

![Fig. 19. Estimation of false target degradation.](image4)

UWB-OFDM waveform with constant pulse shape provides high-resolution SAR image but not effective for rejecting false target while UWB-
OFDM waveform with random sub-carrier orientation is capable of rejecting false target in jamming scenarios. On the other hand, UWB-OFDM waveform with multi-modulation technique is capable of rejecting false target completely. This waveform is evidently hardest to predict and intercept for the jammer because the signal is inherently multi-modulated. The high degree of randomness in SAR transmitted signal also rejects any reflected energy arrived from previous PRI during cross-correlation process as part of matched filtering, which in turns allow us to increase the swath. However, the trade-off is the increased target ambiguity i.e., increased main lobe width. This problem can be analyzed in terms of wide-band ambiguity function.

\[ AF_{wb}(\alpha, t) = \sqrt{|\alpha|} \int_{-T_p/2}^{T_p/2} \Psi(t) \Psi^*(\alpha(t - \tau)) \, dt \] (8)

where, \( \alpha = \frac{c-v}{c+v} \) and \( v \) is the radial velocity of the radar platform to the target and \( c \) is the speed of light. Equation (8) considers the Doppler shift of each sub-carrier individually whereas the narrowband AF considers only one sub-carrier causing incorrect Doppler shift for other sub-carriers. The continuous time analytical OFDM waveform [11] is given by,

\[ \Psi(t) = \sum_{k=1}^{N} x(k) e^{j2\pi k f_0 t} \] (9)

where, \( x(k) \) is the \( k^{th} \) data symbol, \( N \) is the number of sub-carriers and \( T_p \) is the pulse duration. By substituting the analytical form of OFDM signal into equation (8), WAF for a UWB-OFDM signal is given by,

\[ AF_{OFDM}(\alpha, \tau) = T_p \sqrt{|\alpha|} \sum_{l=1}^{N} \sum_{k=1}^{N} x(k) x(l) e^{j2\pi \Delta f \cdot \tau \cdot \text{sinc}(\pi \Delta f (k - l) T_p)} \] (10)

where, sub-carrier spacing \( \Delta f = 1/T_p \) has been substituted and \( \phi_0 = 0 \) is assumed. Equation (10) shows the dependence of the AF on not only number of sub-carrier but also the orientation of the sub-carriers in the OFDM signal.

The range ambiguity can be reduced by increasing the adaptivity factor in UWB-OFDM SAR transmitted signal and is shown in Fig. 21. The reason behind this reduction in mainlobe width is that as long as we increase the adaptivity factor, the UWB-OFDM waveform approaches to the constant pulse shape as shown in Fig. 2. Figure 22 shows that the ambiguity in cross-range decreases as the number of sub-carrier increases. Increasing the number of sub-carrier in the signal has no effect on the main-lobe width because the bandwidth remains constant for any number of sub-carriers. However, increasing the number of sub-carriers will increase the size of raw SAR data, which should be minimized for radar processing purposes to reduce the computation time.
Table 3: OFDM sub-carrier versus PSL.

<table>
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<tr>
<th>OFDM Sub-carriers</th>
<th>Peak side-lobe (dB)</th>
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</thead>
<tbody>
<tr>
<td>128</td>
<td>Adaptivity factor 60%</td>
</tr>
<tr>
<td></td>
<td>-13.24</td>
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<td></td>
<td>Adaptivity factor 70%</td>
</tr>
<tr>
<td></td>
<td>-16.14</td>
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<tr>
<td></td>
<td>Adaptivity factor 80%</td>
</tr>
<tr>
<td></td>
<td>-17.26</td>
</tr>
<tr>
<td>256</td>
<td>Adaptivity factor 60%</td>
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<tr>
<td></td>
<td>-16.02</td>
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<tr>
<td></td>
<td>Adaptivity factor 70%</td>
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<tr>
<td></td>
<td>-18.12</td>
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<td></td>
<td>Adaptivity factor 80%</td>
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<td></td>
<td>Adaptivity factor 80%</td>
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IX. CONCLUSION

Performance of UWB-OFDM based SAR imaging has been investigated in jamming scenarios. UWB-OFDM based SAR can be adapted with both friendly environments and with jamming scenarios just by changing the transmitted waveform. The adaptivity factor can be used to handle mutual exclusion between resolution and false target rejection. The performance of the SAR system in both environments can easily be controlled by changing the number and composition of the OFDM sub-carriers. Wideband ambiguity function has been derived and the effect of adaptivity factor in UWB-OFDM waveform has been analyzed. The results prove that UWB technology enhances the resolution of SAR images while randomness of noise-like OFDM waveform improves the anti-jamming capabilities of SAR system. UWB-OFDM waveform with in addition with multi-modulation technique is an excellent choice to be used as SAR transmitted pulse in hostile environments to achieve secured SAR imaging.

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REFERENCES


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